

In protoplanetary discs, micron-sized grains are known to grow to eventually reach planetesimal sizes. However, dynamical studies show that once they reach a critical size, they rapidly migrate into the accreting star. This is known as the radial-drift barrier (Weidenschilling 1977). In order to overcome this barrier, several methods have been proposed such as particles traps caused by, e.g., vortices, planet gaps, which all involve large-scale dynamics.

In this work, we choose to investigate analytically the intrinsic properties of the grains during their growth, in particular their porosity. Indeed, many objects present in the Solar System including meteorites or comets are porous.

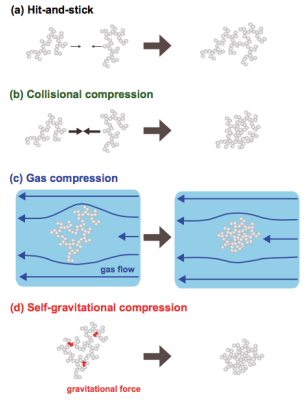
Filling factor ϕ of the grain

$$\phi = \frac{\rho}{\rho_s}$$

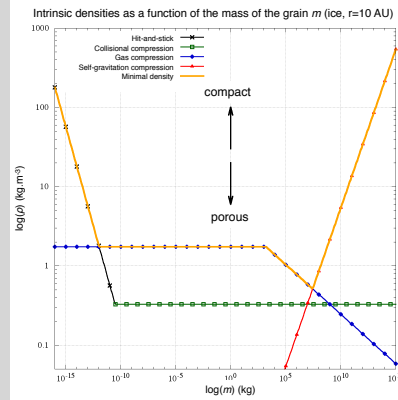
ρ : intrinsic density
(m/V_{tot})
 ρ_s : bulk density
(m/V_{compact})

0 $\xrightarrow{\phi}$ 1
 $\phi \sim 0$: highly porous grain
 $\phi = 1$: compact grain

Spherical grains
with mass m
and radius s



Kataoka et al.(2013b)



Static compression

$$\phi = \left(\frac{a_0^3}{E_{\text{roll}}} P \right)^{1/3}$$

Kataoka et al.(2013a)

a_0 : monomer size
 E_{roll} : rolling energy
 P : compressive strength

- (a) $\rho_{\text{hs}} \propto m^{-1/2}$
 (b) $\rho_{\text{coll}} \propto m^0$
 (c) $\rho_{\text{gas}} \propto \begin{cases} m^0 & (s \leq 9 \lambda/4) \\ m^{-1/4} & (s \geq 9 \lambda/4) \end{cases}$
 (d) $\rho_{\text{sg}} \propto m^{2/5}$
 λ : gas mean free path

T-Tauri disc model

$$M_* = 1 M_{\odot} \quad M_{\text{disc}} = 0.01 M_{\odot}$$

$$0.1 \leq r \text{ (AU)} \leq 300 \text{ AU}$$

$$T_g \propto r^{-3/4} \quad \Sigma_g \propto r^{-3/2}$$

$$\tau(1 \text{ AU}) = 197 \text{ K} \quad \alpha = 0.01$$

Aerodynamical parameters

Stopping time τ

Epstein: $s \leq 9 \lambda/4$ Stokes: $s \geq 9 \lambda/4$

$$\tau_{\text{Ep}} = \frac{\rho_s \phi s}{\rho_g c_g} \quad \tau_{\text{St}} = \frac{4 \rho_s \phi s^2}{9 \lambda \rho_g c_g}$$

c_g : gas sound speed

Stokes number St

$$St = \Omega_k \tau$$

Model for migration

Radial velocity:

$$\frac{dr}{dt} = \tau \frac{1}{\rho_g} \frac{dP_g}{dr} \quad St < 1$$

$$\frac{dr}{dt} = \frac{1}{\tau} \frac{1}{\rho_g} \frac{dP_g}{dr} \frac{r^3}{G M_*} \quad St > 1$$

Weidenschilling (1977)

Model for growth

Relative velocity between identical grains:

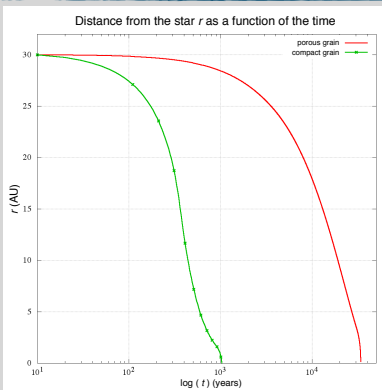
$$V_{\text{rel}}^2 = 2^{3/2} R_o \alpha c_g^2 \frac{St}{(St + 1)^2}$$

R_o : Rossby number for turbulent motions ($R_o = 3$)

Temporal variation of the mass of the grain:

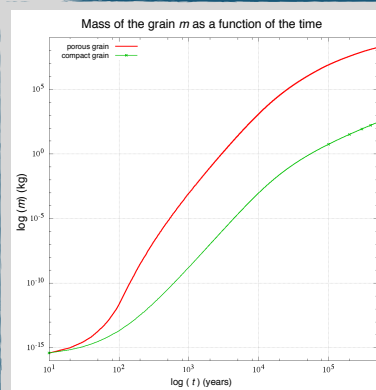
$$\frac{dm}{dt} = 4 \pi s^2 V_{\text{rel}} \rho_d$$

ρ_d : density of matter concentrated into
SPH solid particles
Stepinski & Valageas (1996)



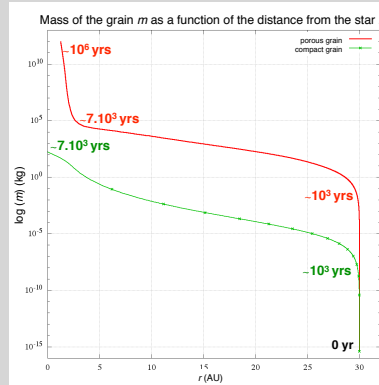
The migration is slowed
down for a porous grain
but in both cases,
the grain is accreted

Initial conditions
Icy grains, $m = 1 \text{ kg}$
 $r_i = 30 \text{ AU}$



The growth is more
efficient and quicker
for a porous grain

Initial conditions
Icy grains, $s_i = 1 \mu\text{m}$, $\phi_i = 0.1$
 $r_i = 30 \text{ AU}$



Porous grains grow faster and
migrate slower, thus they can
decouple from the gas and avoid
being accreted

Porous grains keep growing close to
the star to reach planetesimal sizes

Initial conditions
Icy grains, $s_i = 1 \mu\text{m}$, $\phi_i = 0.1$
 $r_i = 30 \text{ AU}$

