

MASS, RADIUS AND COMPOSITION OF 55 Cnc e :

Using interferometry and correlations

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INTRODUCTION

Planet parameters are never as good as star parameters are.

$$R_p = R_* \times \sqrt{D}$$

$$M_p \sin(i) = M_* K (P/2\pi GM_*)^{1/3}$$

D = transit depth

P = period

K = amplitude of RV signal



The uncertainty on M_* and R_* is often larger than that on K and D, and is too often neglected (or underestimated).

Get M_* and R_* ? From L_* and $T_{\text{eff},*}$, fit stellar evolution models.

Internal error: old vs young solution (e.g. [Bonfanti+15](#)), uncertainty.

External error: models differ. Many unknown parameters (Ω , Z ...)



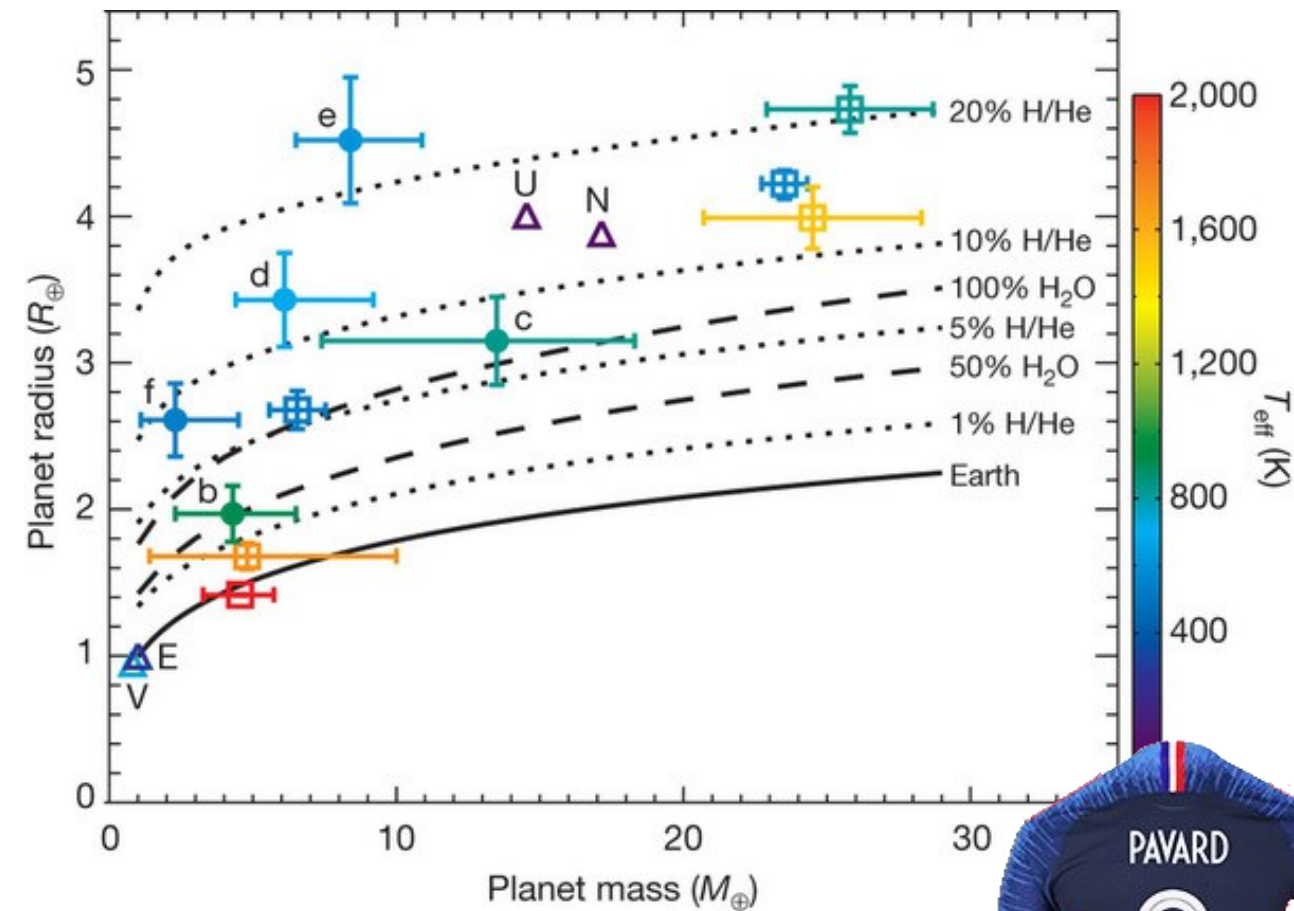
INTRODUCTION

Measure R_* directly: interferometry (e.g.: [Ligi et al. 2012, 2015, 2016](#)).

→ angular diameter θ with up to 2% precision.

This parameter constrains efficiently all the others ([Creevey et al. 2007](#)).

Here, we want to use this tool to narrow the possible radii, masses, therefore composition of transiting exoplanets.



All the next figures are for 55 Cnc.

A Bayesian approach

Observations: θ , π (parallax), $m \rightarrow F_{\text{bol}}$, the bolometric flux.

$$\left. \begin{aligned} L &= 4 F_{\text{bol}} (1 \text{ pc} / \pi)^2 \\ T_{\text{eff}} &= (4 F_{\text{bol}} / \sigma \theta)^{1/4} \end{aligned} \right\} \begin{array}{l} \text{Likelihood} \\ \text{(analytic)} \end{array}$$

$$\mathcal{L}_{HR}(L, T) = \frac{4\sqrt{\pi/\sigma_{\text{SB}}}}{L^{3/2}T^3} \times \int_0^{+\infty} t \times f_{F_{\text{bol}}}(t) \times f_{\Pi} \left(\sqrt{\frac{4\pi t}{L}} \right) \times f_{\theta} \left(\sqrt{\frac{4t}{\sigma_{\text{SB}} T^4}} \right) dt$$



A Bayesian approach

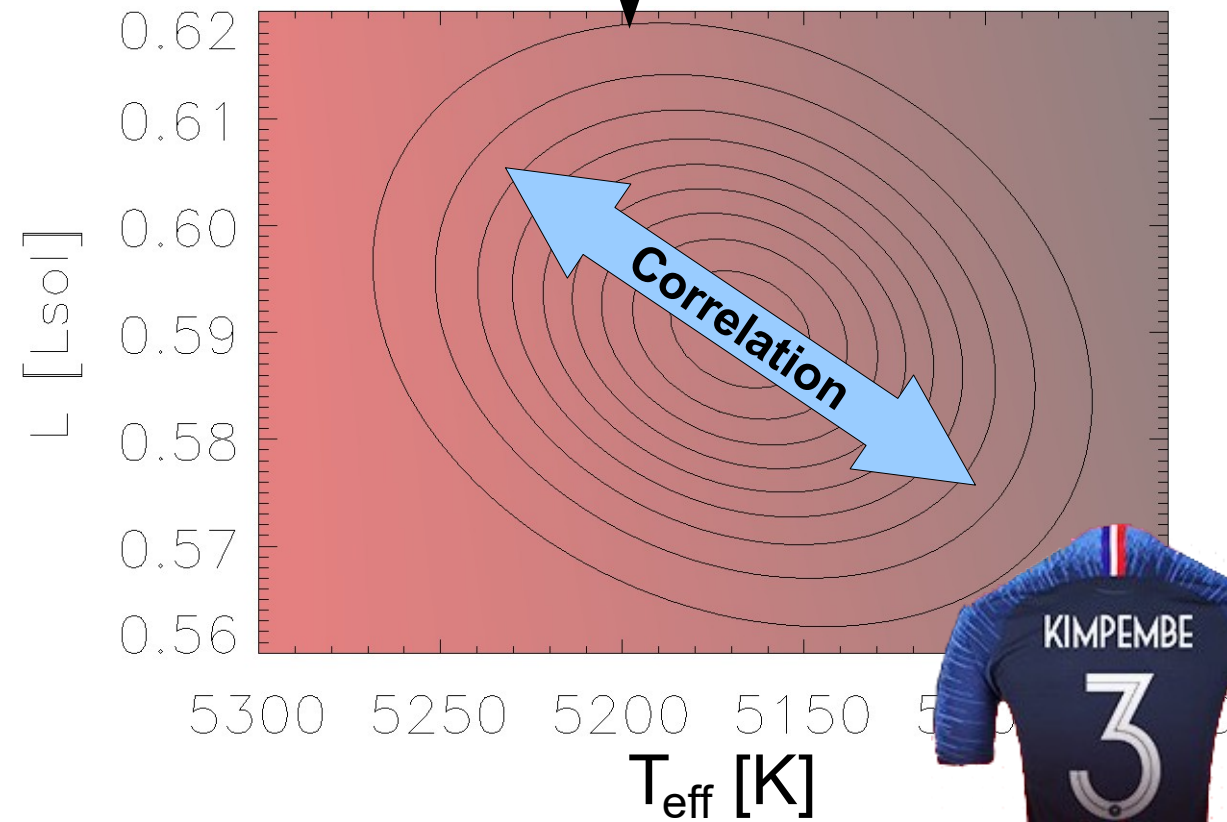
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level curves

Prior: density of stars in the HR diagram of the Hipparcos sample (color).



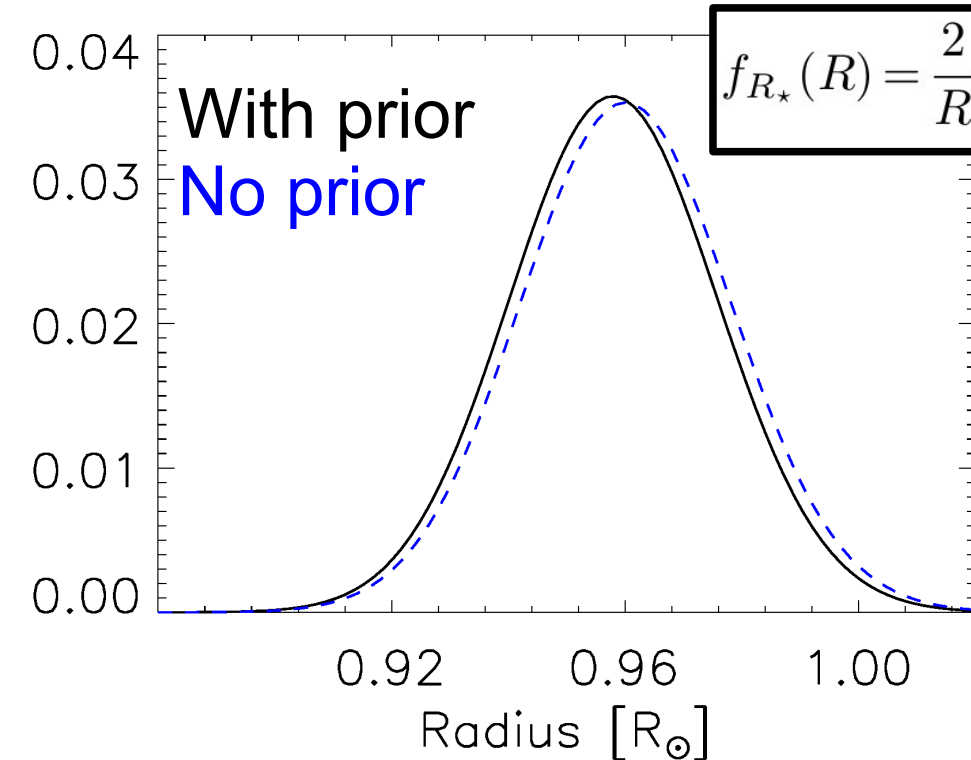
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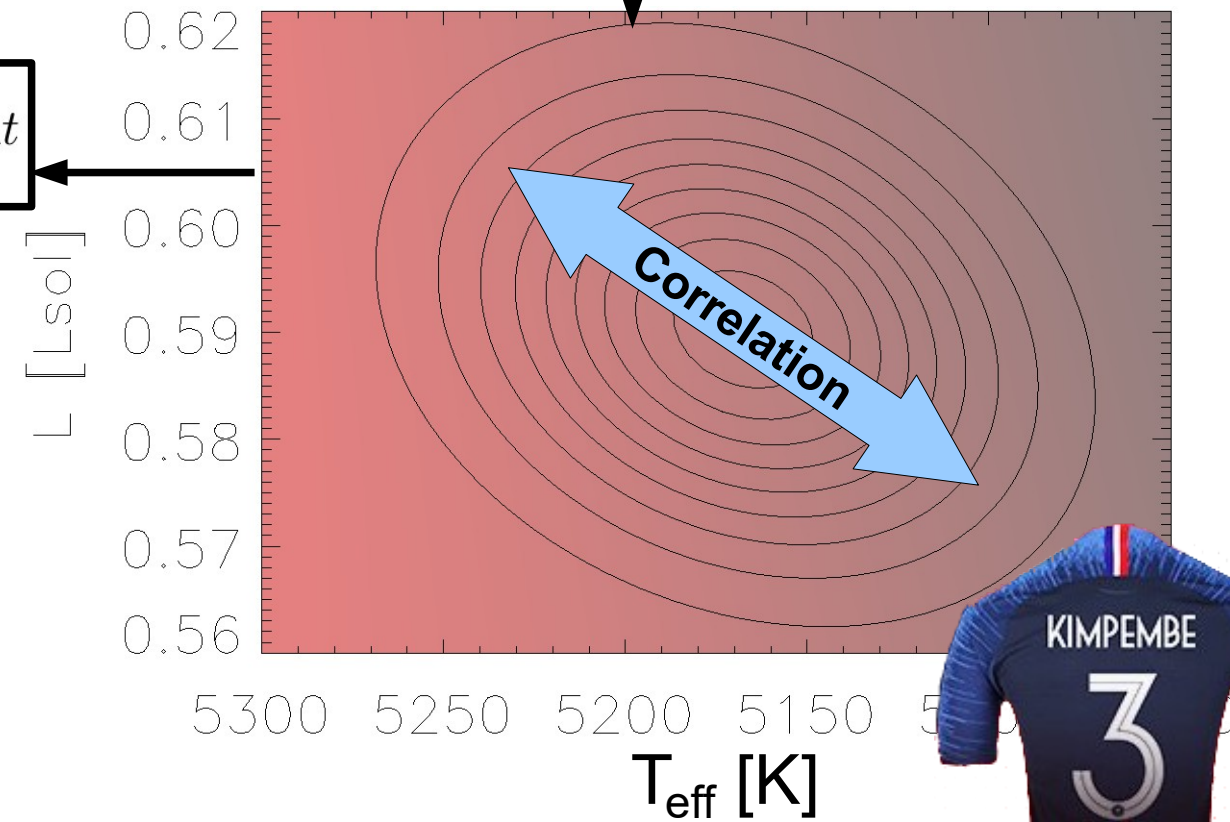
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level curves



$$f_{R_{\star}}(R) = \frac{2}{R} \int_{t=0}^{\infty} L_{(R,t)} f_{HR}(L_{(R,t)}, t) dt$$



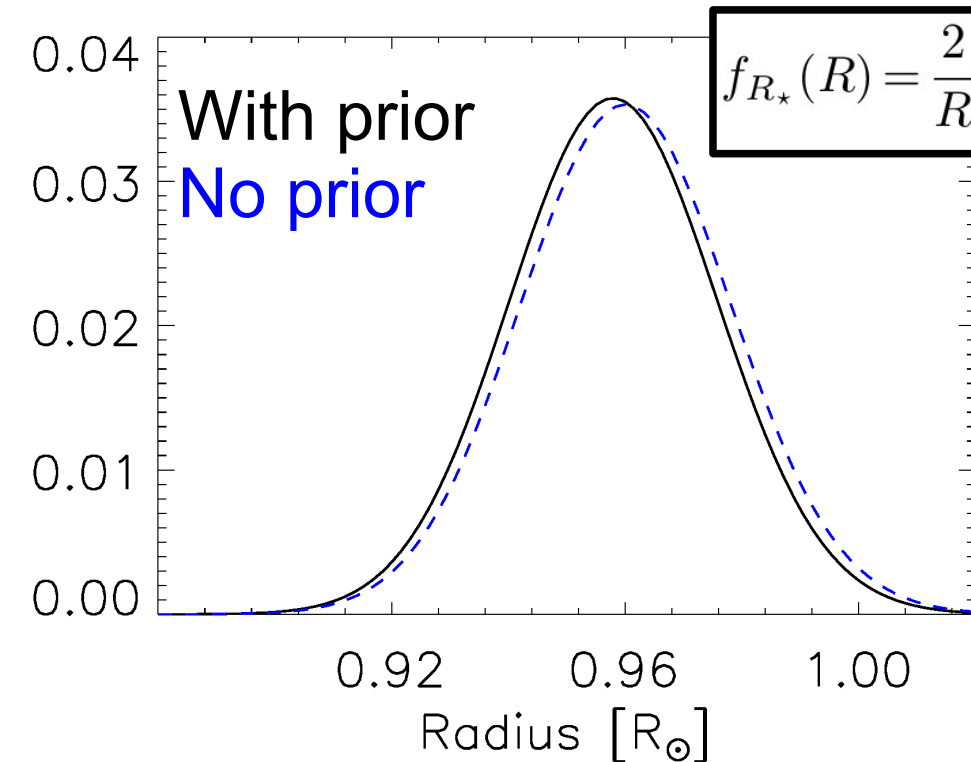
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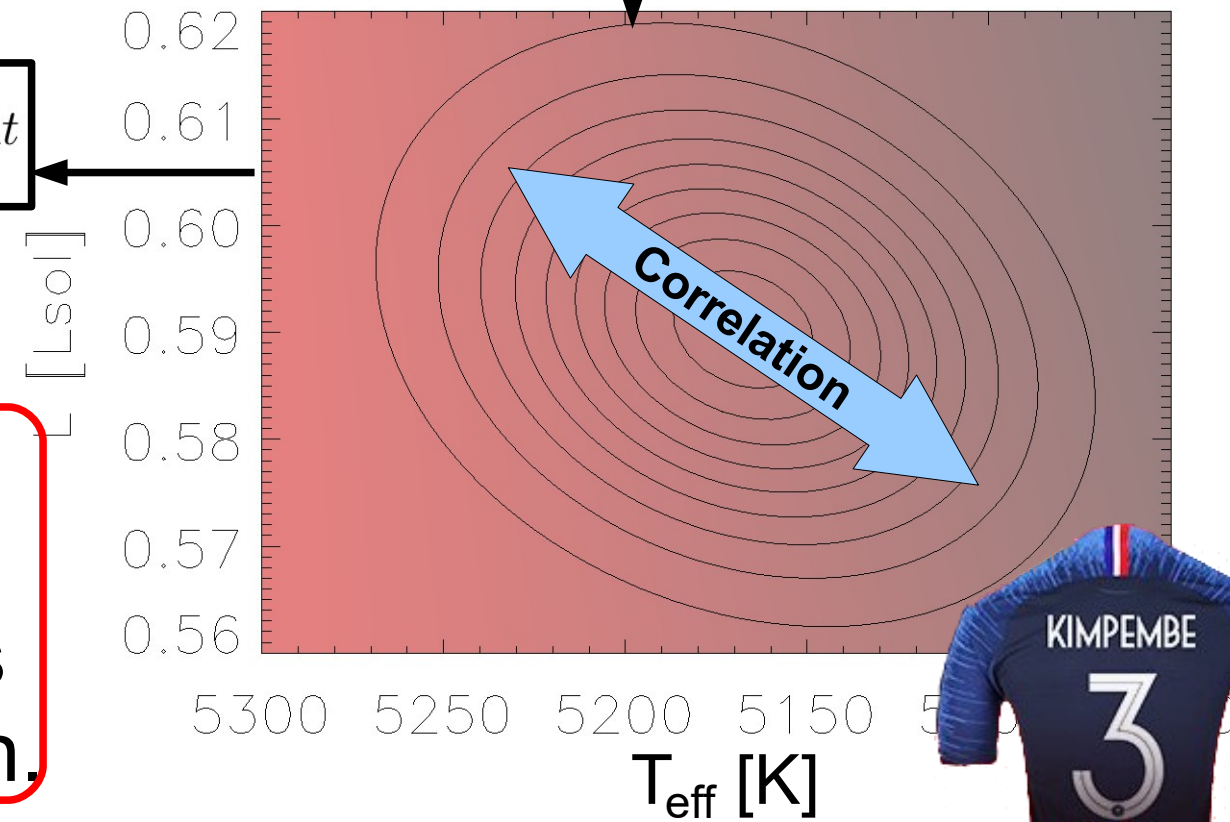
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Interferometry
is precise !
The prior does
not bring much.

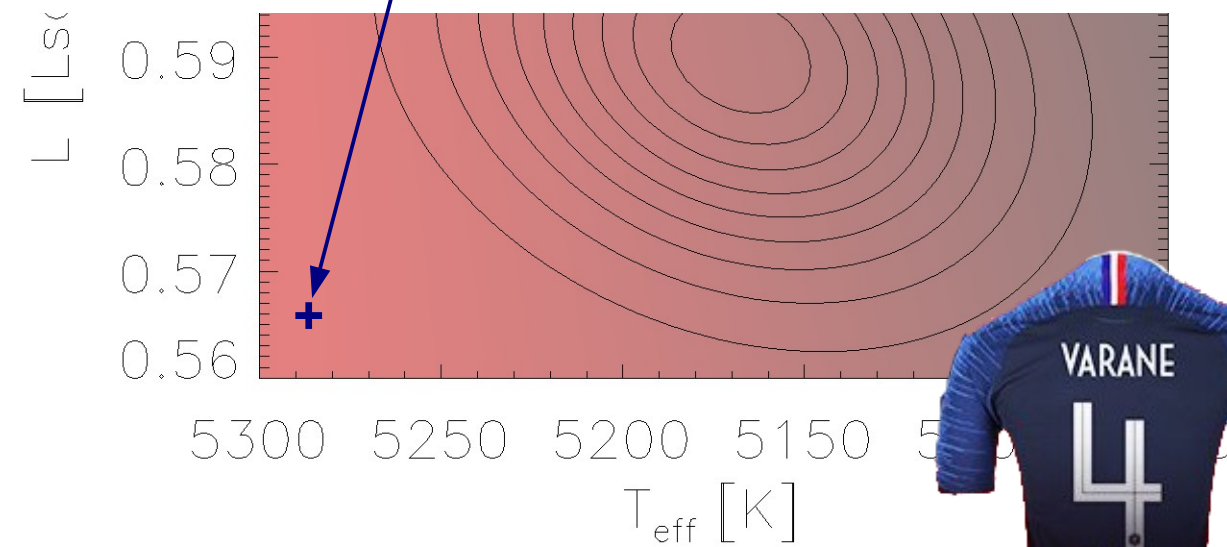
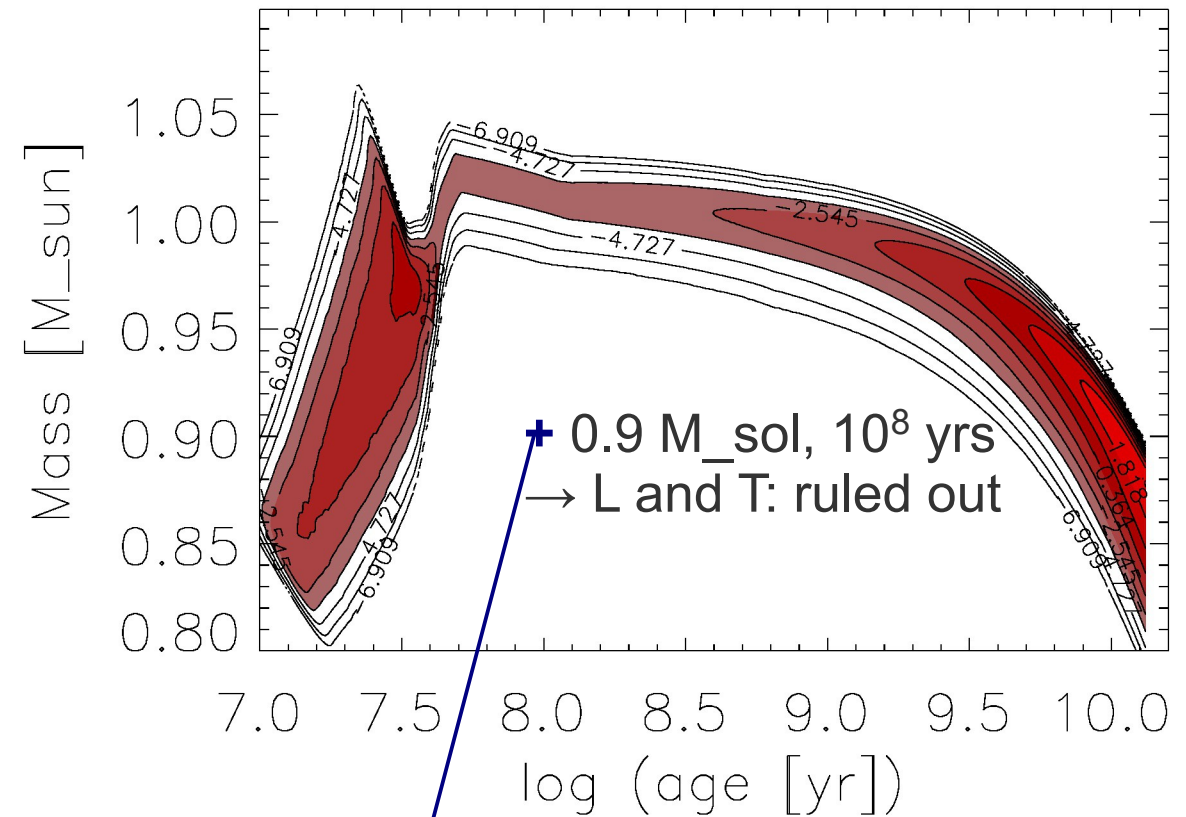


Stellar models ?

Fit stellar evolution models on the L-T distribution \rightarrow mass and age.

Results :

- a) For each model, 2 solutions (young and old, see [Ligi et al. 2016](#)).
- b) Different params in the model \rightarrow different, inconsistent solutions :
CES2MO ([Lebreton & Goupil 2014](#))
gives M_* from 0.950 ± 0.015
to $0.989 \pm 0.020 M_{\text{sun}}$.



Direct Probability Density Function : the Star

Transit duration: $T = 2 R_* / a\Omega$. Period: $P = 2\pi / \Omega$.

$\rightarrow P/T^3 = (\pi^2 G/3) \rho_*$ \rightarrow *measure* of the stellar density.
(Seager & Mallén-Ornelas 2003)



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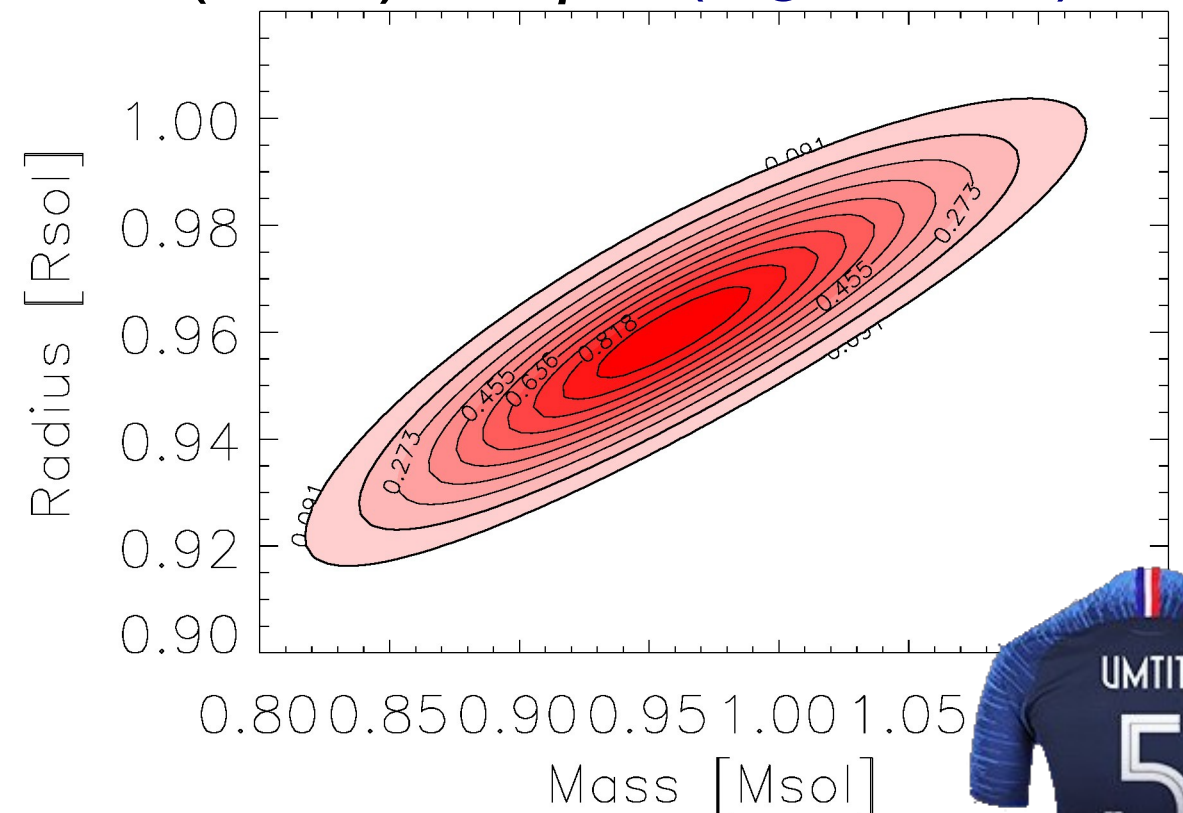
$\rightarrow P/T^3 = (\pi^2 G/3) \rho_*$ \rightarrow *measure* of the stellar density.
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Measure of R_* by interferometry $\rightarrow M_* = (4\pi/3)R_*^3 \rho_*$ (Ligi+ 2016)

From the PDF of R_* and ρ_* ,
analytic joint PDF of $M_* - R_*$.

$$\mathcal{L}_{MR_*}(M, R) = \frac{3}{4\pi R^3} \times f_{R_*}(R) \times f_{\rho_*} \left(\frac{3M}{4\pi R^3} \right)$$

- \rightarrow Strong correlation (0.85) !
- \rightarrow Different M_* than VonBraun et al. (2011) based on isochrones.



Direct Probability Density Function : the Star

Transit duration: $T = 2 R_* / a\Omega$.

Period: $P = 2\pi / \Omega$.

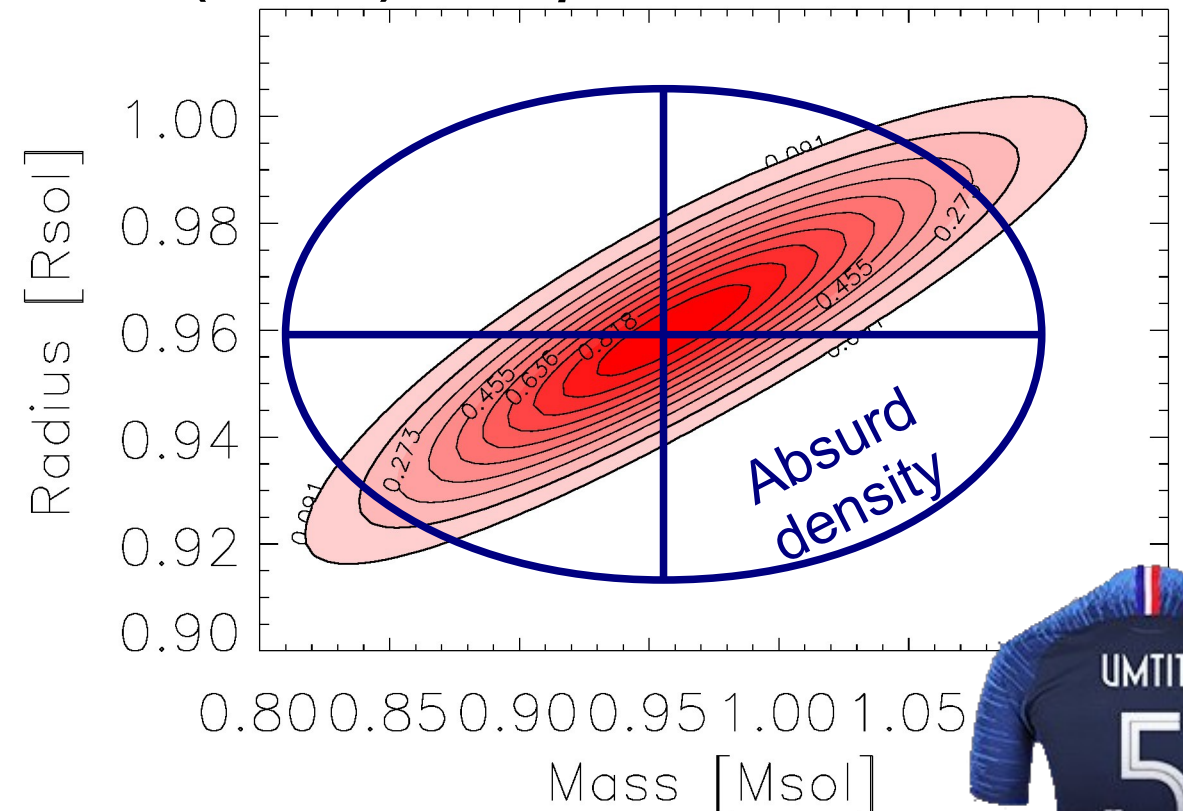
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Taking the values of M_* and R_*
directly from Ligi+16, one gets
the large, wrong, blue ellipse.



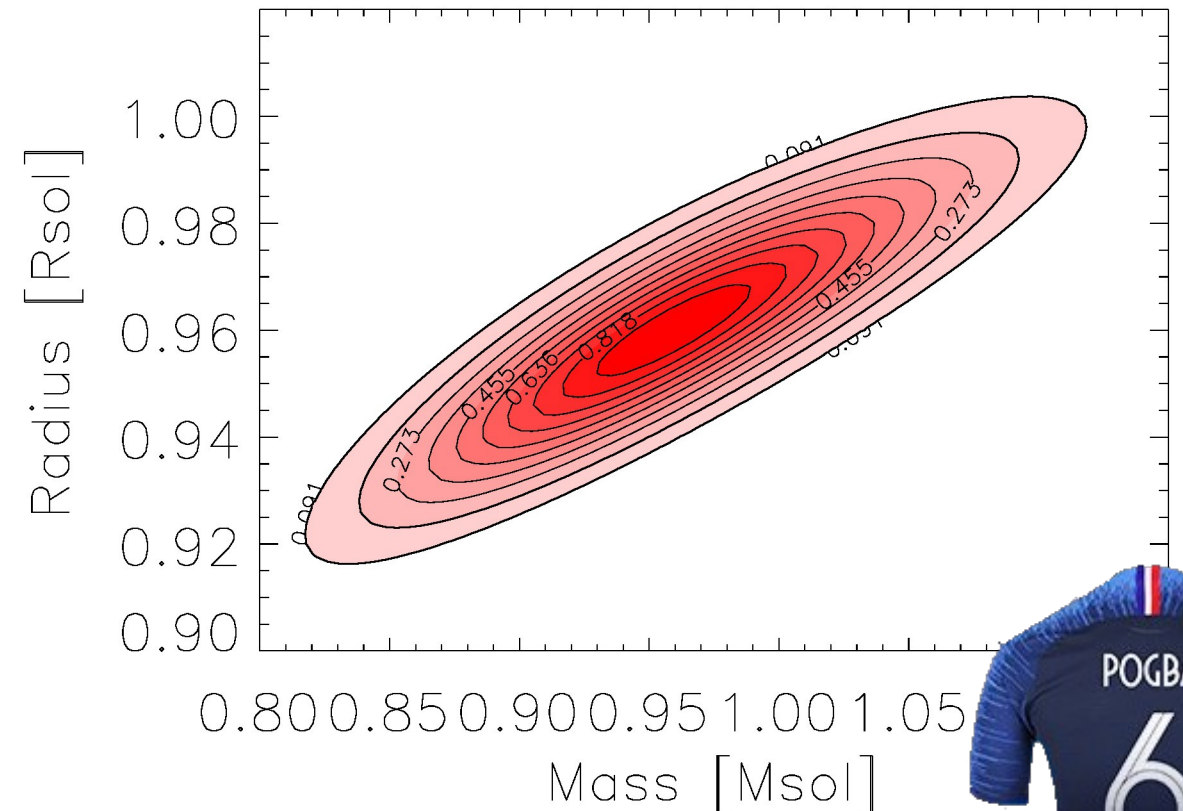
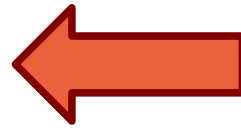
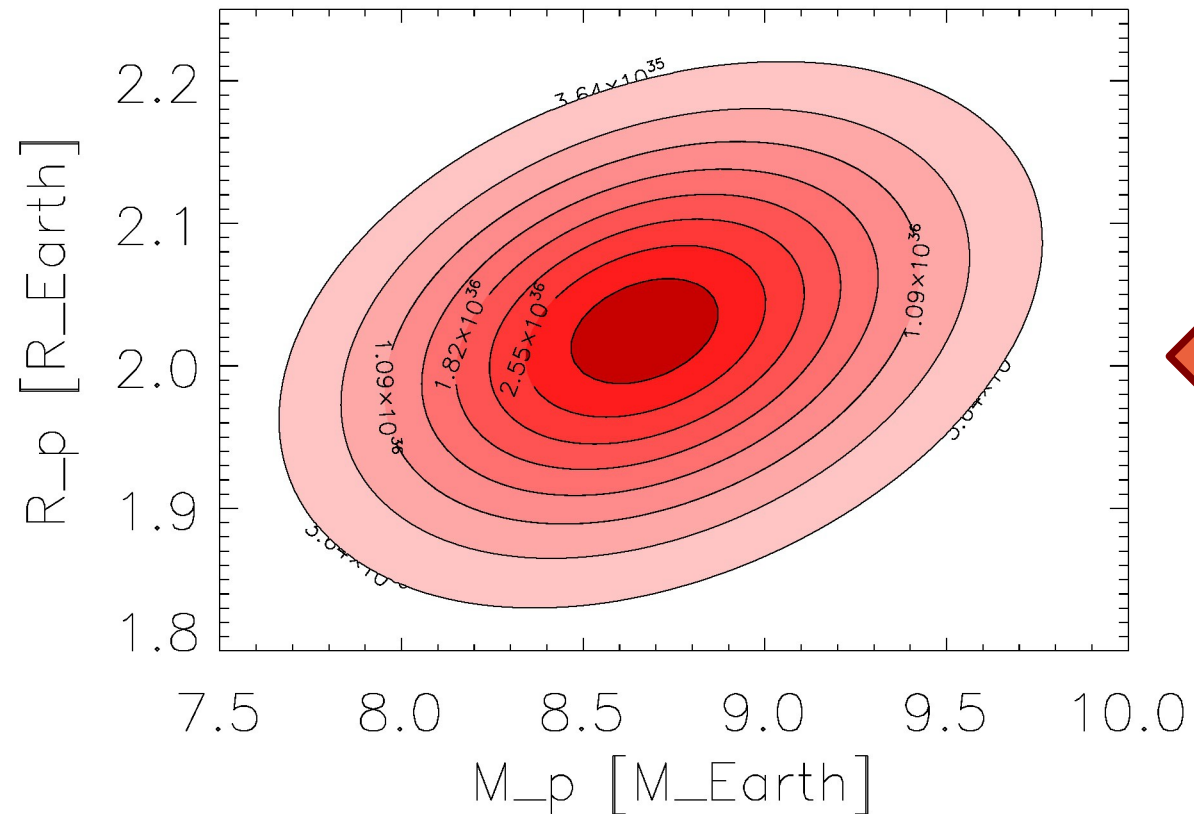
Direct Probability Density Function : the planet

$$R_p = R_* \times \sqrt{D}$$

$$M_p \sin(i) = M_* K (P/2\pi GM_*)^{1/3}$$

→ Analytic PDF of ρ_p .

→ Joint PDF of $M_p - R_p$.



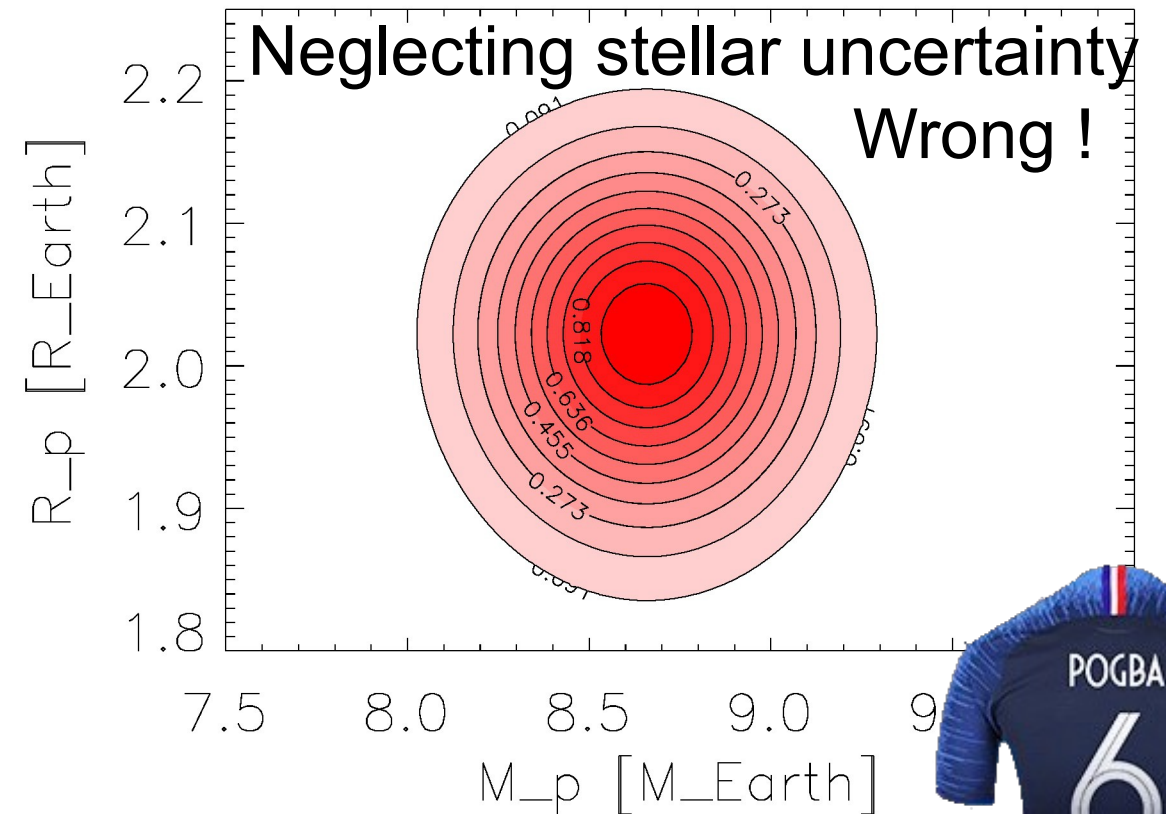
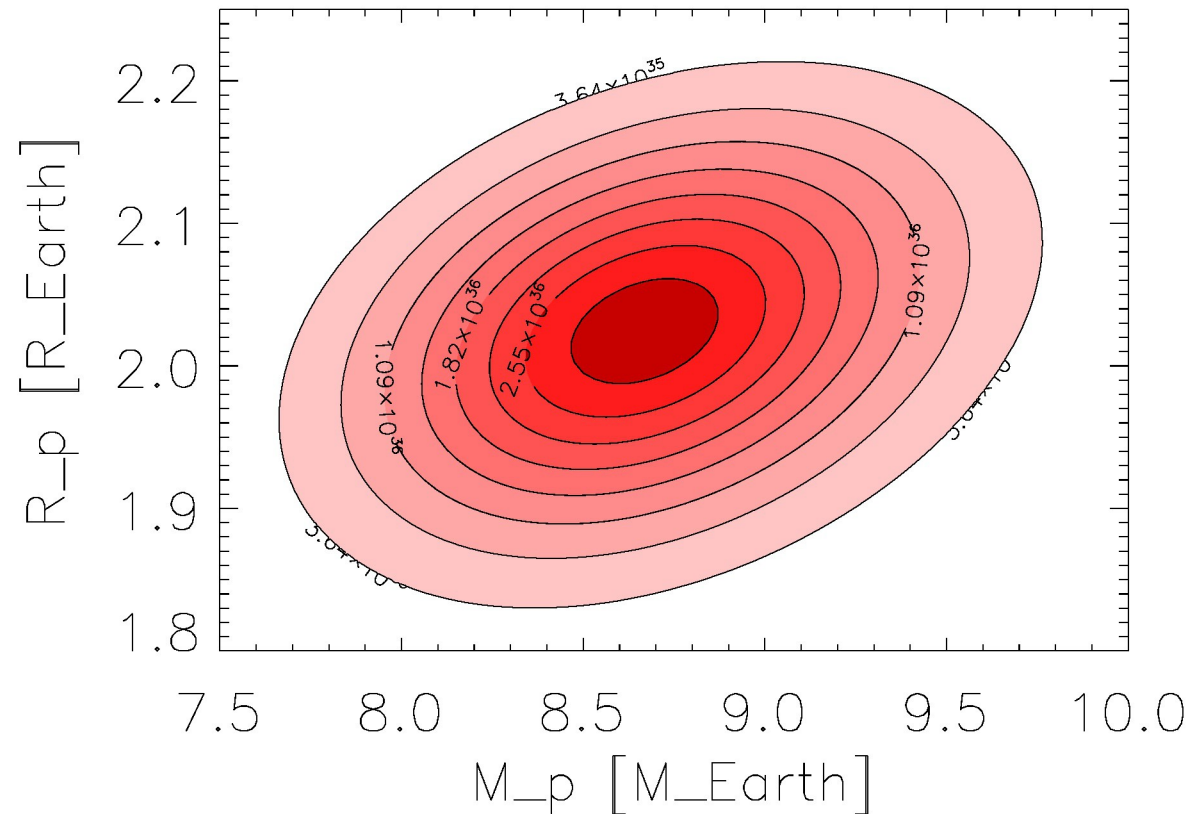
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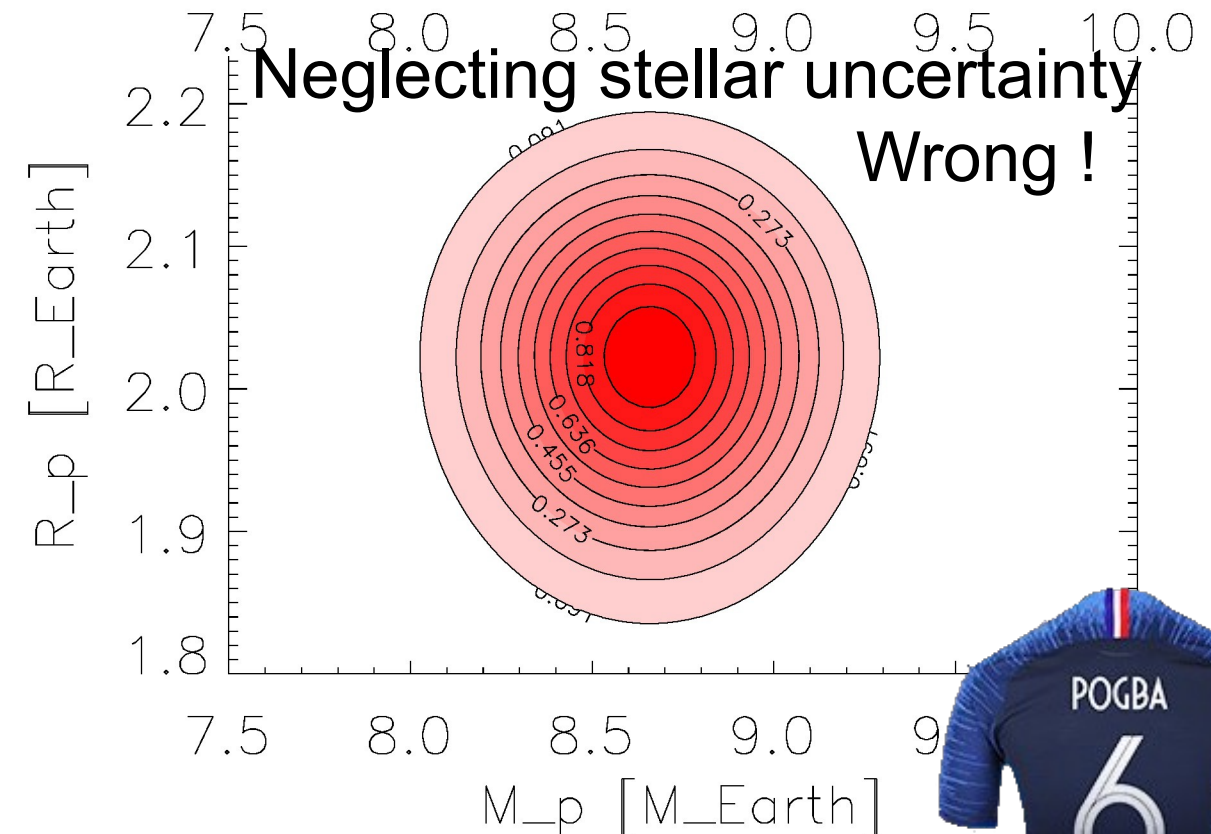
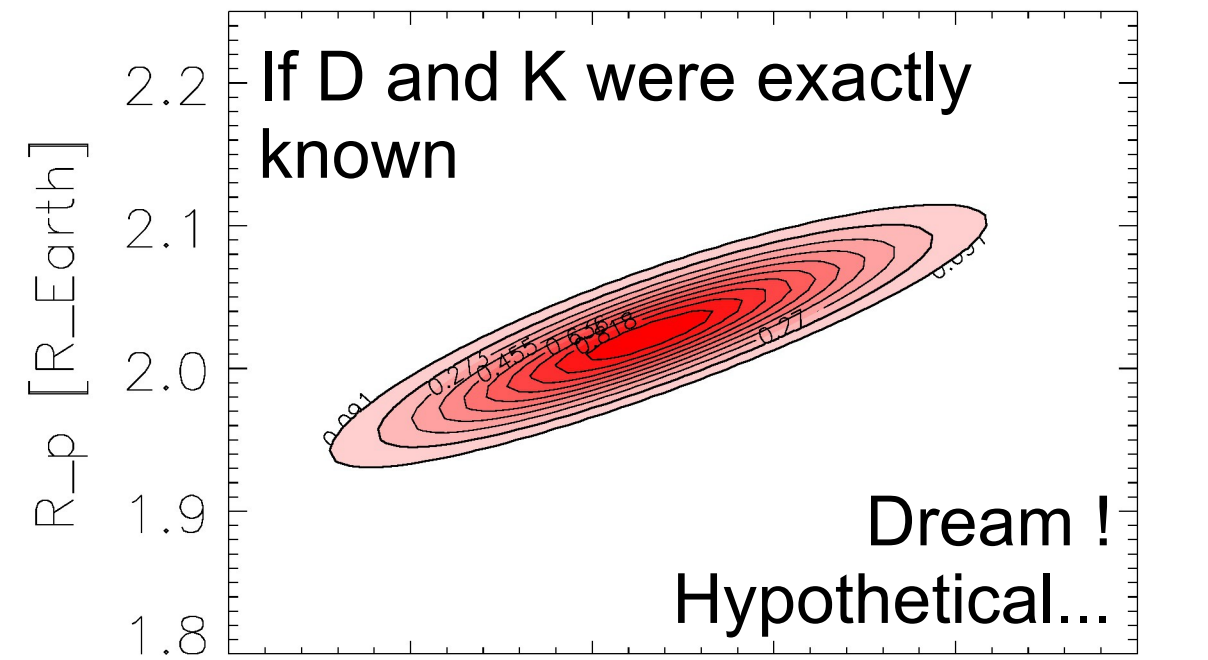
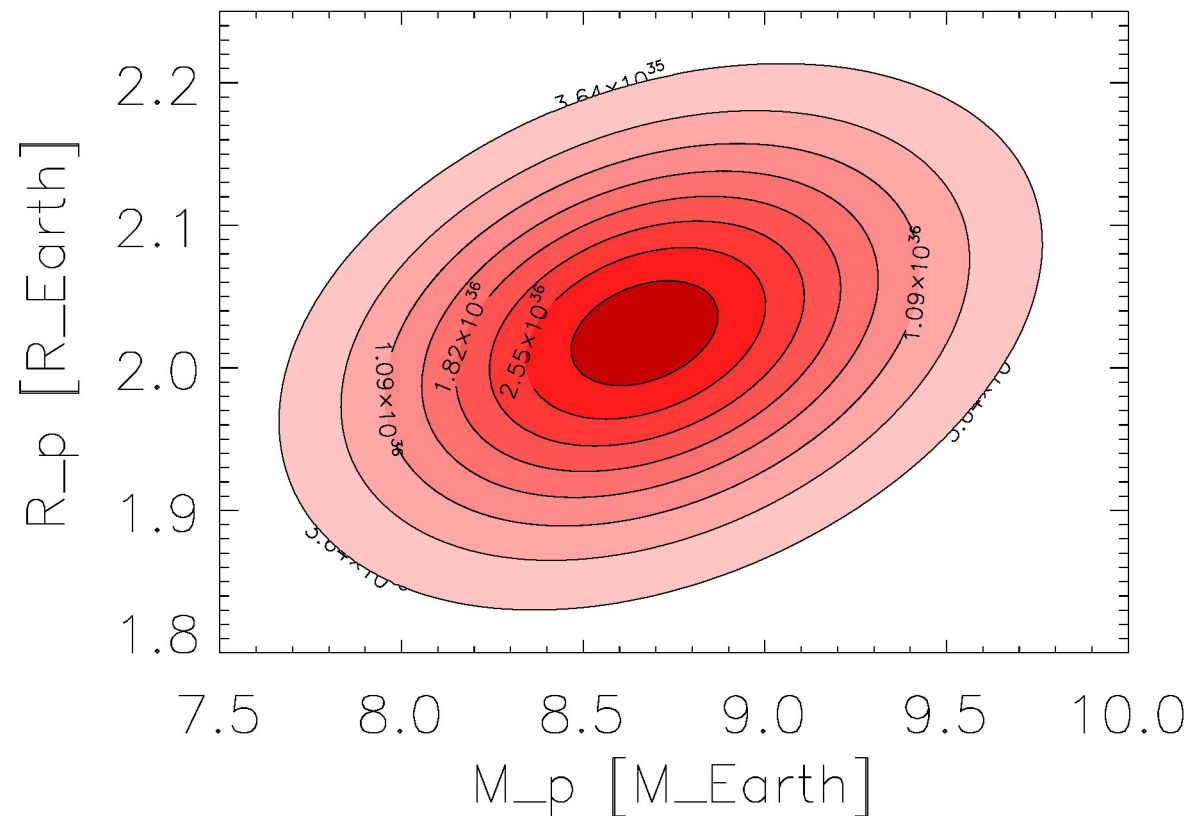
→ Joint PDF of $M_p - R_p$.



Direct Probability Densit

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Application : composition of 55 cnc e

Internal structure model developed by [Dorn et al. \(2017\)](#).

Input :

Original data : M_p , R_p (uncorr.), a , L^* .

Correlation between M_p and R_p (0.30).

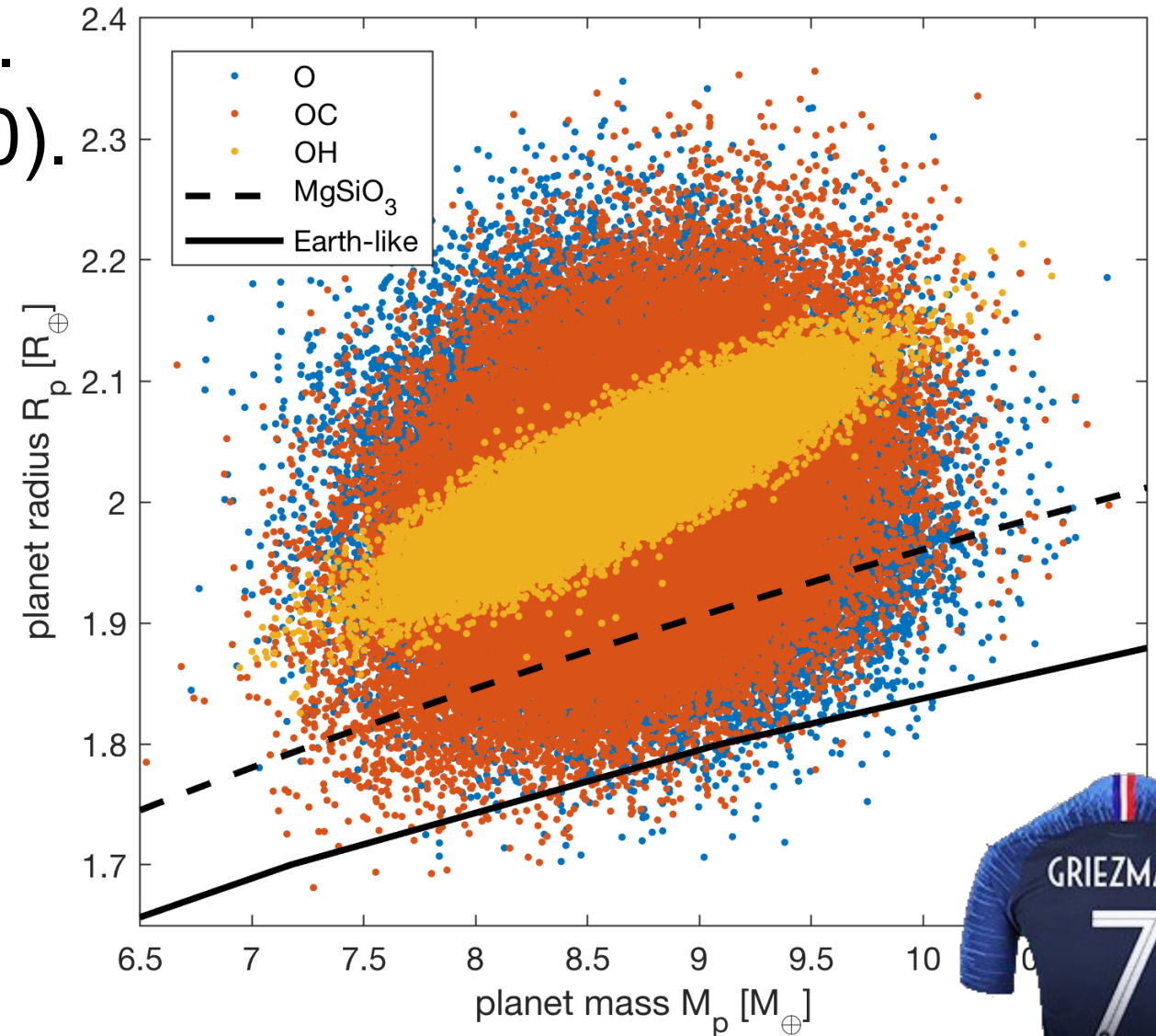
Hypothetical correlation (0.85).

Abundances : stellar Fe/Si, Mg/Si.

Output :

PDF (or CDF) of all the internal parameters.

We test the importance of the various data O, C, H, A.



Application : composition of 55 cnc e

Input :

O Original data

C Correl. M_p - R_p (0.30)

H Hypothetical corr. (0.85)

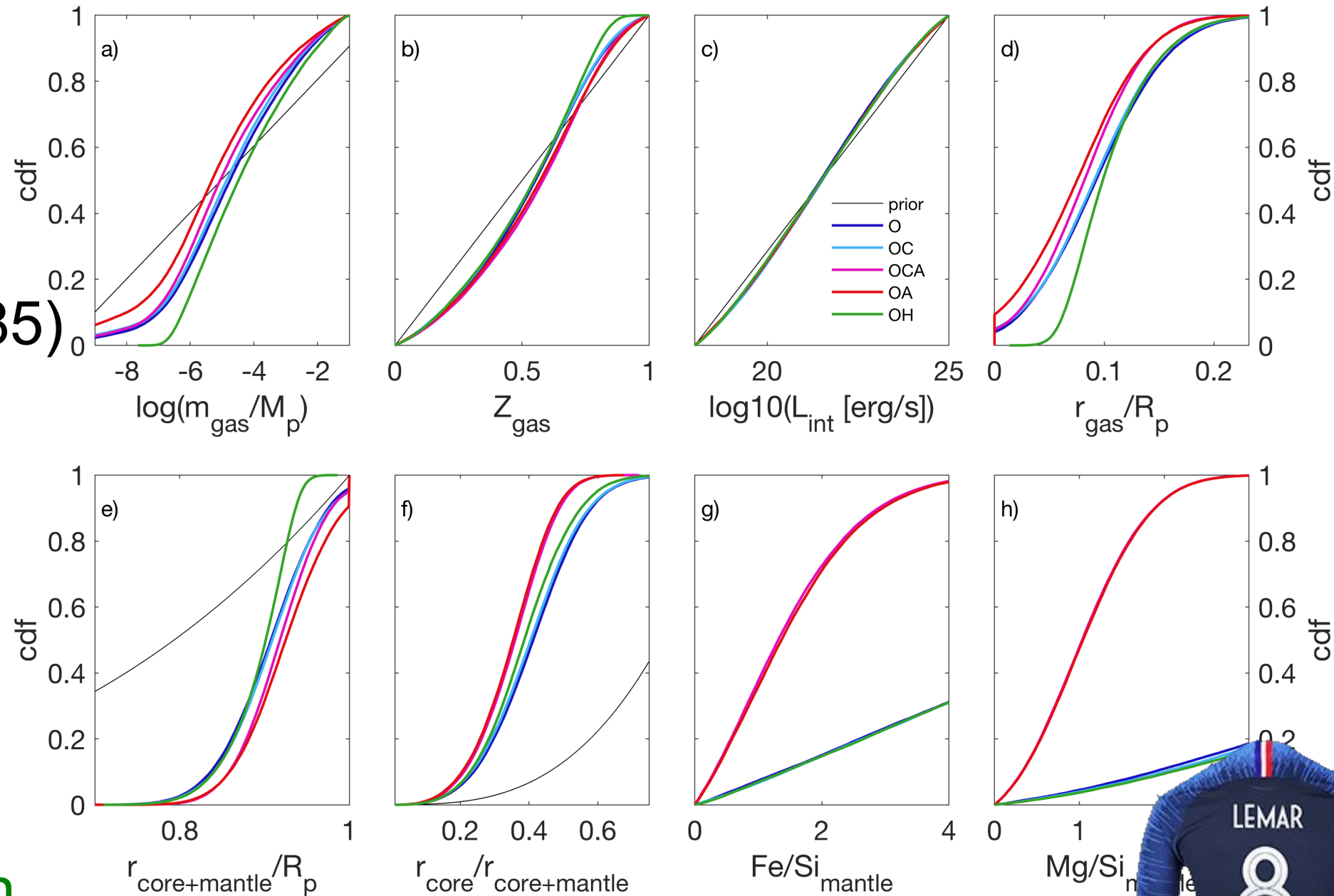
A Abundances

Results :

A → composition of the mantle

C → gas layer

H → could rule out pure solid composition



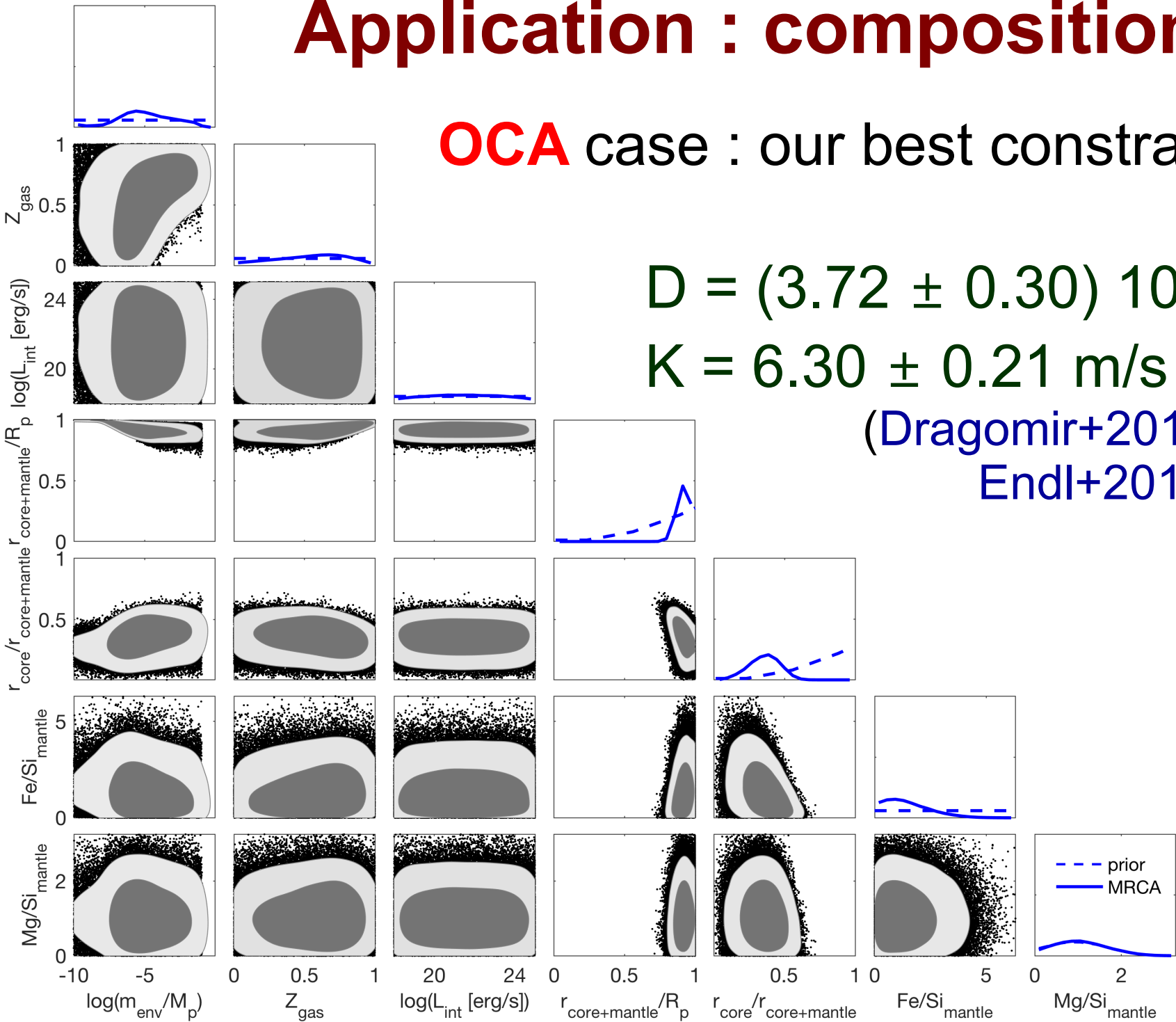
Application : composition of 55 cnc e

OCA case : our best constrains on all the parameters.

$$D = (3.72 \pm 0.30) \cdot 10^{-4}$$

$$K = 6.30 \pm 0.21 \text{ m/s}$$

(Dragomir+2014,
Endl+2012)



interior parameter	OCA
$\log_{10}(m_{\text{gas}}/M_p)$	$-5.07^{+2.14}_{-1.61}$
Z_{gas}	$0.58^{+0.22}_{-0.30}$
$\log_{10}(L_{\text{int}})$	$21.49^{+2.13}_{-2.14}$
r_{gas}	$0.08^{+0.05}_{-0.05}$
$r_{\text{core+mantle}}/R_p$	$0.92^{+0.05}_{-0.05}$
$r_{\text{core}}/r_{\text{core+mantle}}$	$0.36^{+0.10}_{-0.08}$
$\text{Fe}/\text{Si}_{\text{mantle}}$	$1.3^{+0.2}_{-0.2}$
$\text{Mg}/\text{Si}_{\text{mantle}}$	$1.6^{+0.2}_{-0.2}$

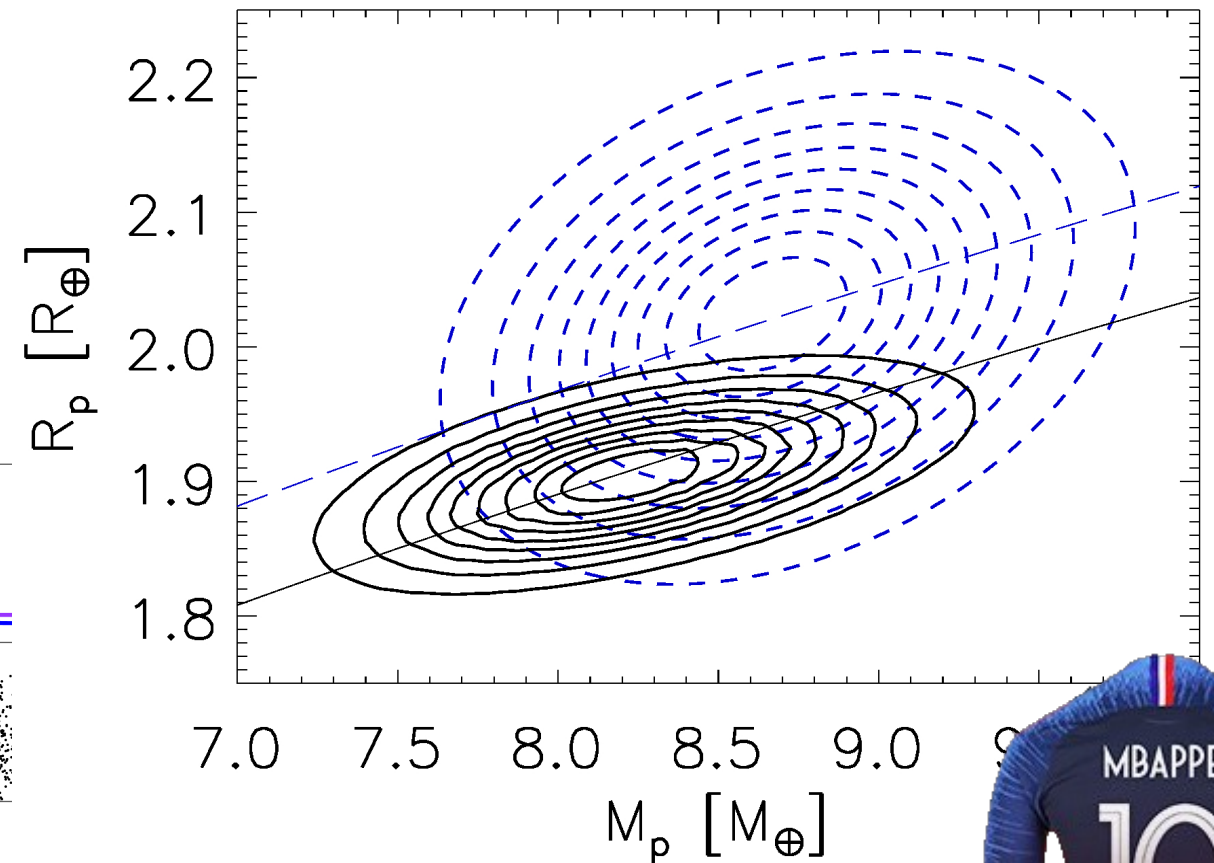
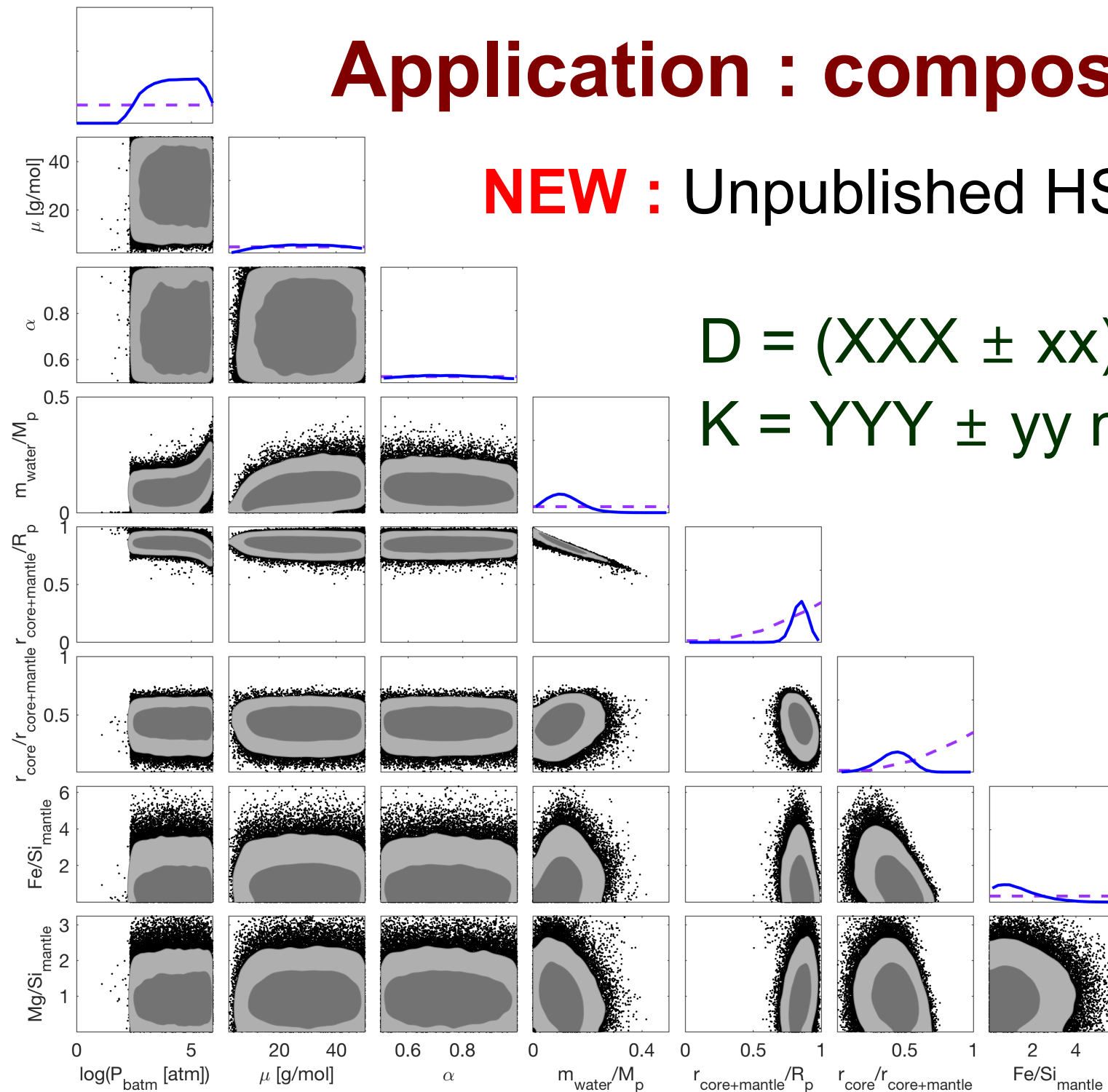


Application : composition of 55 cnc e

NEW : Unpublished HST observations (Bourrier+, accepted)

$$D = (XXX \pm xx) 10^{-4}$$

$$K = YYY \pm yy \text{ m/s}$$



CONCLUSION

- 1) Do not trust too small error bars: stellar parameters are killers !
- 2) Measuring the radius of a star with a transiting exoplanet provides the mass and the mass-radius correlation.
- 3) Use as many constraints as possible :
stellar abundances, M-R correlation...
→ Aim for better estimates of K and D for stronger correlations.

Ref : Crida, Ligi, Dorn & Lebreton (2018, ApJ)



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4) ALLEZ LES BLEUS !



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