

Dark Matter candidates
And
How to probe them on the Galactic (Milky Way) scale

Julien Laval
LUPM – CNRS – U. Montpellier

SF2A 2019 – PNCG mini-workshop

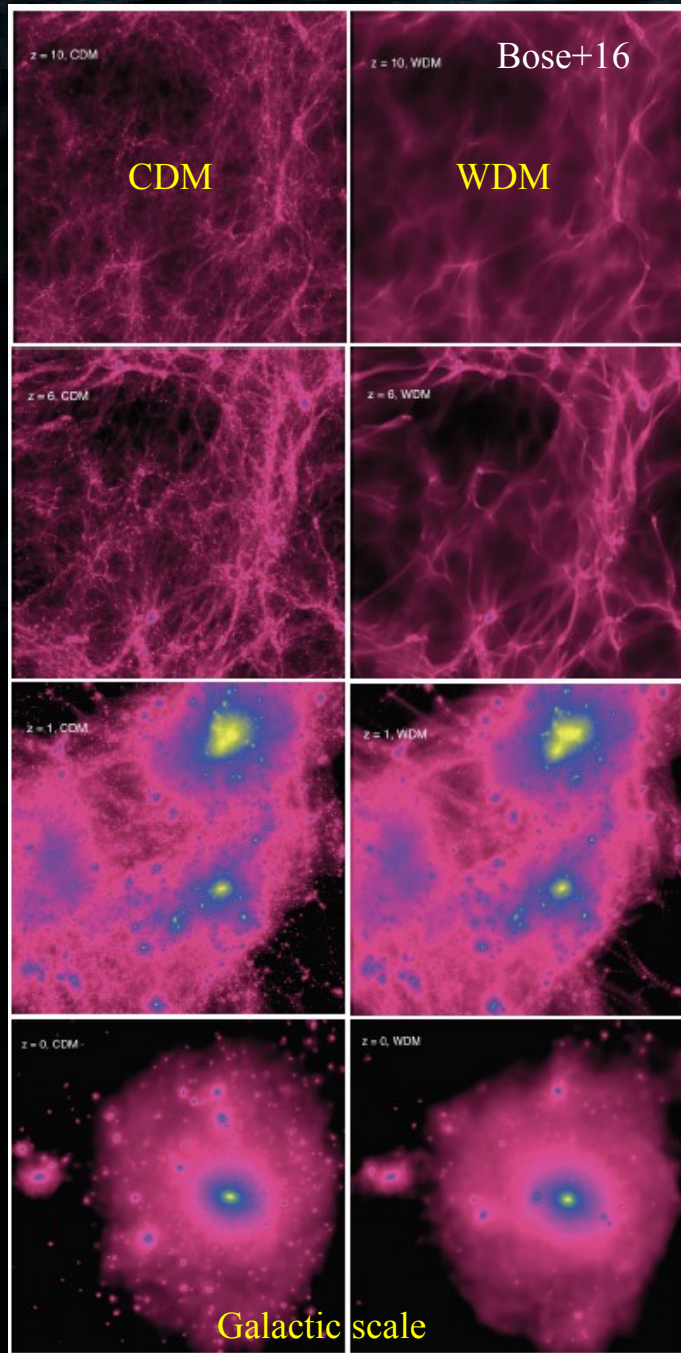
Nice University – May 17, 2019



The GaDaMa Project



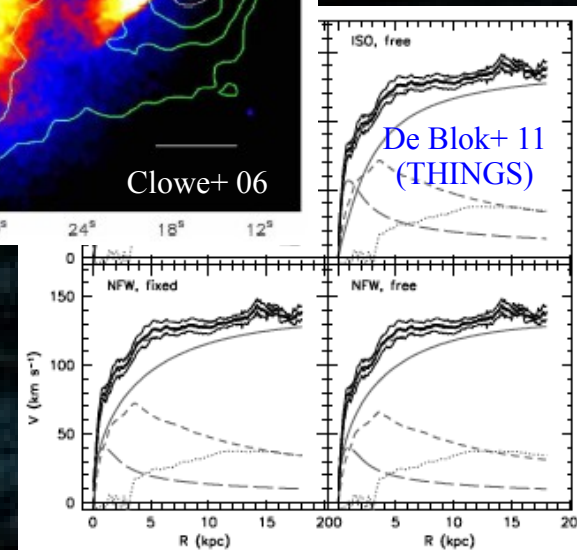
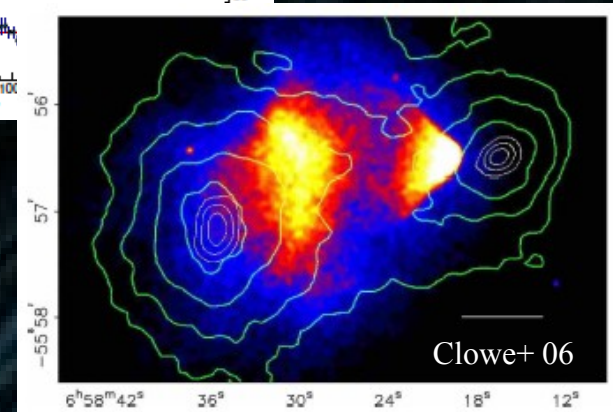
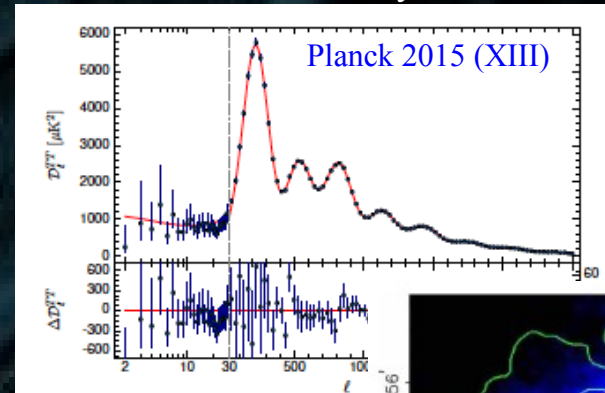
The cold Dark Matter (CDM) paradigm



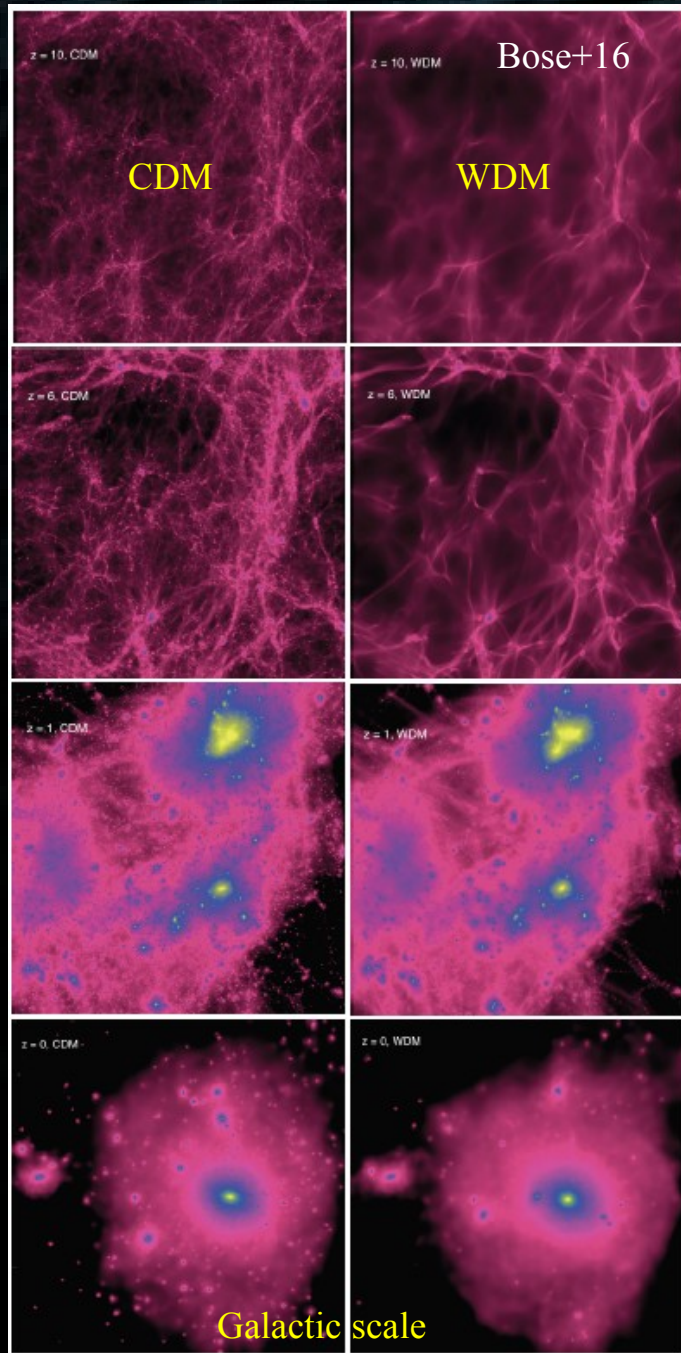
So far, only gravitational evidence for DM
(cosmological structures+CMB)

CDM successes:

- CMB peaks
- Successful structure formation (from CMB perturbations)
=> CDM seeds galaxies, galaxies embedded in DM halos
- Lensing in clusters + rotation curves of galaxies
- Also consistent with Tully-Fisher relation (baryonic physics)



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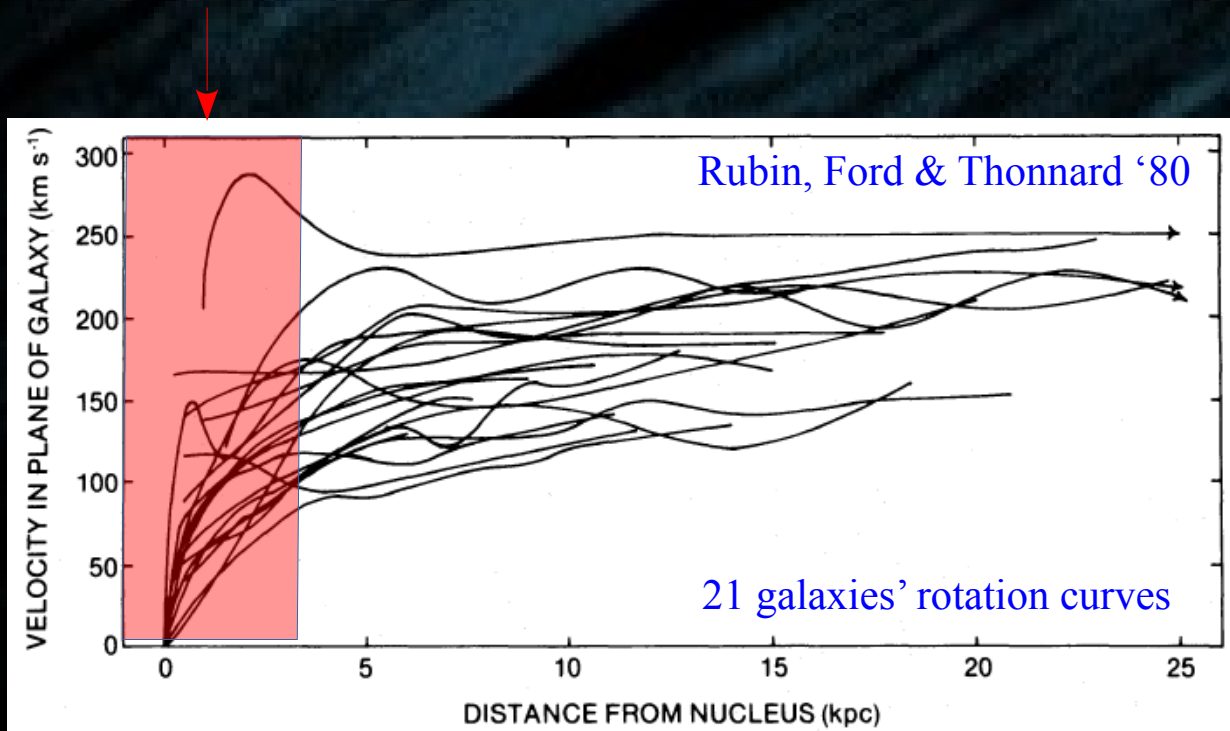
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ISSUES:

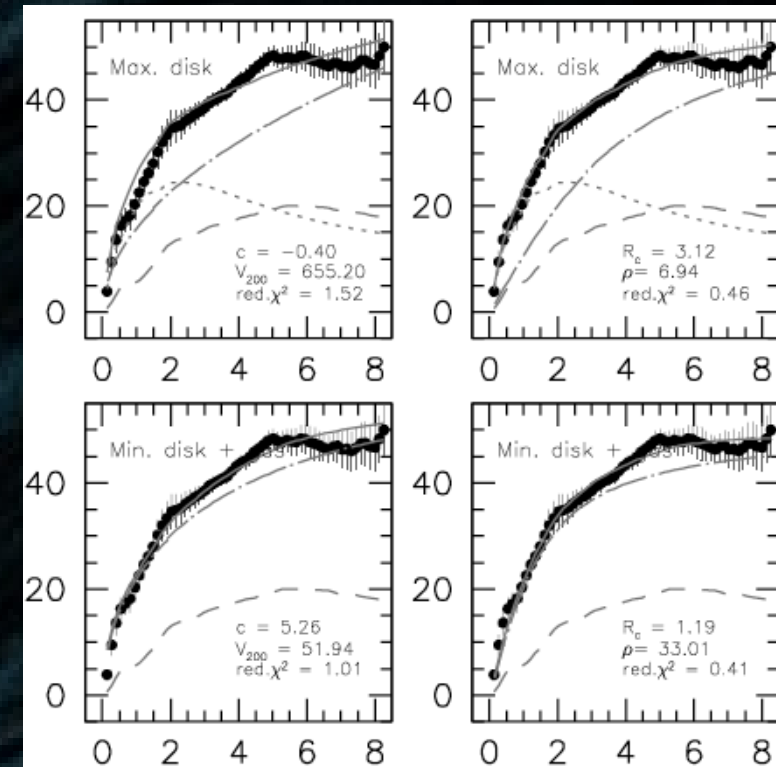
- * No DM particles identified so far
(a generic statement for the dark universe: issue of the origin/s)
- * How cold must it be?
- * Some observational issues on cosmological scales? (e.g. Hubble tension)
- * Some observational issues (challenges?) on small scales

Dark Matter on galactic scales

Bulk of luminous matter



Oh+11



- * **Keplerian decrease** of rotation velocity **not observed**
- * Stars and gas not bounded to the object unless invisible mass there
=> **Spherical dark matter halo** could explain this + natural stabilizer

CDM issues on small (subgalactic) scales

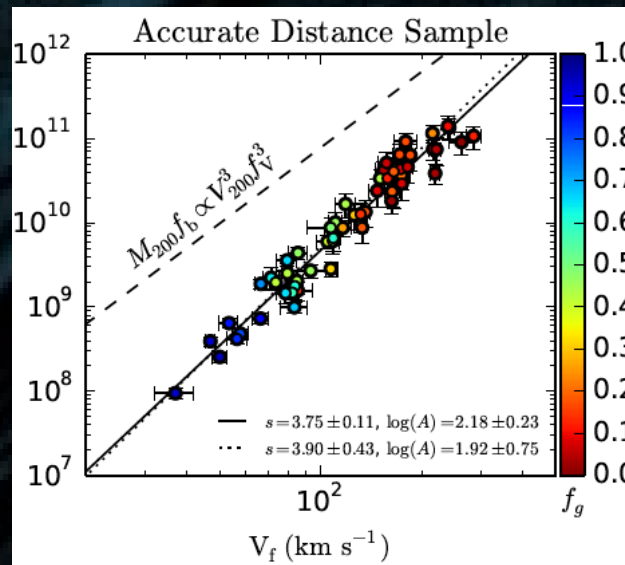
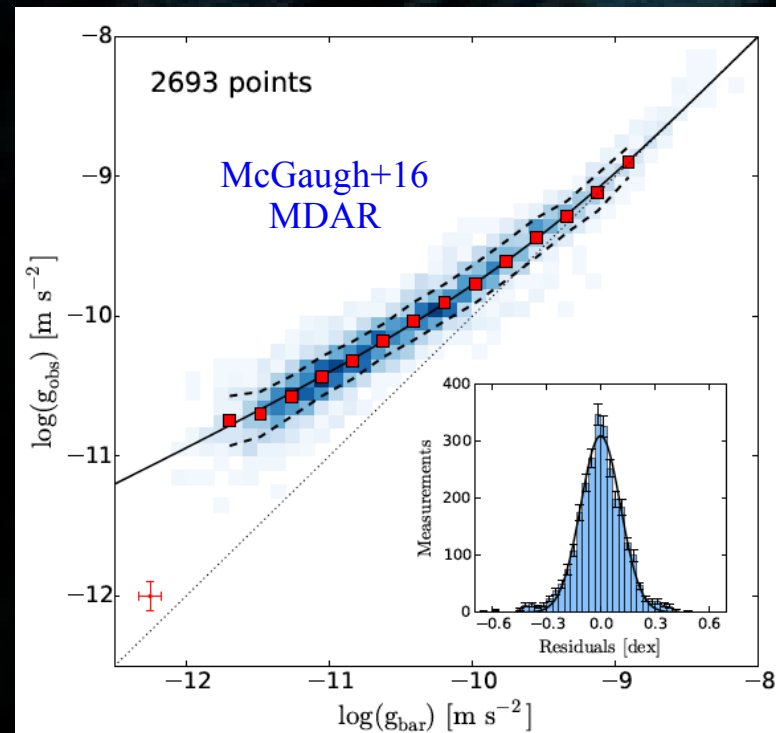
Small-Scale Challenges to the Λ CDM Paradigm

arXiv:1707.04256

James S. Bullock¹ and Michael Boylan-Kolchin²

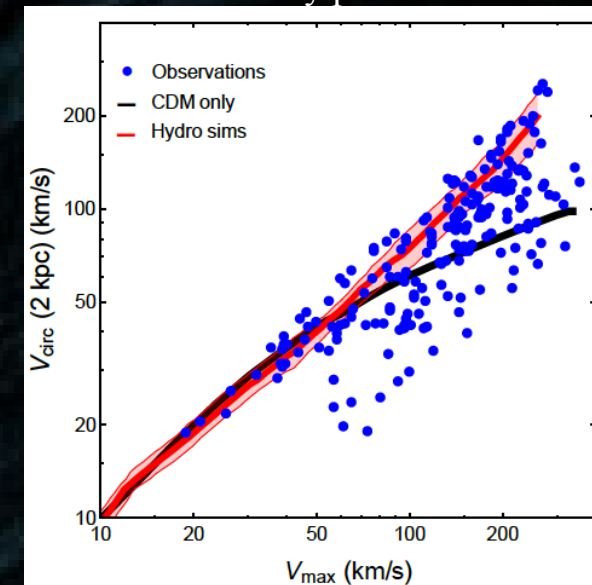
¹Department of Physics and Astronomy, University of California, Irvine, CA 92697, USA; email: bullock@uci.edu

²Department of Astronomy, The University of Texas at Austin, 2515 Speedway, Stop C1400, Austin, TX 78712, USA; email: mbk@astro.as.utexas.edu



Lelli+15, BTFR

Tulin+18 after Oman+15
Diversity problem



Core/cusp+diversity problems or regularity vs. diversity problems.
Maybe baryonic effects, but clear statistical answer needed.
Does same feedback recipe solve all problems at once?

CDM issues on small (subgalactic) scales

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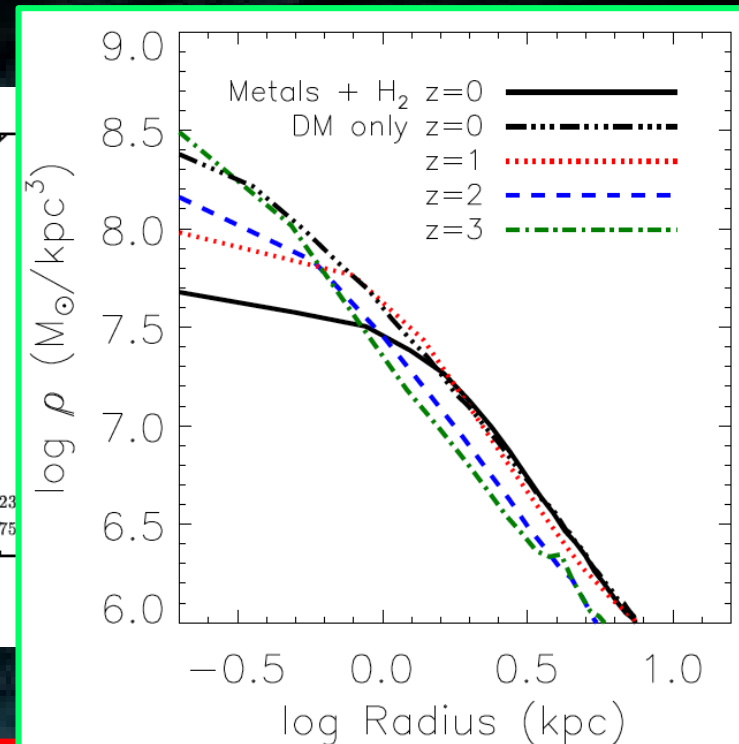
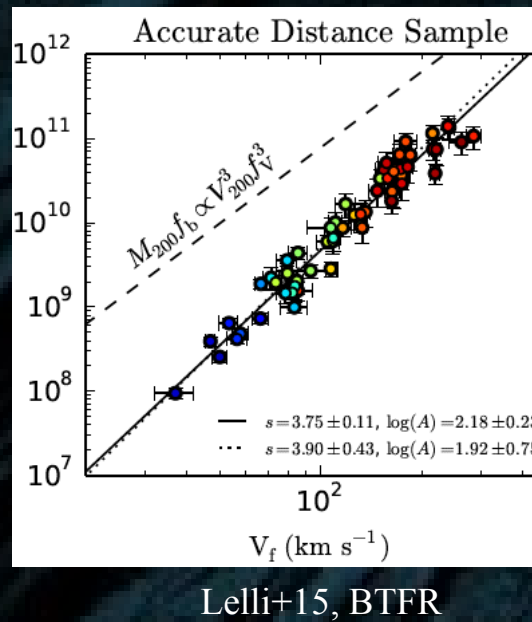
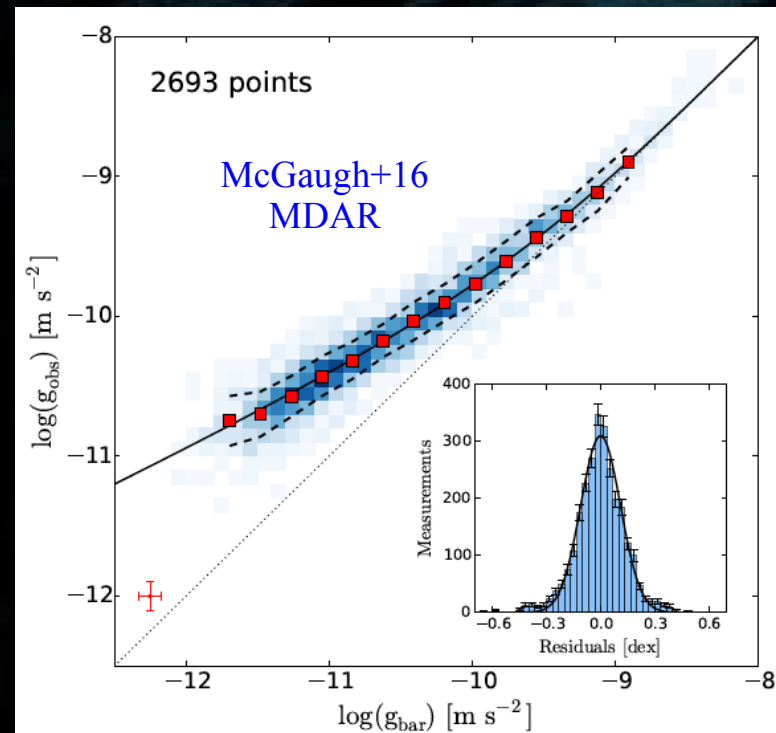
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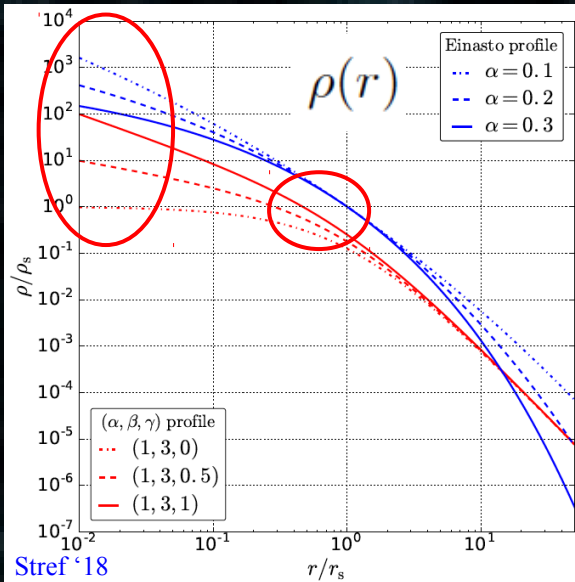
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Governato+12
Cusps \rightarrow cores



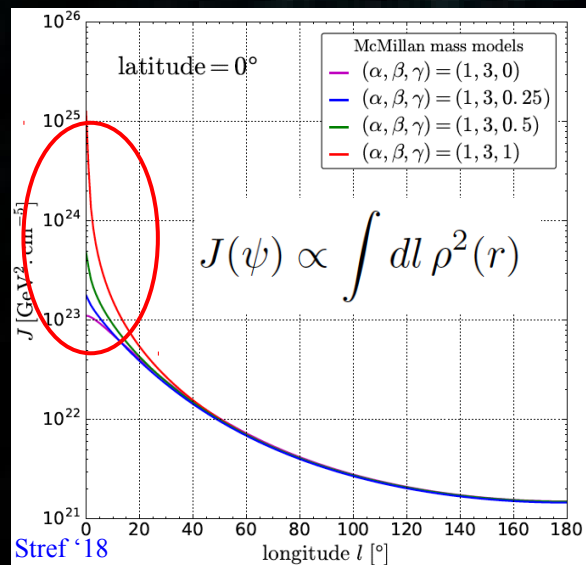
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Dark matter distribution properties (and why it matters)



Mass density profile/s

(but mind potentially strong difference between peculiar objects and average expectations)

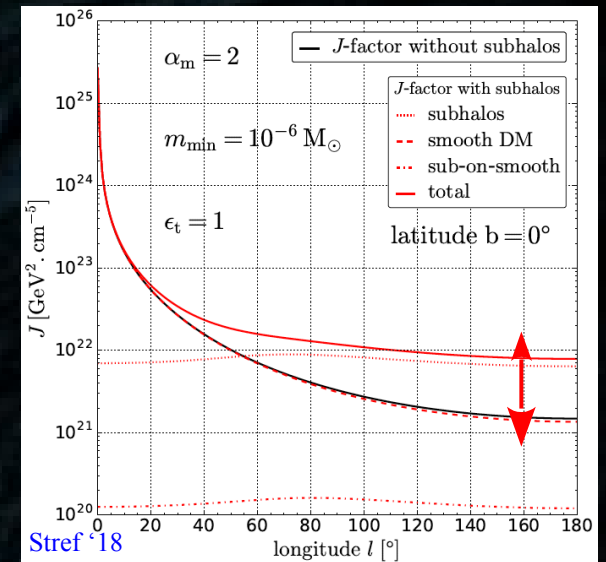


Smooth galaxy

Clumpy galaxy

Granularity of halos
(aka subhalos)

Related to clustering
properties of dark matter
→ Impact on a bulk of
predictions



++ Phase-space distribution of dark matter

Many observables related to dark matter
searches may depend on velocity (e.g. cross
sections, microlensing events, etc.)

Generic constraints on DM particles

→ Assume a single DM species:

* Massive

* Cold or close to cold (or cold-warm):

CMB peaks + Ly-alpha + structure formation + dwarf galaxy phase space

=> For **DM produced thermally** in the early universe: **$m > 1\text{-}5\text{ keV}$** (bosons or fermions)

=> For **DM produced non thermally** in the early universe: **particle statistics matters!**

Fermions: the Tremaine-Gunn limit ('78) => use **dwarf galaxies as test systems**

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Liouville's theorem for non-interacting fermions, assuming they were close to FD distribution in early universe

$$f_\nu(p, T) = \frac{g_\nu}{(2\pi)^3} \frac{1}{e^{E/T} + 1} \xrightarrow{\text{max}} \frac{g_\nu}{2(2\pi)^3} \geq \frac{\rho(r)}{m_\nu} \times \left\{ f(p) = \frac{e^{-\frac{p^2}{2m_\nu^2 \sigma_v^2}}}{(2\pi m_\nu^2 \sigma_v^2)^{3/2}} \right\}$$

$$\rho(r) = \frac{9 \sigma_v^2}{4 \pi G (r + r_0)^2}$$

Cored-isothermal sphere

$$m_\nu \gtrsim \left\{ \frac{9 \sqrt{2} \pi M_P^2}{g_\nu \sigma_v r_0^2} \right\}^{1/4} = 0.1 \text{ keV} \left\{ \frac{r_0}{1 \text{ kpc}} \right\}^{-1/2} \left\{ \frac{\sigma_v}{30 \text{ km/s}} \right\}^{-1/4}$$

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Pauli exclusion principle (no assumption on initial phase space): cannot exceed density of degenerate Fermi gas!

$$E_F = \left(\frac{\hbar^2}{2m} \right) (3\pi^2 n)^{2/3} \longrightarrow v_{F,\nu} \equiv \sqrt{\frac{2E_{F,\nu}}{m_\nu}} = \left(3\pi^2 \frac{\rho}{m_\nu^4} \right)^{1/3} \leq v_{\text{esc}}$$

$$m_\nu > \left\{ 3\pi^2 \frac{\rho}{v_{\text{esc}}^3} \right\}^{1/4} \approx 0.1 \text{ keV} \left\{ \frac{r_0}{1 \text{ kpc}} \right\}^{-1/2} \left\{ \frac{\sigma_v}{30 \text{ km/s}} \right\}^{-1/4}$$

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→ Updated by Boyarsky+09: $m > 0.5 \text{ keV}$

Bosons: de Broglie wavelength > size of system => $m > 10^{-22} \text{ eV}$

→ see review in e.g. Marsh '15 (axion-like particles)

Lower mass bounds only!
(except for unitarity constraints – thermal case)

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* Interactions?

→ Electrically **neutral** (or charge $\ll 1$: milli-charged – except in secluded dark sector)

→ If thermally produced => **(weak) couplings to SM particles**

→ **No prejudice on asymmetry** dark matter/antimatter

→ **Self-interactions** and/or **annihilations** allowed

but SI cross sections bounded

→ Possibility of entire dark sector(s)

$$2\text{cm}^2/\text{g} \simeq 4 \text{ b/GeV} \lesssim \frac{\sigma_{\text{self}}}{m_\chi} \lesssim 0.4 \text{ b/GeV}$$

Original proposal by
Carlson+'92

To solve core-cusps
(e.g. Spergel+'00,
Calabrese+'16)

Dynamics of
clusters
(Kaplinghat+'15)

Model building

Two main approaches

*** Top-down**
“DM is a consequence”



*** Motivated by “defects” in SM**

- Asymmetry matter-antimatter not achieved
- Strong CP pb
- Stability of the Higgs sector (hierarchy pb)
- Metastability of EW vacuum
- Flavor hierarchy
- Gauge unification
- Quantum gravity (strings)
- etc.

+++ may solve several issues + **DM candidates**
- - - DM “solution” potentially embedded in large parameter space (tricky phenomenology)

*** Motivation from Cosmology**

- scalar field cosmology (for the sake of itself)
- non-minimal inflation (primordial black holes)

*** Bottom-up**
“DM is a requirement”



*** Consistent QFT**

- +++ Production mechanism/s
- +++ DM phenomenology with a minimal set of parameters => predictive
- - - built on purpose (ad hoc)

Model building

Two main approaches

* **Top-down**
“DM is a consequence”

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The **hierarchy pb** (Higgs stability),
aka the **theoretical particle physics crisis**



$$\delta m_H^2 = \left[\text{Challenged by LHC} - y_t^2 \right]$$

(e.g. Csaki & Tanedo '16)

Higgs mass receives quantum corrections
→ very **sensitive to any new heavy scale** (fine tuning)

- * Might be cured by adding canceling terms
- * e.g. **Supersymmetry** ⇒ bosons ↔ fermions cancel in loops
- * want to **forbid new interactions, like:**
 - **discrete symmetry** (parity, Z₂, etc.)
 - ⇒ proton does not decay
 - ⇒ lightest particle stable

STANDARD

NEW

STANDARD

DM: neutralino, sneutrino, gravitino, etc.

+QCD axion DM, “string-inspired” axions (eg ULA)
+(Sterile) right-handed neutrino DM
+Others (e.g. relaxions ...)

* Consistent QFT

- +++ Production mechanism/s
- +++ DM phenomenology with a minimal set of parameters ⇒ predictive
- - - built on purpose (ad hoc)

Status of current searches

*** WIMPs (thermal DM)**

- Many ongoing experiments (multiwavelength, multimessenger + laboratory)
- Sensitivity in the right ballpark for mass range 10-100 GeV => many constraints
- Still to probe: $m < 10$ GeV, $m > 100$ GeV
- Gamma-rays, cosmic rays, CMB, 21 cm, collider+lab searches, impact on stellar evolution, gravitational searches.

*** Axions**

- Several ongoing experiments (probe conversion of axions to photons, absorption of photons)
- QCD axion: mass range (10 μ eV) not reached yet.
- Axion-like particles (ALP, e.g. ULA): ongoing studies, astrophysical probes.

*** Sterile neutrinos**

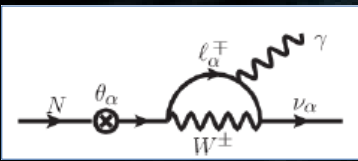
- Excitement after the 3.5 keV line (evidence disputed)
- Tiny room left in parameter space from structure formation (Ly-alpha) and X-ray constraints.

Sterile neutrino (W/C)DM

e.g. Dodelson & Widrow '94,
Shi & Fuller '99,
Asaka, Shaposhnikov, Boyarsky+ '06-16

- Neutrino masses (see-saw)
- Leptogenesis
- DM candidates (more or less warm)
- keV mass range (!= thermal mass)

$$\mathcal{L} \supset \mu \left[\frac{\phi}{v} \right] \bar{\nu}_l \nu_r + M \nu_r \nu_r + \text{h.c.}$$



$$\Gamma_{N_1 \rightarrow \gamma \nu} = \frac{9 \alpha G_F^2}{1024 \pi^4} \sin^2(2\theta_1) M_1^5$$

Aspects relevant to cosmology:

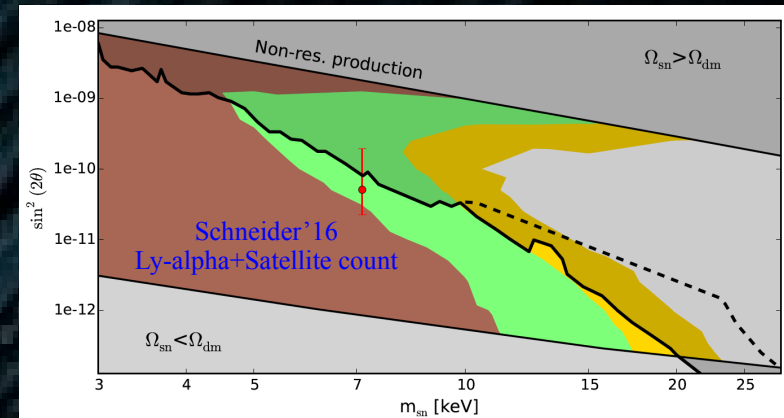
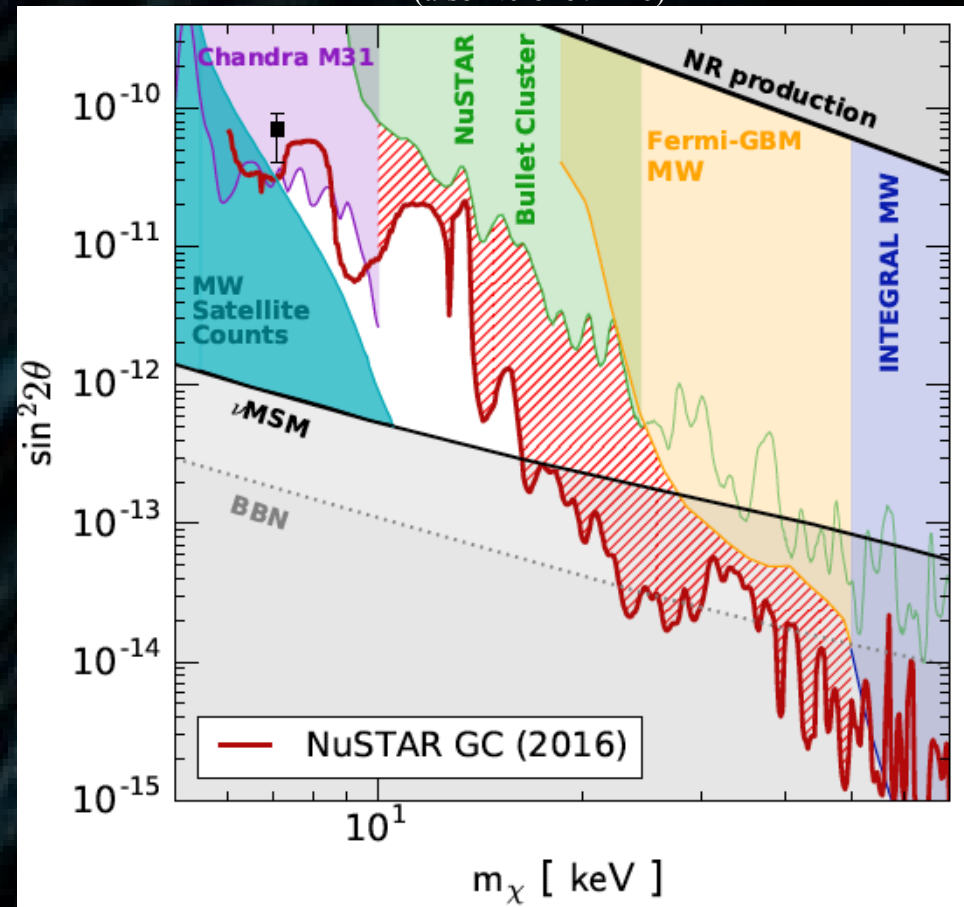
- * suppress power on small scales
(free-streaming scale larger than CDM)
- viable? (e.g. Schneider 15)
- * current limits on thermal masses > 1.7 keV

Detection (main):

- * neutrino experiments (double β decay)
- * decays to X-ray line: hints @ 3.5 keV (Bulbul+14, Boyarsky+14)
- 7 keV consistent with thermal mass of 2 keV (e.g. Abazajian 14)
- hot debate, could be systematics (cf. Jeltema & Profumo)
- Hitomi excludes excess in Perseus cluster (1607.07420 see also 1608.01684)

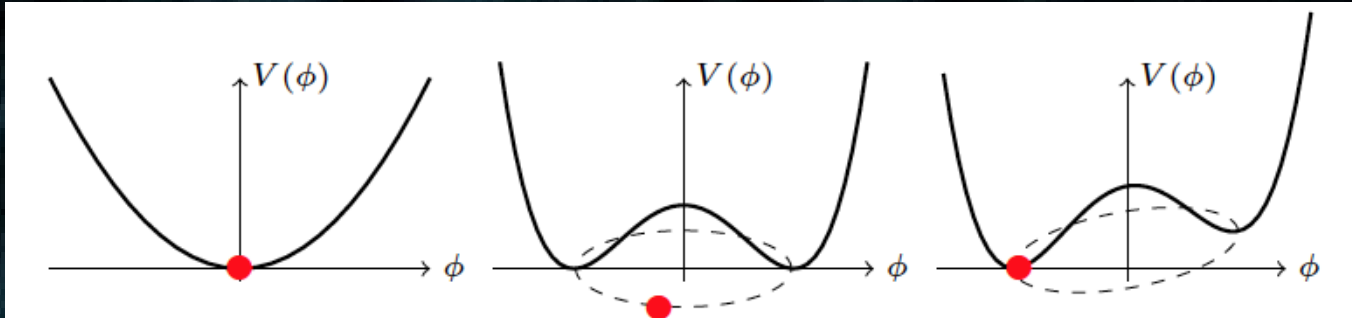
Constraints: Resonant-production mechanism almost excluded ----->

Perez+ '16
(also Neronov+ '16)



(QCD) axions

Peccei-Quinn, Wilczek, Weinberg, Kim, Shifman, Vainshtein, Zakharov, Dine, Fishler, Srednicki, Sikivie – 70'-80'



Peccei-Quinn (PQ) symmetry unbroken
Very high T

PQ symmetry broken
@ $T \sim f_a \sim 10^{10}$ GeV

The axion picks up a mass
 $T \sim T_{\text{QCD}} \sim 150$ MeV

$$\mathcal{L}_{\theta\text{QCD}} = \frac{\theta_{\text{QCD}}}{32\pi^2} \text{Tr } G_{\mu\nu} \tilde{G}^{\mu\nu}$$

NB: QCD axion needs physics beyond standard model

Production mechanism (relevant to DM axions):

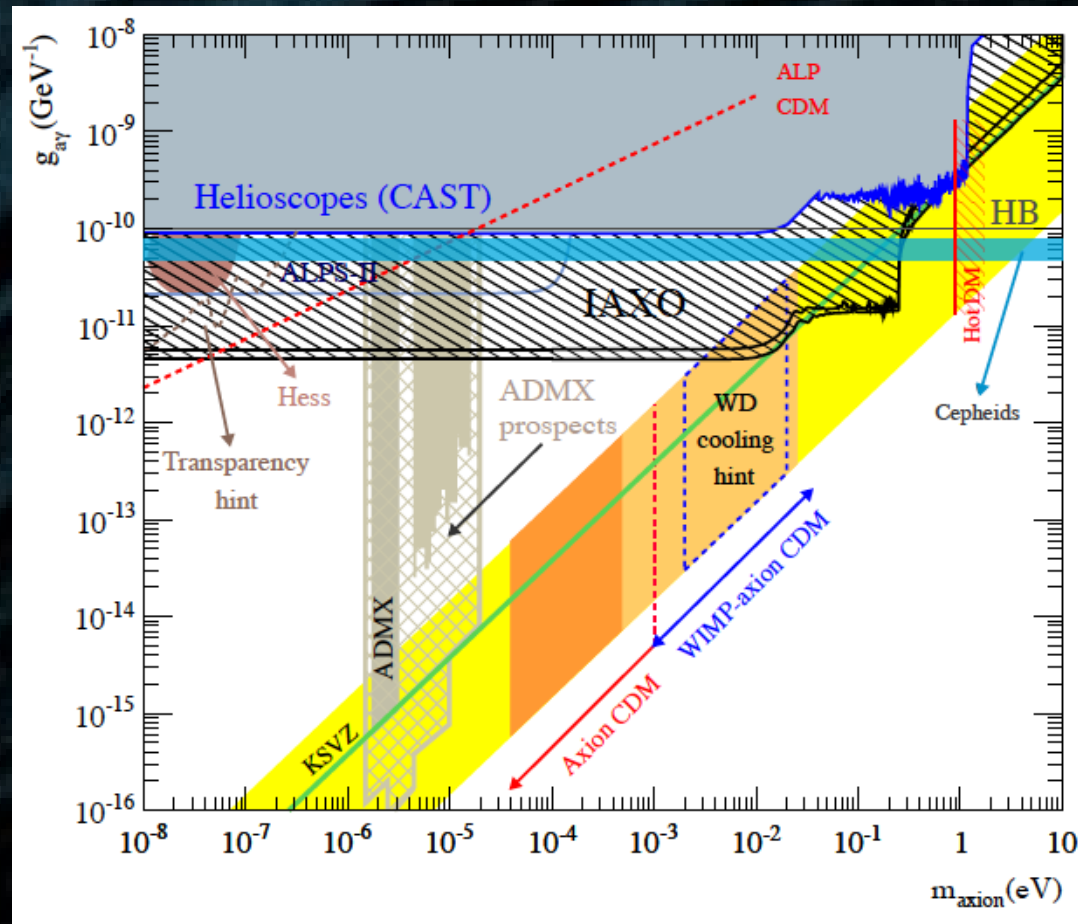
- * Misalignment mechanism (generic)
- * Decay of topological defects (if PQ broken after inflation)
→ compact axion asteroids! ($f \sim 0.5$) – Tkachev'86
- * $m \ll \text{eV} \Rightarrow$ large occupation # \Rightarrow classical field
- * QCD axions = CDM \Rightarrow searches through EM couplings!

$$\Omega_a h^2 \sim 2 \times 10^4 \left(\frac{f_a}{10^{16} \text{ GeV}} \right)^{7/6} \langle \theta_{a,i}^2 \rangle$$

Axion cosmology
(review)
Marsh'15

$$m_a^2 = \frac{m_\pi^2 f_\pi^2}{(f_a/N_{\text{DW}})^2} \frac{m_u m_d}{(m_u + m_d)^2}$$

Constraints on QCD axions



Compiled by Marsh'15

Non-QCD ultra-light axions (ULA = fuzzy DM)

Hu+00, Peebles'00, Marsh+15, Hui+16, Schive+14, Du+18, etc.

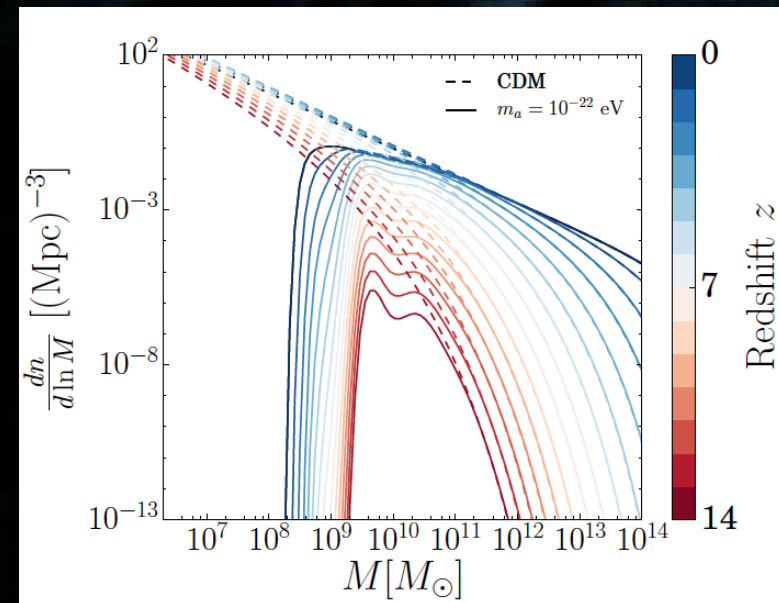
Same production mechanisms as axions but not meant to solve the strong CP (QCD) pb
 => PQ breaking + axion mass free parameters (cosmological constraints) => EM couplings optional

Main properties:

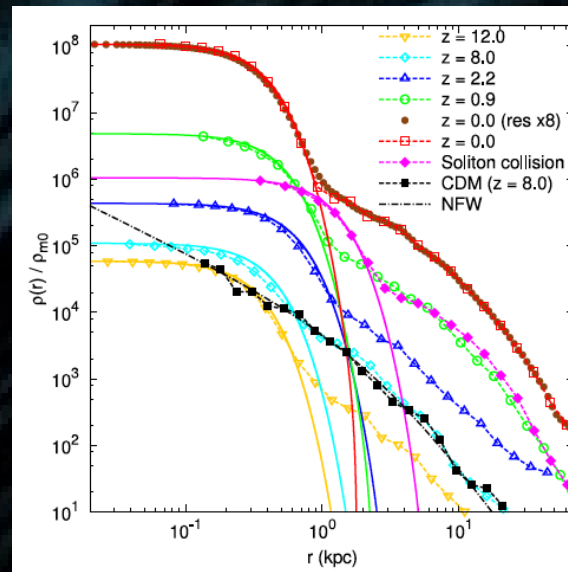
- * Suppression of small-scale perturbations
- * incoherent interference pattern and granularity on scales ~ 1 -100 kpc
- * formation of solitonic cores at halo centers
- * core/cusp solved in galaxies if $m \sim 10^{-22}$ eV

$$i\hbar \left(\dot{\psi} + \frac{3}{2}H\psi \right) = \left(-\frac{\hbar^2}{2mR^2} \nabla^2 + m\Phi \right) \psi$$

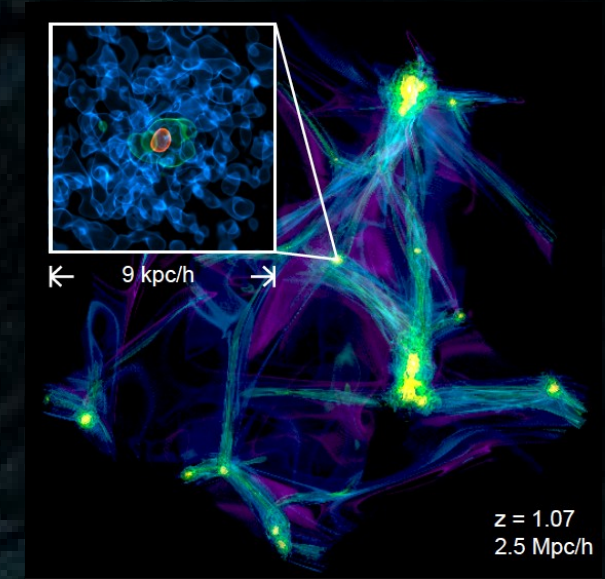
$$\nabla^2 \Phi = 4\pi G m_a |\psi|^2$$



Bozek+15
Halo mass function



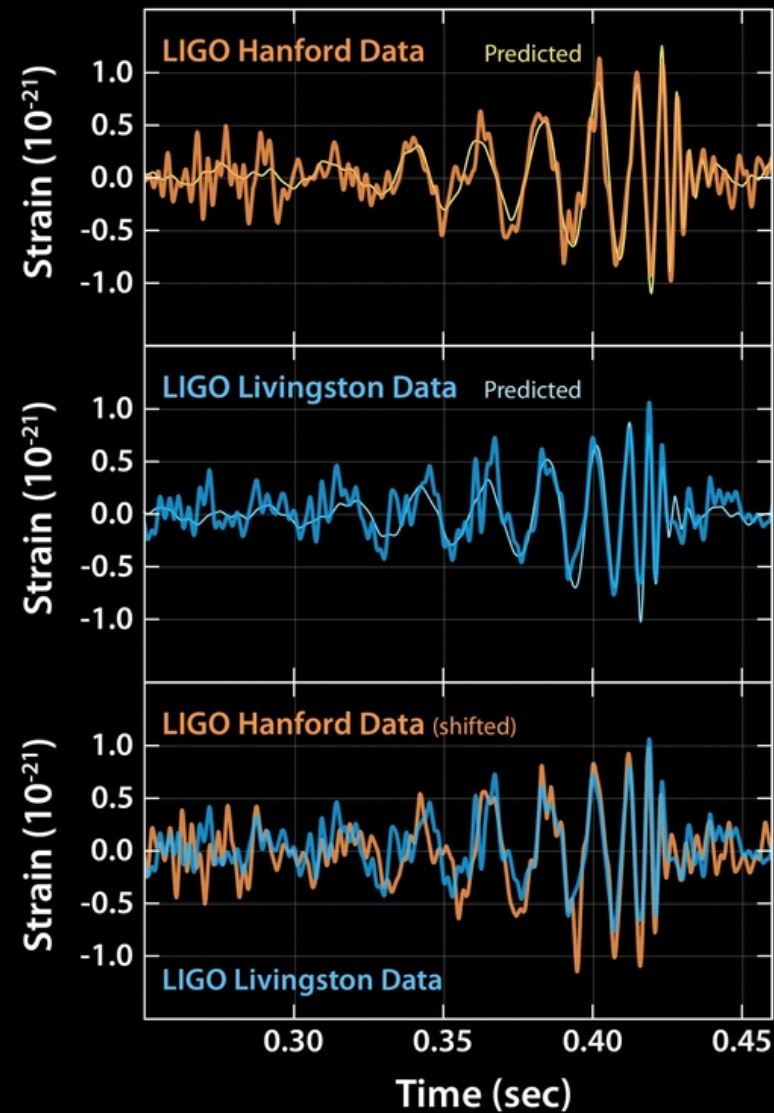
Schive+14
Solitonic cores in
Fuzzy DM simulations



Veltmaat+18
Evolution of solitonic cores

Black holes as DM?

LIGO+VIRGO '16



Did LIGO detect dark matter?

Simeon Bird,* Ilias Cholis, Julian B. Muñoz, Yacine Ali-Haïmoud, Marc Kamionkowski, Ely D. Kovetz, Alvise Raccanelli, and Adam G. Riess¹

¹Department of Physics and Astronomy, Johns Hopkins University,
3400 N. Charles St., Baltimore, MD 21218, USA

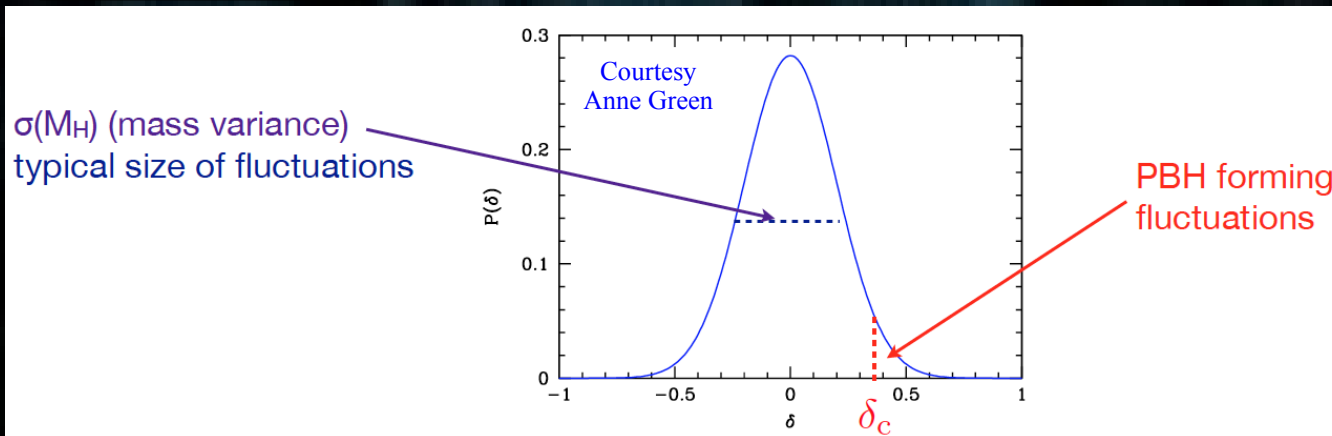
arXiv:1603.00464 (PRL)

Primordial black holes

Generic idea (Zel'dovich&Novikov, Hawking, Carr&Hawking'70's):

- * Very large density fluctuations may collapse directly into Bhs in the radiation era
- * $M_{pbh} \sim$ mass within horizon
- * Fluctuation amplitude $\sim 10^{-5}$ at CMB scales
- * ~ 0.01 needed \Rightarrow **more power (e.g. non gaussianity) needed on very small scales**
- * **Production enhanced at phase transitions** (e.g. QCD \leftrightarrow Mh ~ 1 M_{sun})
- * A potentially **macroscopic CDM candidate**

Review in Carr+16



$$\delta \geq \delta_c \sim w = \frac{p}{\rho} = \frac{1}{3}$$

$$M_H \sim 10^{15} \text{ g} \left(\frac{t}{10^{-23} \text{ s}} \right)$$

$$\beta(M) \sim \int_{\delta_c}^{\infty} P(\delta(M_H)) d\delta(M_H)$$

Gaussian spectrum

$$\beta(M) = \text{erfc} \left(\frac{\delta_c}{\sqrt{2}\sigma(M_H)} \right)$$

$$\sigma(M_H) \sim 10^{-5}$$

CMB scale

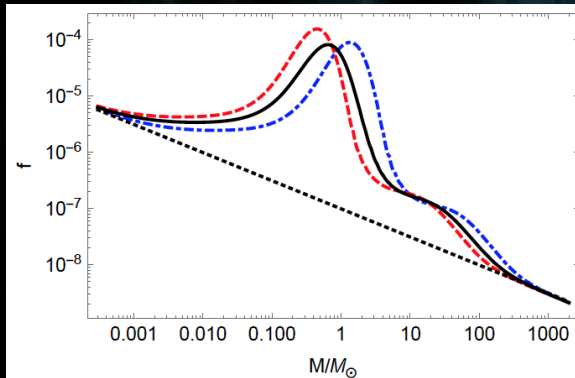
$$\sim 10^5 \exp [-(10^5)^2]$$

Mass fraction in PBHs strongly suppressed in standard inflation.
 \Rightarrow **Fine-tuned inflation models**

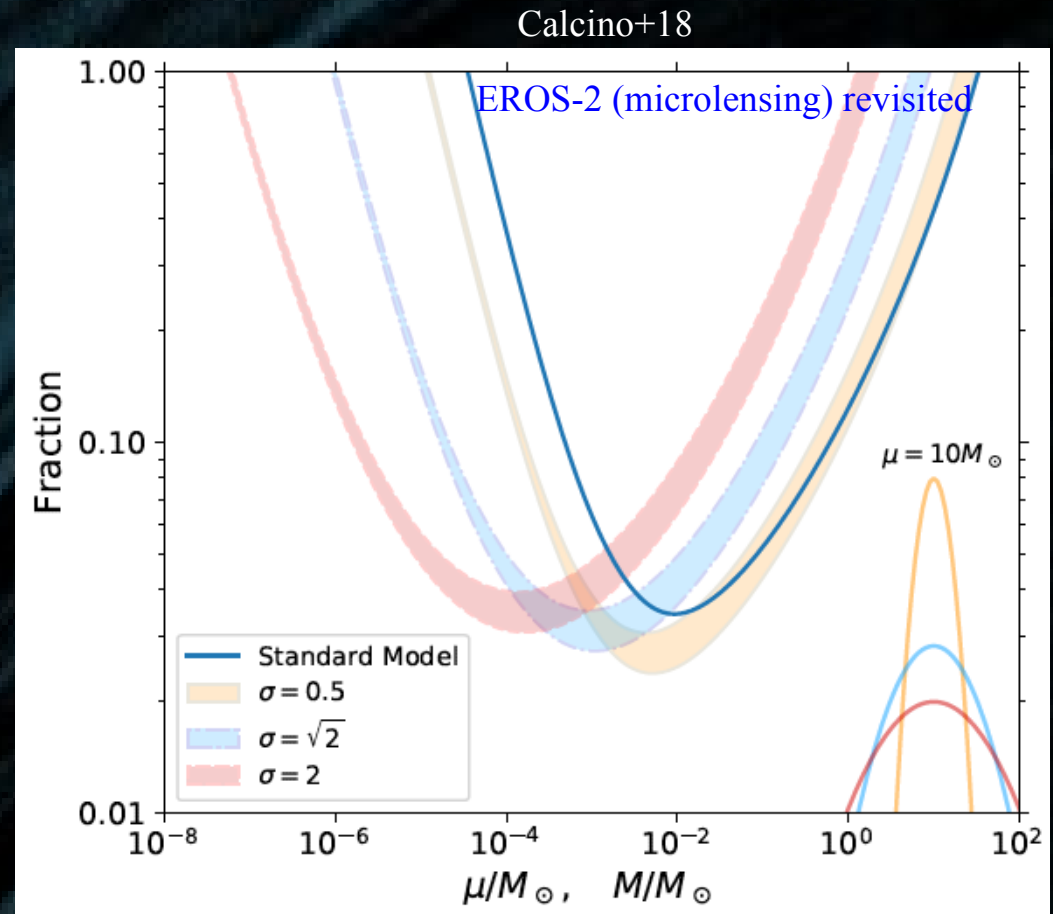
Primordial black holes

- * Most (past) constraints based on assuming peak mass function
- * Huge effort to reconsider them (e.g. Green+, Kamionkowski+, Carr+, Garcia-Bellido+)
- * Typically two windows: below and above microlensing constraints.
- * If mass function extended enough, PBHs could be ~100% of DM
 - if 1-100 Msun, might solve core/cusp
 - GW with < 1 Msun a specific signature

$$M = kM_{\text{H}}(\delta - \delta_{\text{c}})^{\gamma}$$



Byrnes+18 – impact of QCD PT
Extended mass function (logN)
(also Choptuik; Niemeyer & Jedamzik; Musco+)



Caveat:

potentially strong constraints from lensing of SNe Ia for $M_{\text{pbh}} > 1 M_{\text{sun}}$
→ see Zumalacarregui & Seljak '17 (PBHs < 0.4 CDM)

Thermal production in the early Universe

Assume DM particle coupled to SM:

→ **Production** of DM from plasma if $T > m$

→ **Chemical equilibrium** if production rate $>$ expansion rate

(then production = annihilation)

→ **Annihilation** if $m > T$ (species is **depleted**)

→ Annihilation ceases when rate $<$ expansion rate

⇒ **Freeze out (or in)** ↔ **relic abundance**

Thermal contact (DM temperature) ensured by both

* production/annihilation;

* **elastic scattering**.

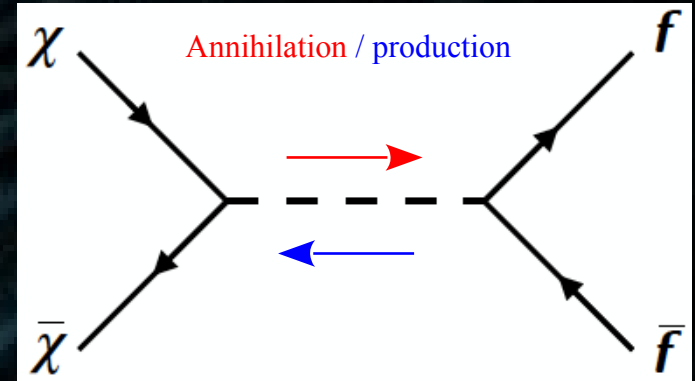
After freeze out, DM still thermally coupled to plasma.

Thermal/kinetic decoupling

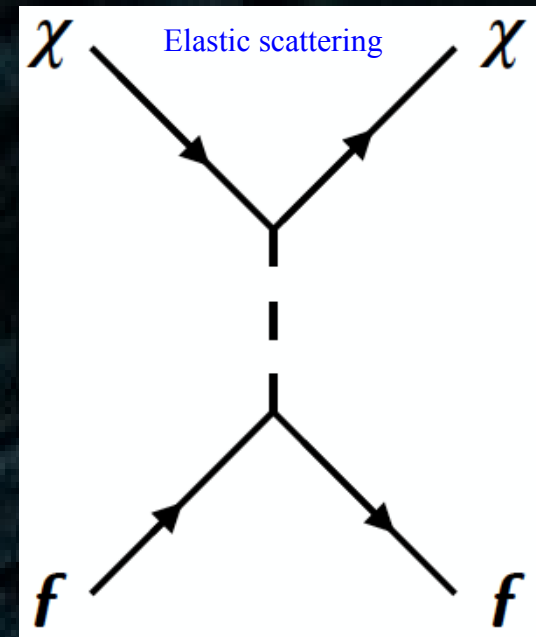
when scattering rate $<$ expansion rate

⇒ **Free streaming** DM particles

⇒ Sets the **minimal size of DM structures**



$$\Gamma_{\text{ann}} = n_{\chi} \langle \sigma_{\text{ann}} v \rangle$$



$$\Gamma_{\text{scatt.}} = n_f \langle \sigma_{\text{scatt}} v \rangle$$

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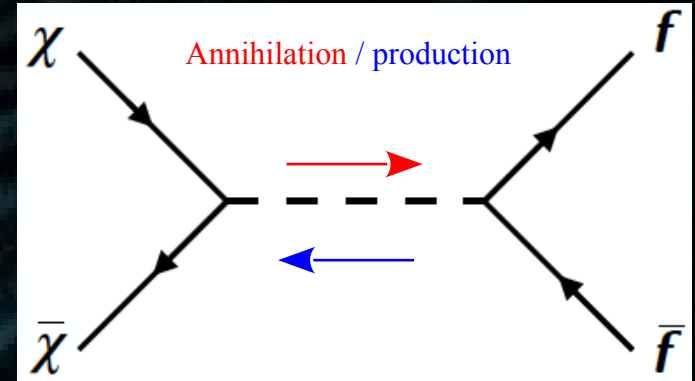
when scattering rate < expansion rate

⇒ **Free streaming** DM particles

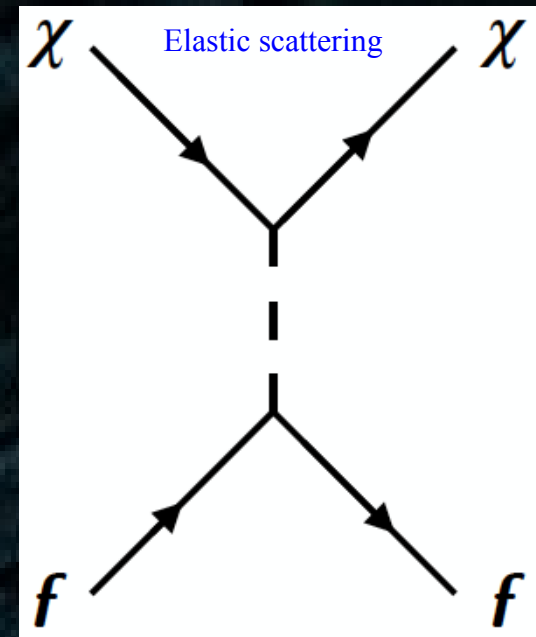
⇒ Sets the **minimal size of DM structures**

Solve moments of Liouville-Boltzmann equation for coupled species

$$\frac{d f(x^\mu, p^\mu)}{d\lambda} = \hat{C}[f]$$



$$\Gamma_{\text{ann}} = n_\chi \langle \sigma_{\text{ann}} v \rangle$$

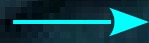


$$\Gamma_{\text{scatt.}} = n_f \langle \sigma_{\text{scatt}} v \rangle$$

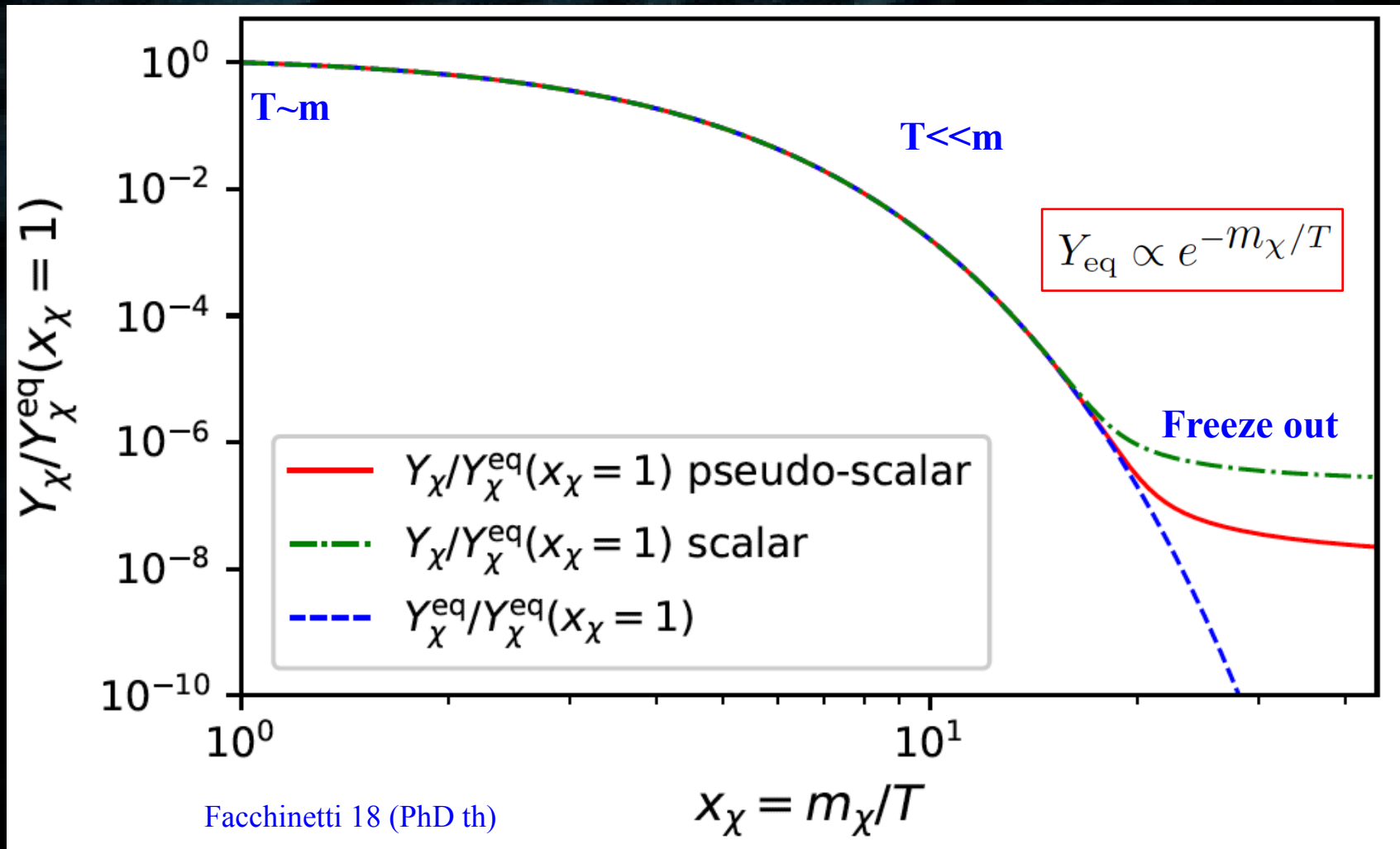
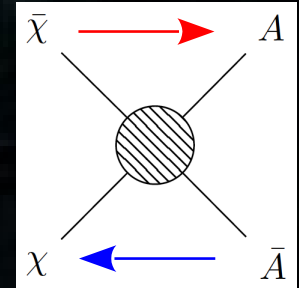
Thermal production in the early Universe

Master equation: Boltzmann equation (e.g. Lee & Weinberg '77, Bernstein+'85-88)

$$\frac{d f(x^\mu, p^\mu)}{d\lambda} = \hat{C}[f]$$



$$\frac{dY_\chi}{dx} \propto \frac{g_*^{1/2}(x)}{x^2} \langle \sigma v \rangle \{ Y_{\chi,eq}^2 - Y_\chi^2 \}$$



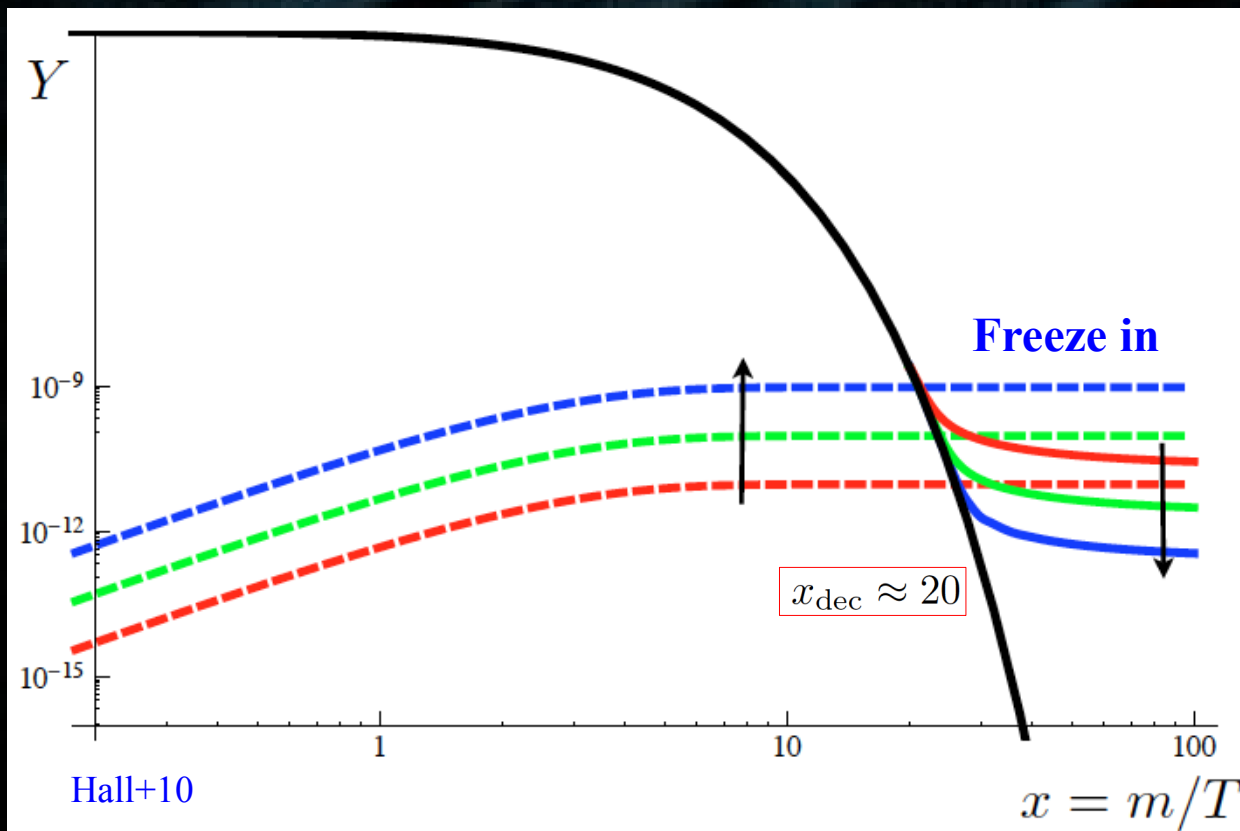
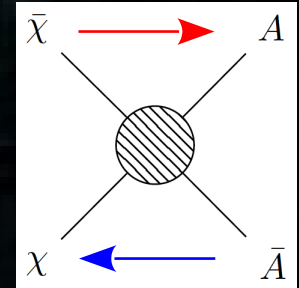
Thermal production in the early Universe

Master equation: Boltzmann equation (e.g. Lee & Weinberg '77, Bernstein+'85-88)

$$\frac{df(x^\mu, p^\mu)}{d\lambda} = \hat{C}[f]$$



$$\frac{dY_\chi}{dx} \propto \frac{g_\star^{1/2}(x)}{x^2} \langle \sigma v \rangle \{ Y_{\chi,eq}^2 - Y_\chi^2 \}$$



Freeze-in mechanism:

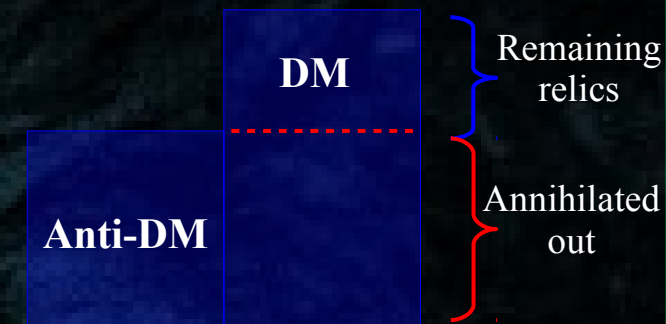
Dodelson & Widrow '94
McDonald '02
Hall+ 10

$$\Omega_{\text{WIMP}} \tilde{\propto} \frac{1}{g_\star^{1/2}(x_{\text{dec}}) \langle \sigma v \rangle}$$

$$\Omega_{\text{FIMP}} \tilde{\propto} g_\star^{1/2}(x_{\text{dec}}) \langle \sigma v \rangle$$

$$\langle \sigma_{\chi\bar{\chi}} v \rangle_{\text{FIMP}} \ll \langle \sigma_{\chi\bar{\chi}} v \rangle_{\text{WIMP}}$$

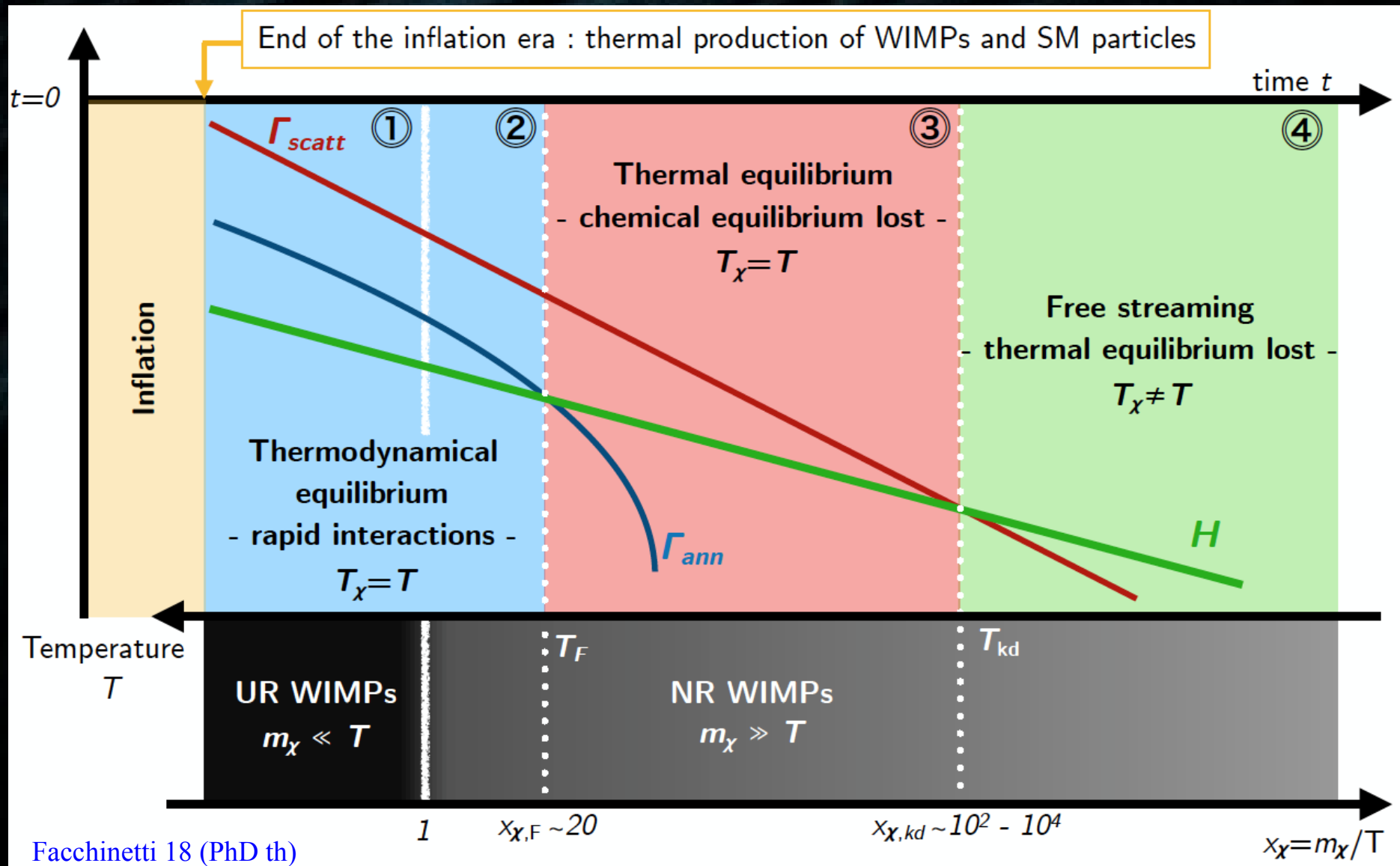
Asymmetric DM (Nussinov' 85)



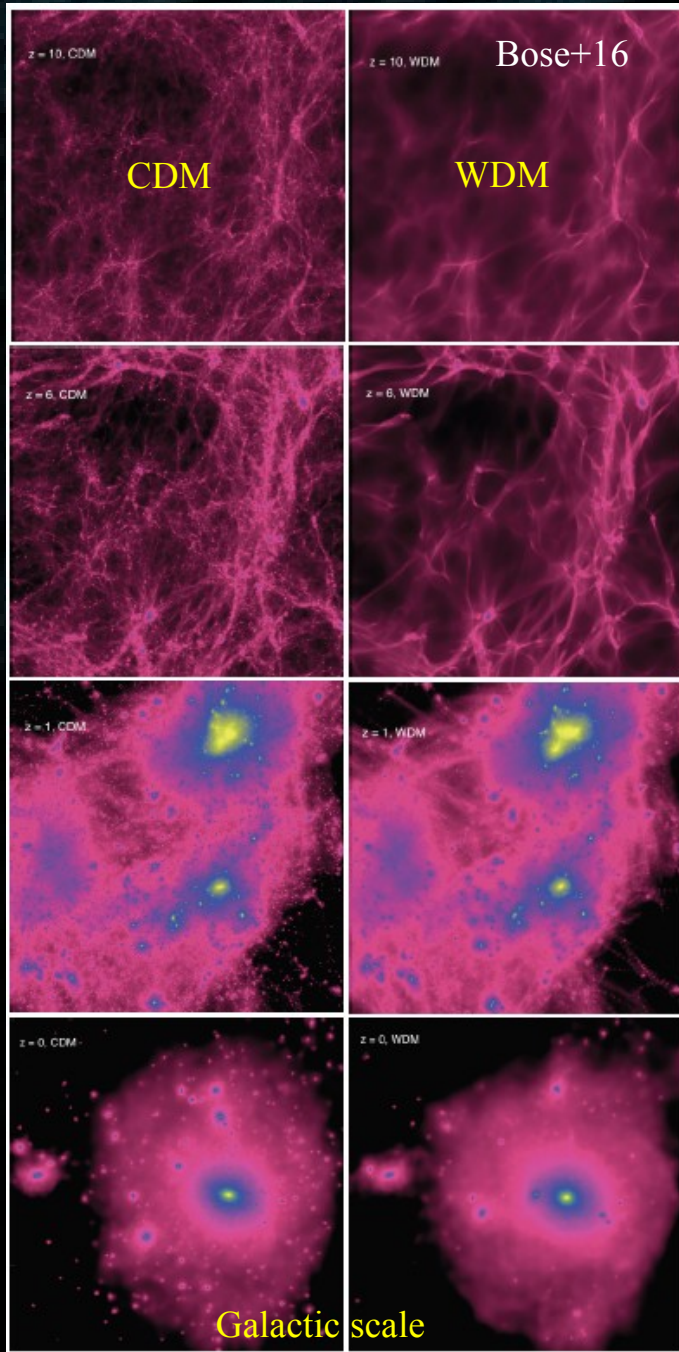
$$\langle \sigma_{\chi\bar{\chi}} v \rangle_{\text{ADM}} > \langle \sigma_{\chi\bar{\chi}} v \rangle_{\text{WIMP}}$$

All this picture is also valid for self-interacting dark matter (SIDM)
→ generic properties: extended dark sector (interaction mediators)

Thermal production in the early Universe



Kinetic decoupling, free streaming scale, and small-scale structures



$$\lambda_{\text{fs}} = a_{\text{eq}} \int_{t_{\text{kd}}}^{t_{\text{eq}}} dt \frac{v(t)}{a(t)} \approx v_{\text{kd}} (a_{\text{kd}}/a_{\text{eq}}) / H_{\text{eq}}$$

- * Density perturbations grow efficiently after matter-radiation equivalence
- * Kinetic decoupling time sets free-streaming scale
- * Other competing effects (collisional damping)

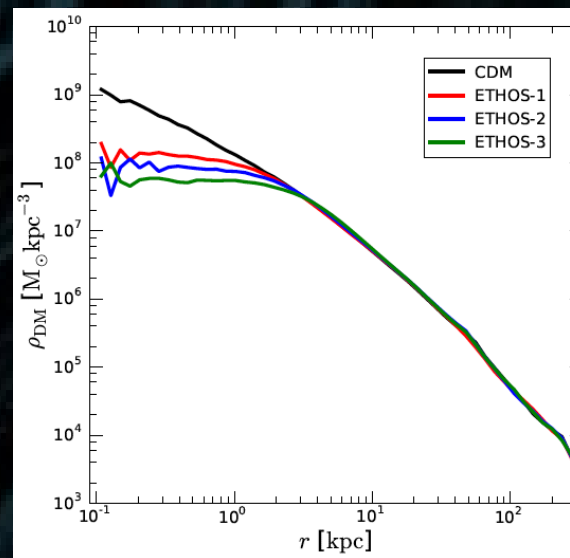
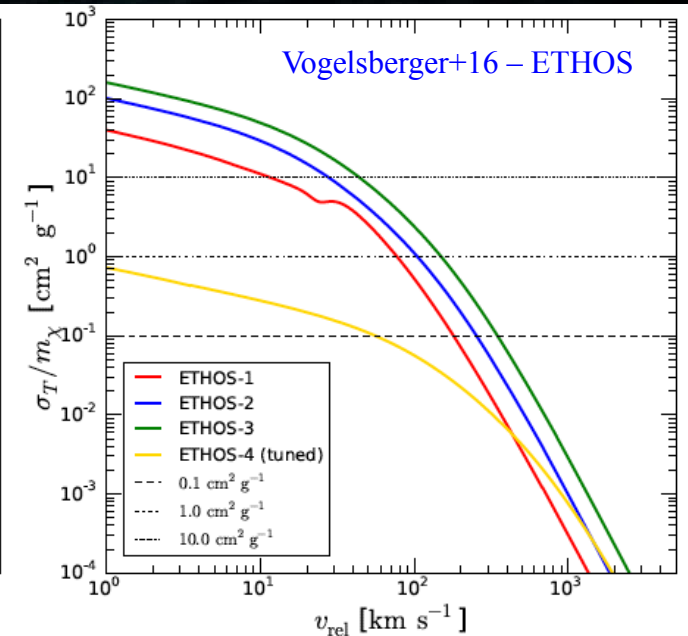
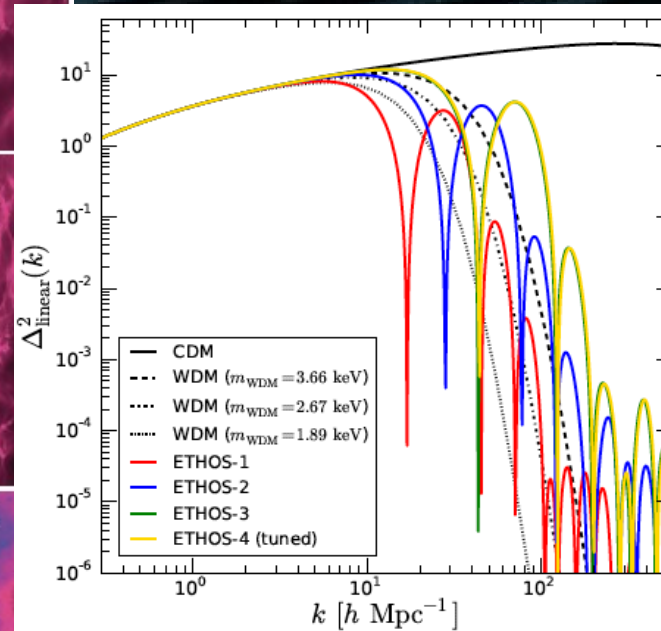
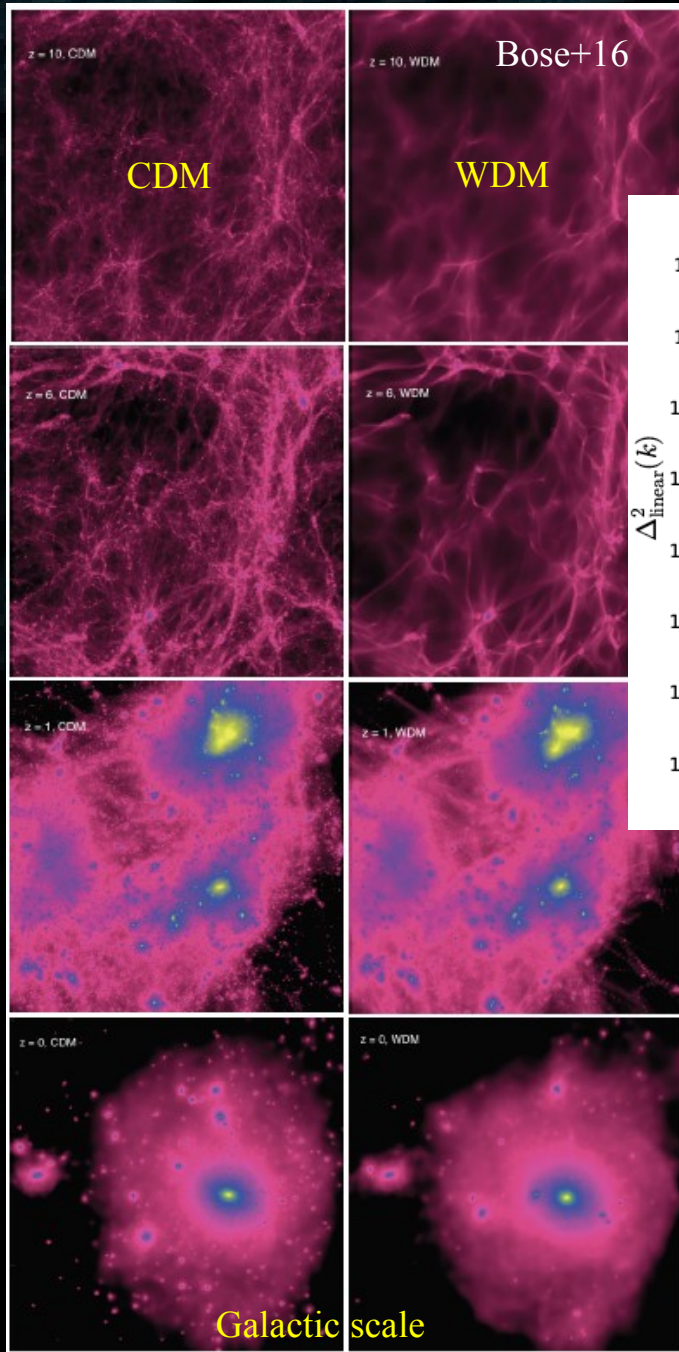
=> Minimal size of structures have impact on DM searches

=> Depends on DM interaction properties

[e.g. Hofmann+01, Berezhinsky+03, Green+04-05, Bertschinger 06, Bringmann+07, Facchinetti+ in prep.]

Kinetic decoupling, free streaming scale, and small-scale structures

$$\lambda_{\text{fs}} = a_{\text{eq}} \int_{t_{\text{kd}}}^{t_{\text{eq}}} dt \frac{v(t)}{a(t)} \approx v_{\text{kd}} (a_{\text{kd}}/a_{\text{eq}})/H_{\text{eq}}$$



CDM candidates: minimal scale of structures depend on interactions. For TeV particle, can be $\sim 10^{-10} \text{ M}$

SIDM: self-interactions set cores in massive objects (not in light objects).

Dark matter in the Milky Way

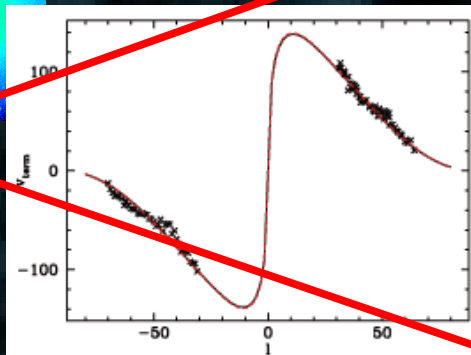
→ GAIA: THE GALACTIC CENSUS TAKES SHAPE



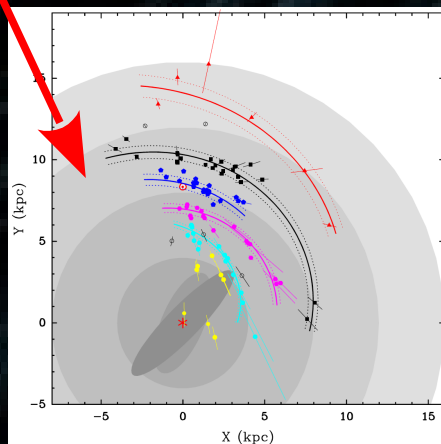
Making predictions for DM searches?

The Milky Way a strongly constrained system!
(specific history + properties + observational data)

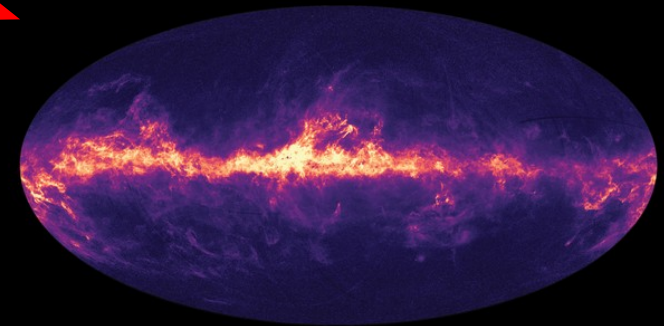
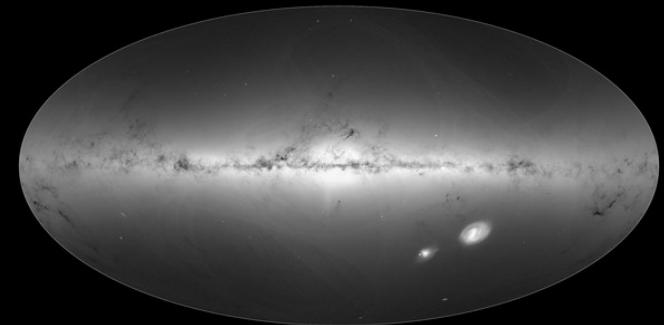
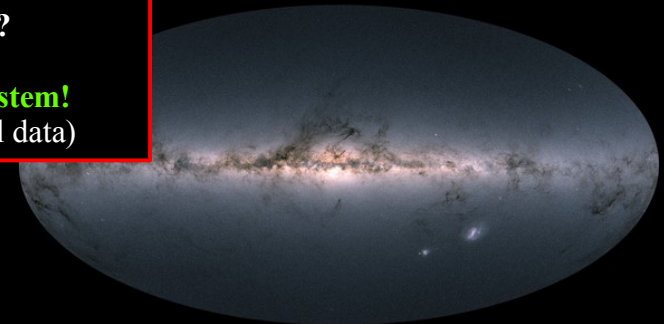
Cannot be a mere rescaling!



MW terminal velocities, McMillan '11



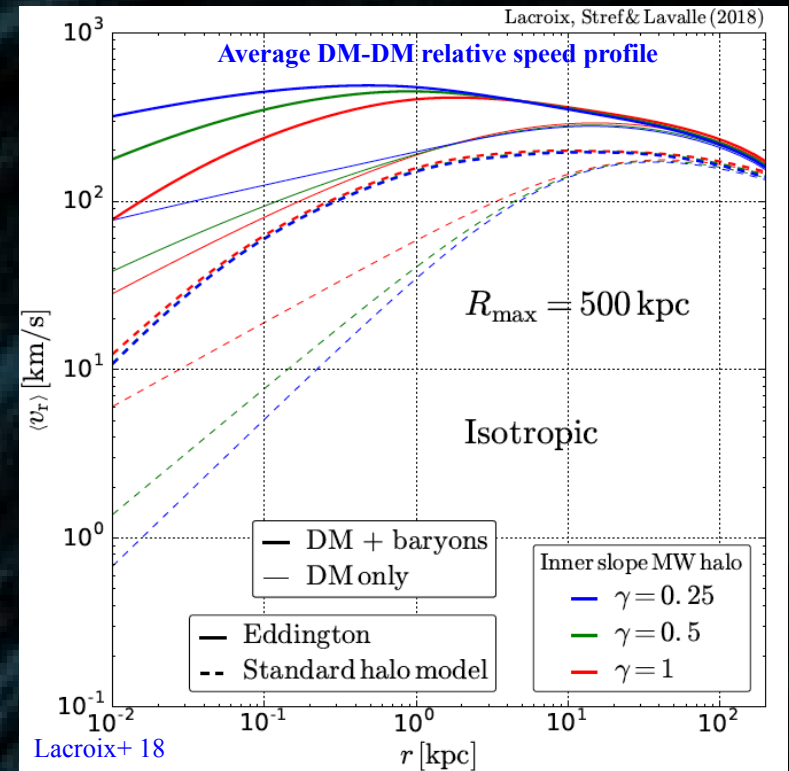
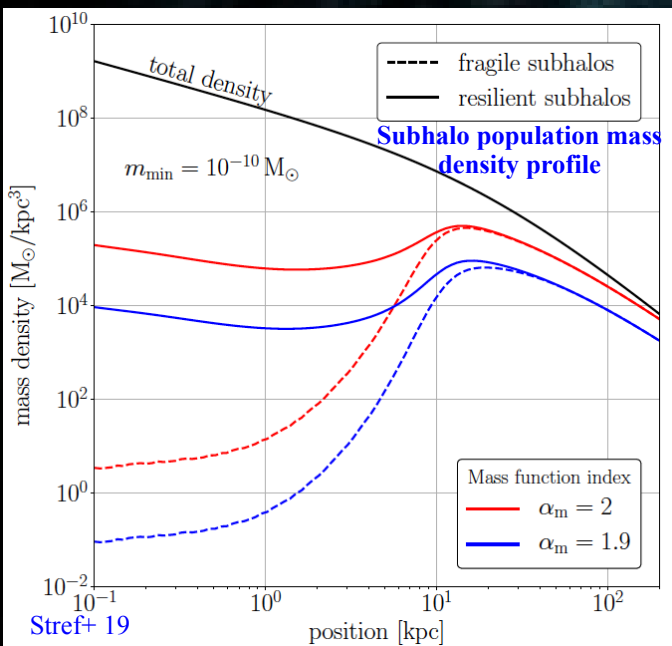
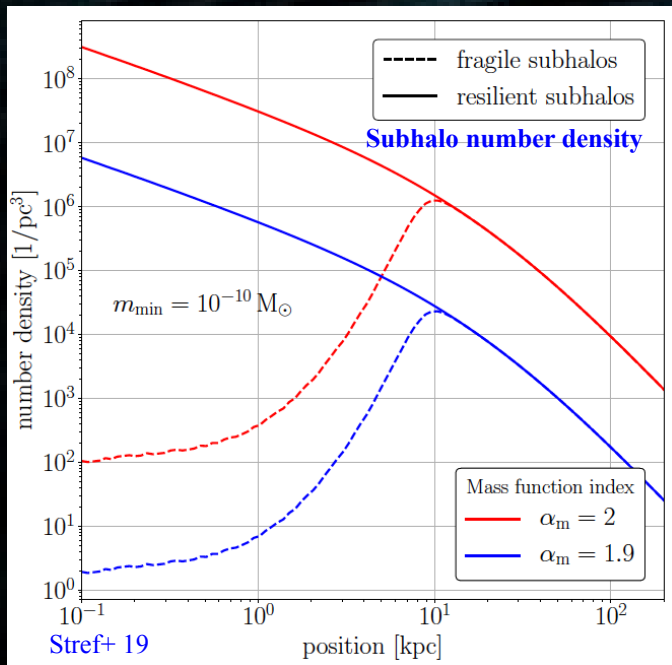
MW masers, Reid+14



Gaia: Data Release 2 (DR2) @ESA

Constrained MW mass models matter in predicting/constraining ...

The Galactic subhalo population down to the tiniest masses
→ Subhalo number density + mass density profiles

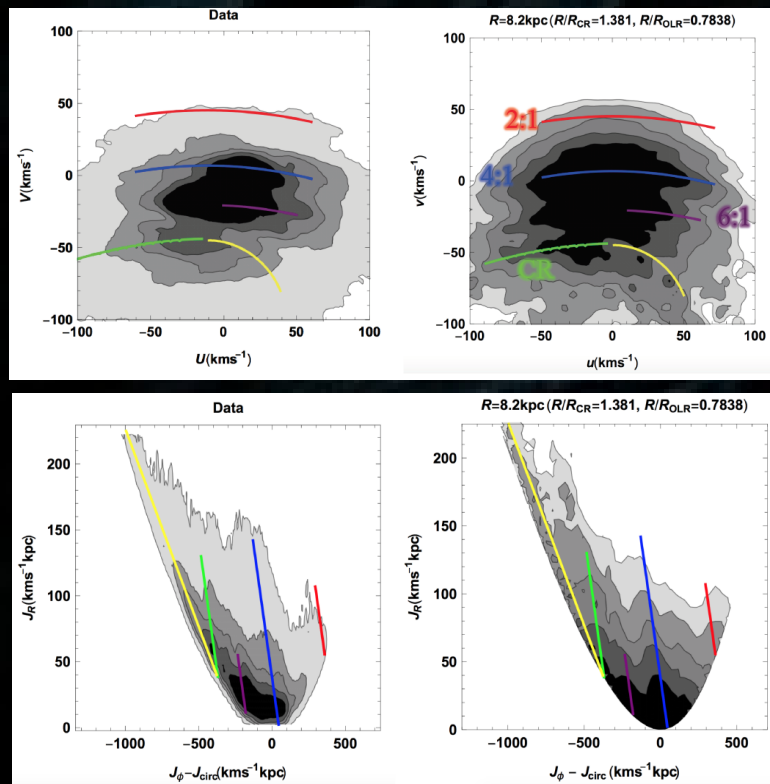


The velocity distribution of dark matter
→ moments of the relative speed from improved Eddington equation

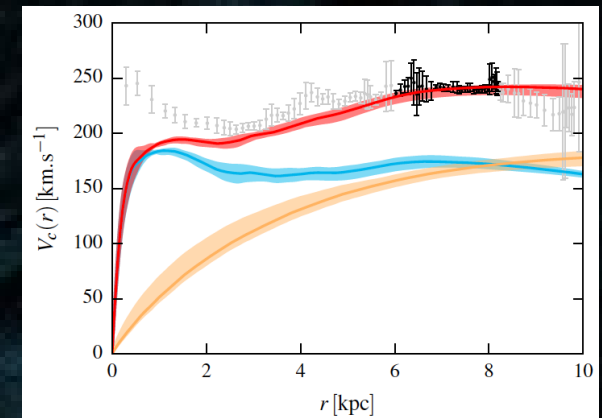
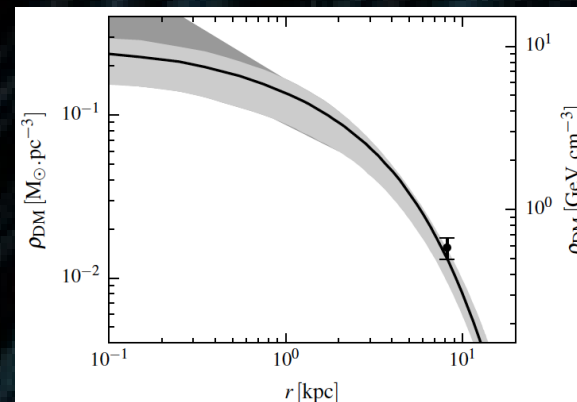
Will improve with Gaia

Local dynamics probed with Gaia

- * Jeans theorem: Phase-space distribution of steady-state system naturally described by functions of closed integrals of motion
- * Natural basis is: action (\mathbf{J}) and angle ($\boldsymbol{\theta}$) conjugate variables; the Hamiltonian reads $H(\mathbf{J})$ (Binney & Tremaine '08)
- * At equilibrium, $f_0(\mathbf{J})$ solution of collisionless Boltzmann equation
- * Take perturbations of the bar and spiral arms into account: **resonances (trapped orbits)**!
 \Rightarrow new set of action-angle coordinates (Monari, Famaey, Fouvry, Binney '17)
 \Rightarrow applied to **Gaia DR2** (Monari, Famaey, Siebert, Wegg & Gerhard '19), using Galactic bar model of Portail+'17

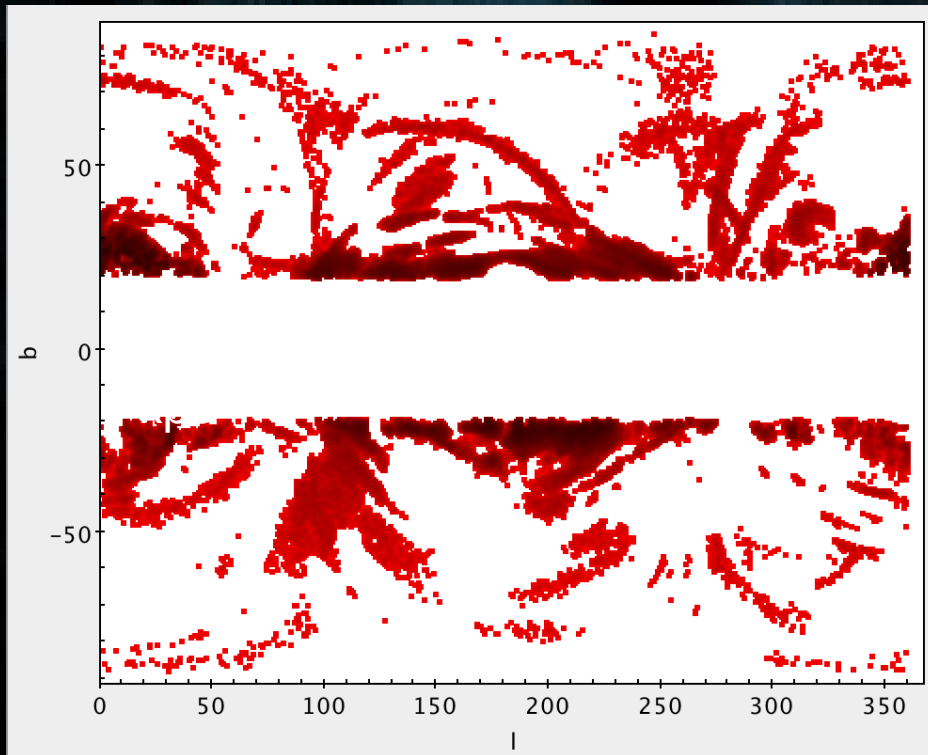


- Sample of 3×10^5 stars within 200 pc + bar model only (no spiral arms)
- \Rightarrow find the predicted resonant orbits in the data!
- \Rightarrow somewhat a unique long-distance test of the Portail+ bar model
- \Rightarrow favors a DM core at the Galactic center (but doesn't match inner RC)



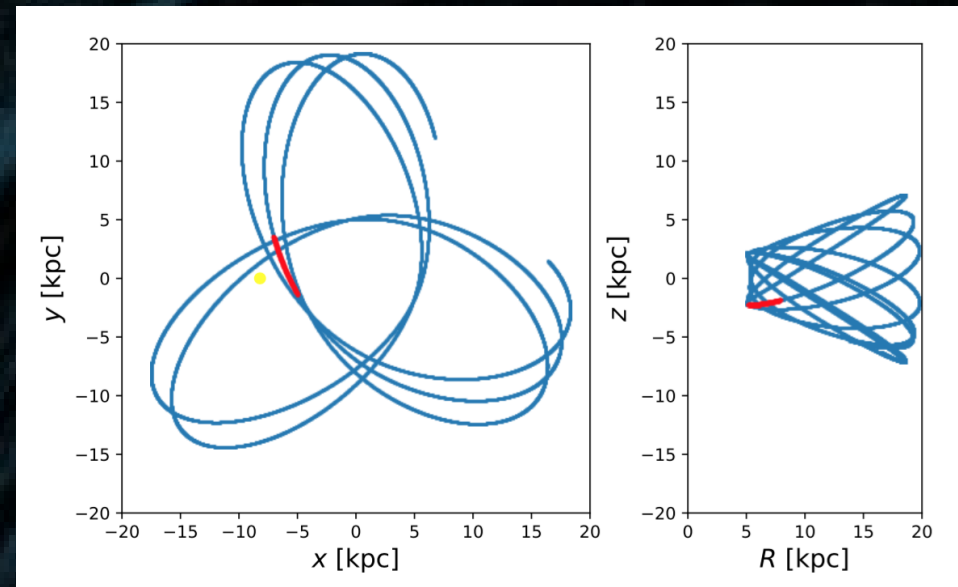
Global dynamics probed with Gaia

Streams (Ibata et al.):



>10 new confirmed streams in total

Integrate streams orbits by exploring all distances and radial velocities until stream candidate found (STREAMFINDER)



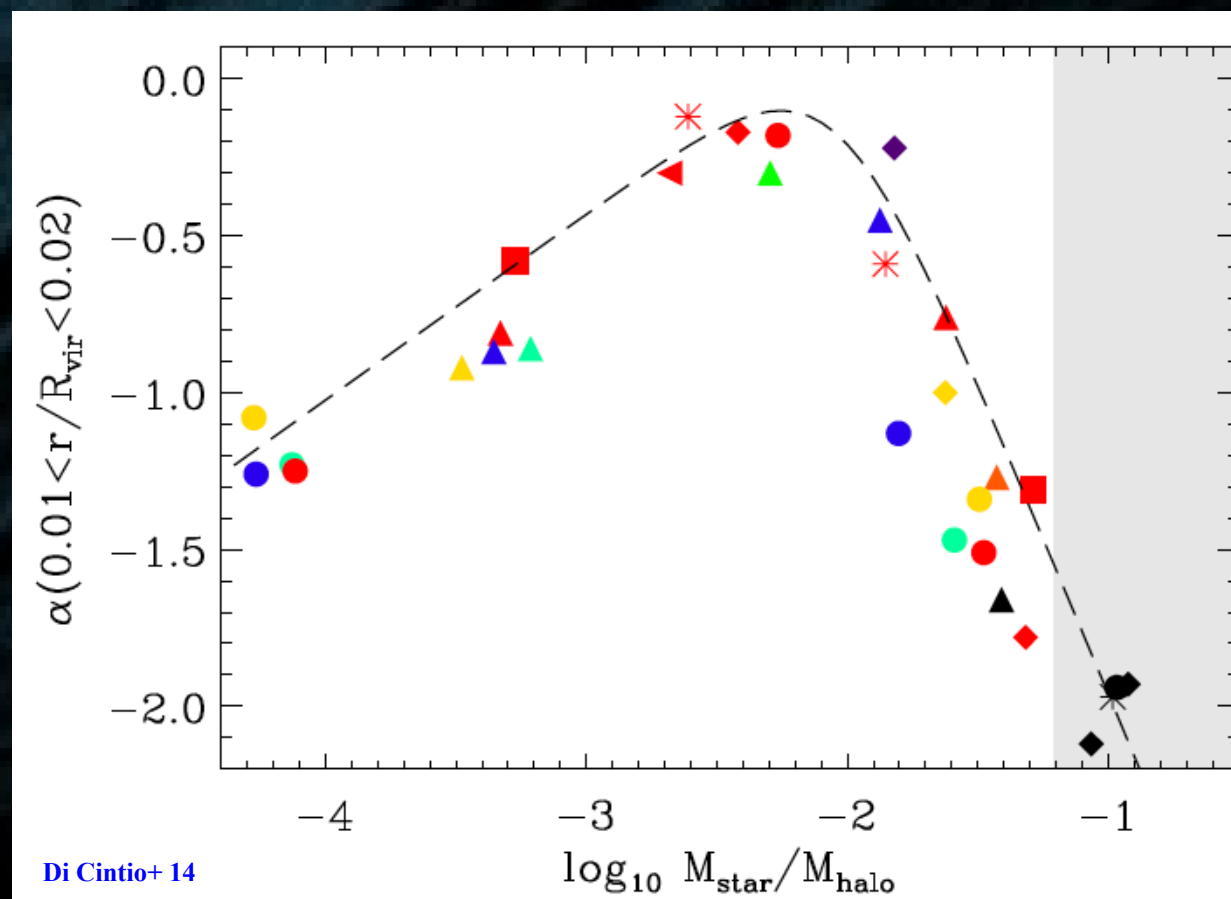
Phlegethon: a faint nearby (3.8 kpc) disk-like retrograde stream (~ 2580 M) Ibata et al (2018)

Stellar streams: a powerful probe of global dynamics + subhalos (e.g. heating and gaps)

Conclusions

- * DM candidates
 - no longer particle-theory driven
 - focus on production mechanism and interaction properties vs. observational signatures
 - a rich phenomenology, but many potentially observable signatures
 - astrophysical (multiwavelength+multimessenger – photons, neutrinos + gravitational) + cosmological observations (CMB+21cm+Ly-alpha) very powerful probes
- * The Milky Way (MW) itself provides many probes of fundamental dark matter properties
- * MW is a single object:
 - detailed properties NOT predicted by cosmological simulations (specific baryonic distribution, merger history, etc.)
 - not overstate the theoretical consequences of (non)observations (e.g. core/cusp in the MW)
- * Strong complementarity with other probes (other galaxies, other scales, other ages).
- * Dark matter structuring properties on small scales very important (far below resolution of cosmological simulations → need to build and rely on analytical models) → strong impact on several observables + gravitational searches
- * Gaia DR2: (already) impressive improvement on dynamical understanding of MW (incl. merger history).
 - global dynamics (DM halo + gravitational potential)
 - local dynamics (local DM density)
 - subhalos (gaps in stellar streams, etc.)
- * A lot theoretical/modeling work needed to improve predictions

Backup



Di Cintio+ 14

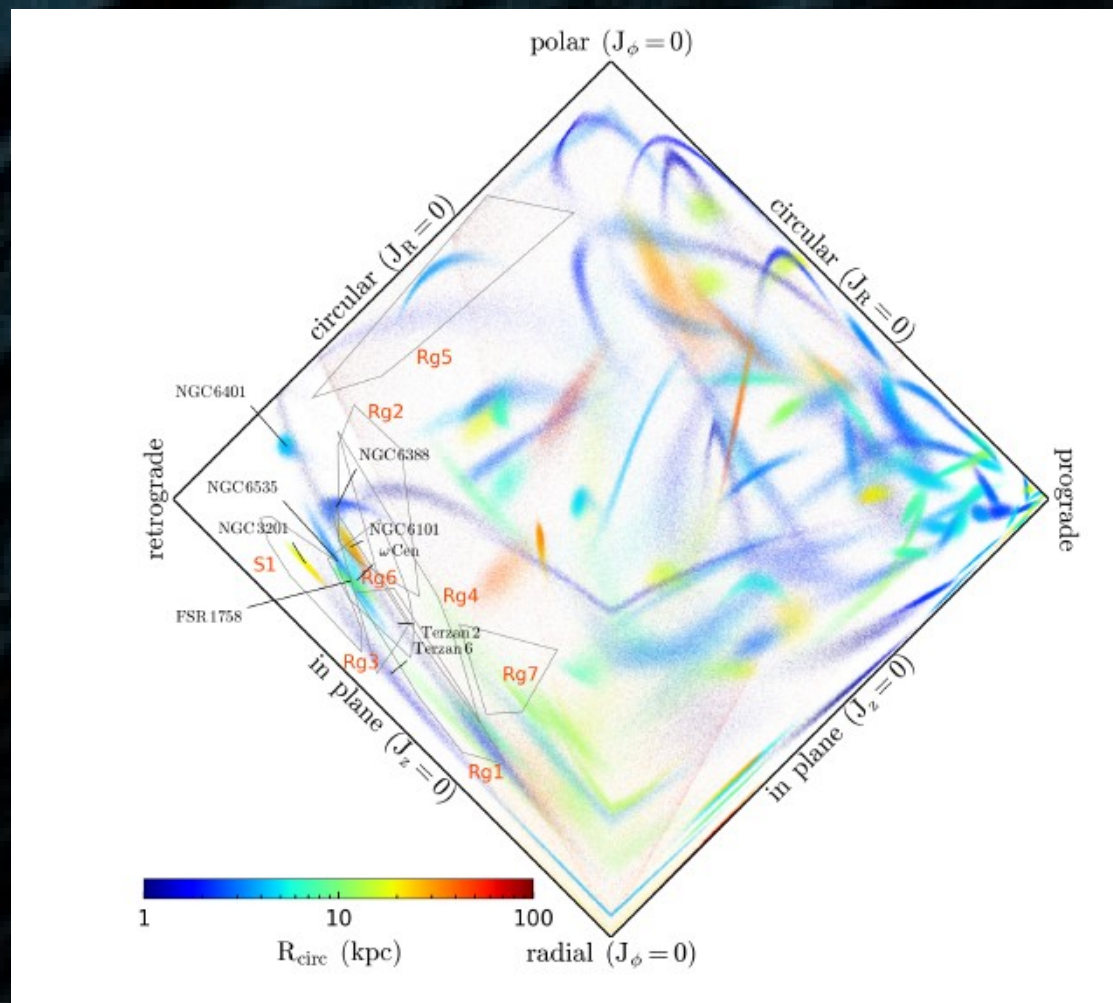
Evidence for Two Early Accretion Events That Built the Milky Way Stellar Halo

G. C. Myeong¹, E. Vasiliev^{1,2}, G. Iorio¹, N. W. Evans¹, V. Belokurov¹

¹*Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK*

²*Lebedev Physical Institute, Leninsky Prospekt 53, Moscow 119991, Russia*

arXiv:1904.03185v1



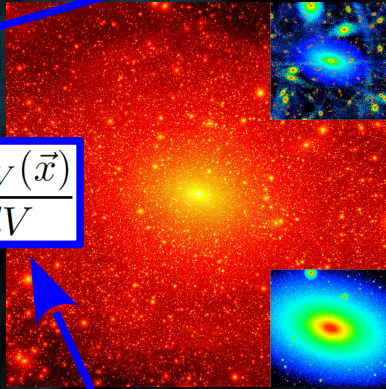
Defining the whole subhalo “phase space”

At MW formation, all (cosmological) properties factorize out

$$\frac{d^n N^0}{d\omega^n} = N_0 \frac{d\mathcal{P}_V^0(\vec{x})}{dV} \times \frac{d\mathcal{P}_m^0(m)}{dm} \times \frac{d\mathcal{P}_c^0(c, m)}{dc}$$

$$\frac{d\mathcal{P}_V^0(\vec{x})}{dV} = \frac{\rho_{\text{tot}}(\vec{x})}{M_h} = \frac{d\mathcal{P}_V(\vec{x})}{dV}$$

Hard sphere approx:
subhalos track the
evolving DM
distribution, even
after disruption.
=> redistribution of
DM from subhalos
to the smooth
component.



$$\frac{d^n \bar{N}}{d\omega^n} = \frac{\bar{N}_{\text{tot}}}{\bar{K}_w} \frac{d\bar{\mathcal{P}}_V(\vec{x})}{dV} \times \frac{d\bar{\mathcal{P}}_m(m, \vec{x})}{dm} \times \frac{d\bar{\mathcal{P}}_c(c, m, \vec{x})}{dc}$$



1st step: compute tides induced by final MW halo
=> parameter space becomes intricate!

=> generic enough to be calibrated from simulations
=> subhalo mass fraction $\sim 10\%$ in range $(10^{-5}, 10^{-2}) M_h$
(eg Diemand+08) fixes N_{tot}

2nd step: compute tides induced by MW baryons
=> parameter space even more intricate

=> CANNOT be calibrated from simulations

$$\frac{d^n N}{d\omega^n} = \frac{N_{\text{tot}}}{K_w} \frac{d\mathcal{P}_V(\vec{x})}{dV} \times \frac{d\mathcal{P}_m(m, \vec{x})}{dm} \times \frac{d\mathcal{P}_c(c, m, \vec{x})}{dc}$$

Tides from stellar encounters and disk shocking

Encounters with stars:

(Ostriker+, Weinberg+, Gnedin+, 80-00, Berezhinsky+03)

* impulse approximation during fly-by
=> negligible wrt disk shocking

$$\Delta E = \frac{1}{2} \int d^3\vec{r} \rho_{\text{int}}(r) (\delta v_x - \delta \tilde{v}_x)^2$$

$$\Delta E = \frac{2\pi}{3} \left(\frac{2G_N M_*}{v_{\text{rel}} t^2} \right)^2 \int_0^R dr r^4 \rho_{\text{int}}(r)$$

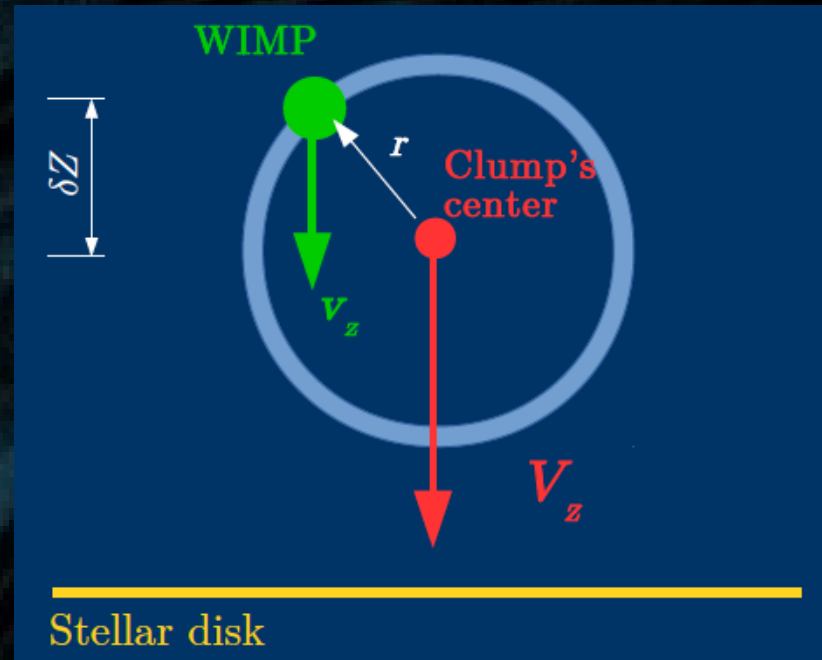
Disk shocking:

* impulse approximation during crossing
* adiabatic invariance correction
=> the dominant effect

$$\begin{aligned} \frac{dv_z}{dt} &= g_d(R, z_p) - g_d(R, z_c) \\ &\simeq \Delta z \frac{\partial g_d}{\partial z}(z_c), \end{aligned}$$

$$\Delta v_z = \int dt \Delta z(t) \frac{\partial g_d}{\partial z}[z_c(t)]$$

$$\epsilon_k(z) \equiv \frac{2 g_{z,\text{disk}}^2(z=0) z^2}{V_z^2} A(\eta)$$



Associated tidal radius

Differential definition (default)

$$r_{t,i} \text{ such that } \langle \epsilon_k \rangle(r_{t,i}) = -\tilde{\phi}(r_{t,i}, r_{t,i-1})$$

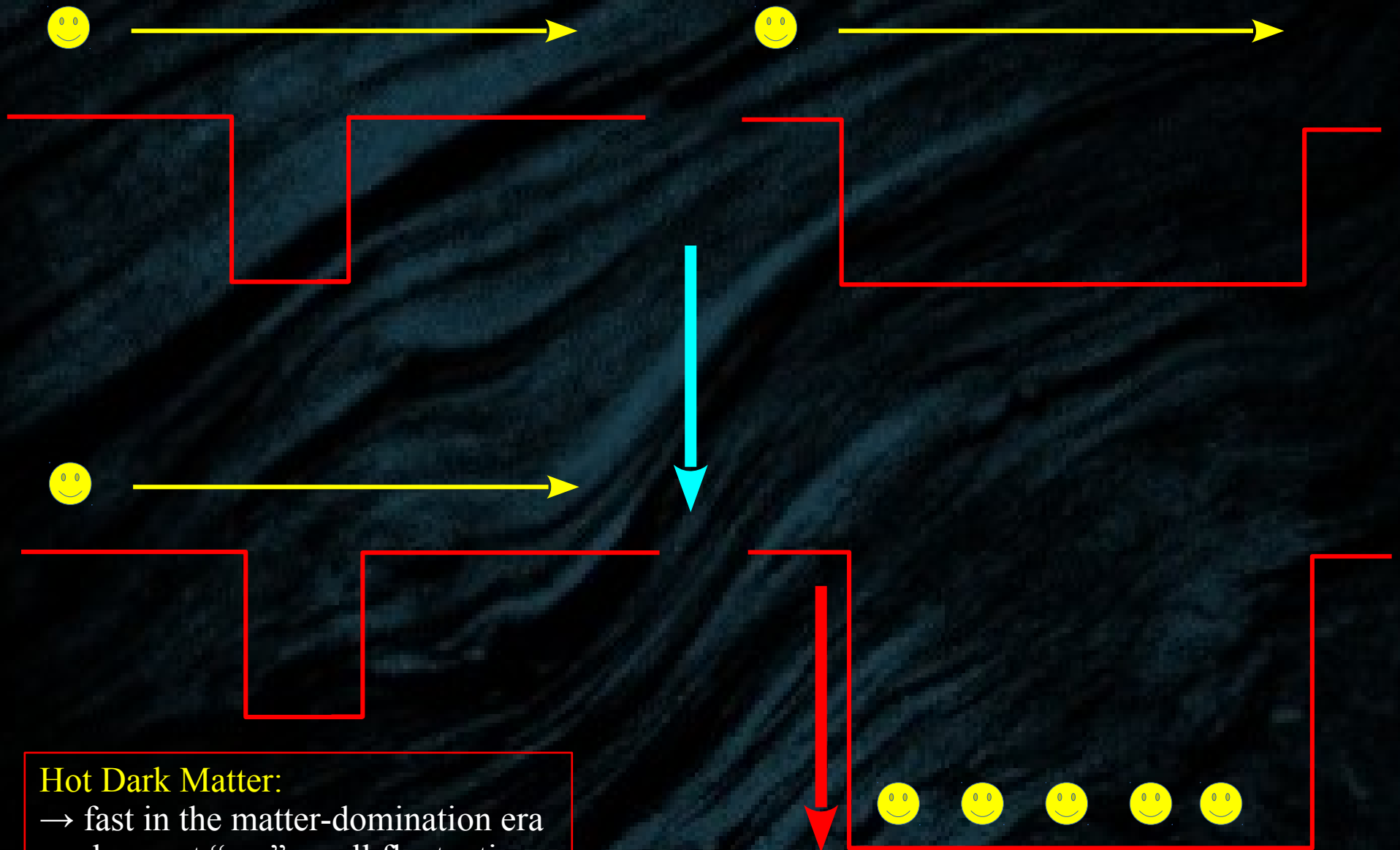
Integrated definition

$$r_t \text{ such that } N_{\text{cross}} E_k(r_t, R) = E_b(r_t)$$

Fit from D'Onghia+10

$$\frac{\tilde{E}_k(r_t, R)}{E_b(r_t)} = \frac{(1.84 r_{1/2})^2 g_{z,\text{disk}}^2}{3 \tilde{\sigma}_v^2 V_z^2}$$

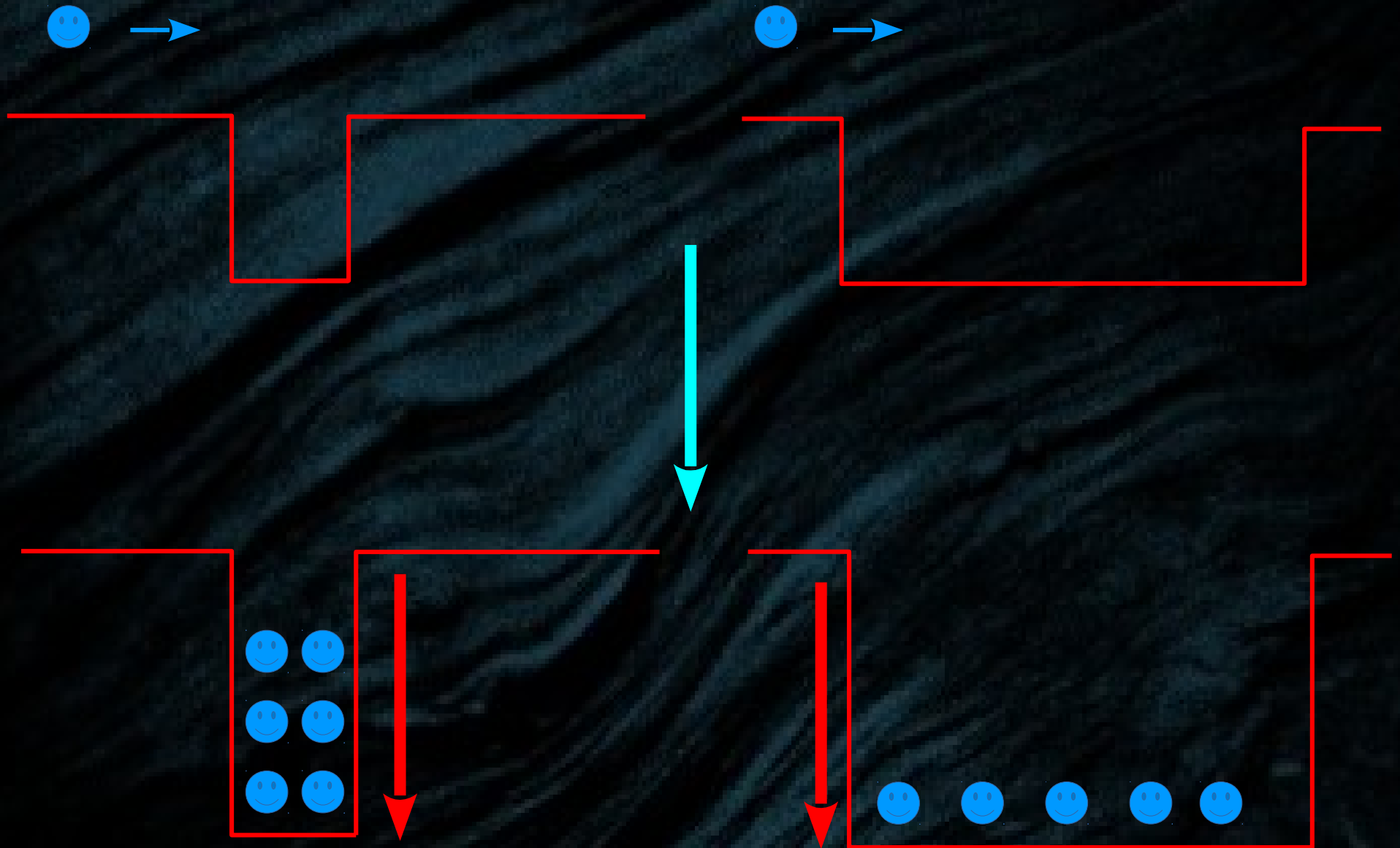
The coldness of Dark Matter



Hot Dark Matter:

- fast in the matter-domination era
- does not “see” small fluctuations
- falls only in big ones
- ⇒ Big structures form first

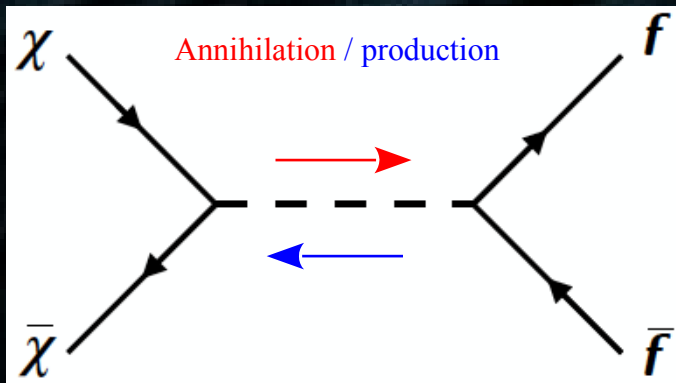
The coldness of Dark Matter



Cold Dark Matter:

- slow in matter-domination era
- falls in small fluctuations
- => small structures form first

Searches for thermal dark matter

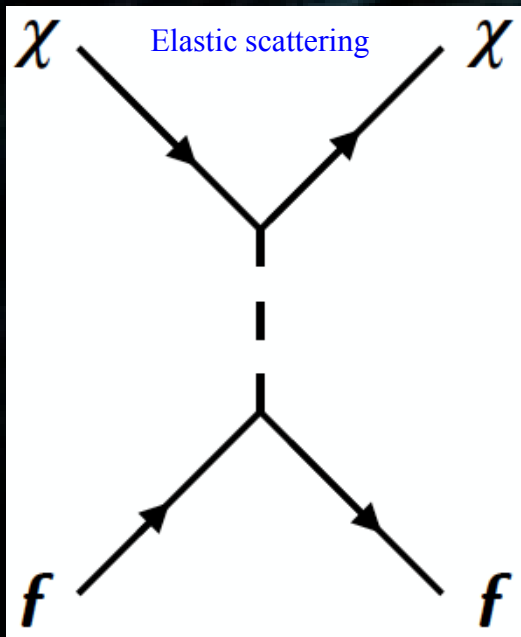


$$\Gamma_{\text{ann}} = n_{\chi} \langle \sigma_{\text{ann}} v \rangle$$

* **Production** at colliders (model dependent)
=> **collider searches**

* **Annihilation/decay** rate potentially large in
dense DM regions: **centers of halos + CMB**
=> **indirect searches**

* **Beware velocity dependence**
(scalar exchange between fermions v-suppressed;
pseudo-scalar exchange is not)



$$\Gamma_{\text{scatt.}} = n_f \langle \sigma_{\text{scatt}} v \rangle$$

* **elastic or inelastic scattering**
→ nuclear **recoils** at underground experiments
=> **direct searches**

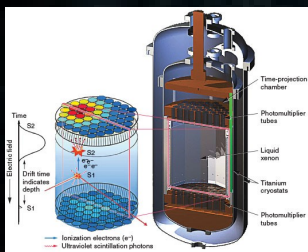
→ scattering with **astrophysical objects**
=> **stellar physics**
=> neutrinos from capture+annihilation in stars
=> **indirect searches**

* **Beware velocity dependence**
(pseudo-scalar exchange v-suppressed;
scalar exchange is not)

Astro/particle complementarity

Direct detection rate – WIMP-matter scattering

$$\frac{d\Gamma_{\chi-N}}{dE_r}(E_r, t) = \frac{\sigma_{\chi-N} F^2(E_r)}{2\mu_r^2} \frac{\rho_\odot}{m_\chi} \int_{v>v_{\min}} d^3\vec{v} \frac{f(\vec{v}, t)}{v}$$



Annihilation vs. scattering

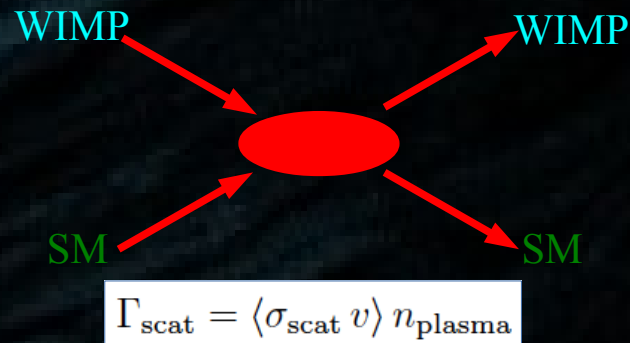
=> constraints from cosmological abundance
+ minimal scale for DM structures
(subhalos)

Dark matter profile + phase space (+ cosmic-ray transport)

=> constrained by Milky Way-mass model
(full gravitational potential DM +
baryons)

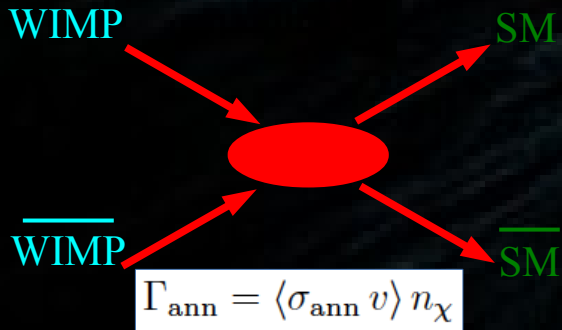
Scattering

(→ kinetic decoupling in early universe
+ subhalo mass cutoff)



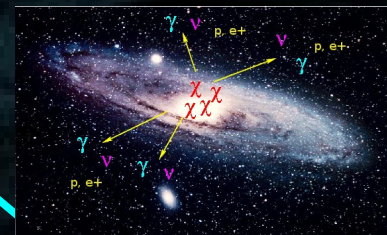
Annihilation

(→ chemical decoupling in early universe)



Indirect detection rate (e.g. gamma rays)
– WIMP annihilation

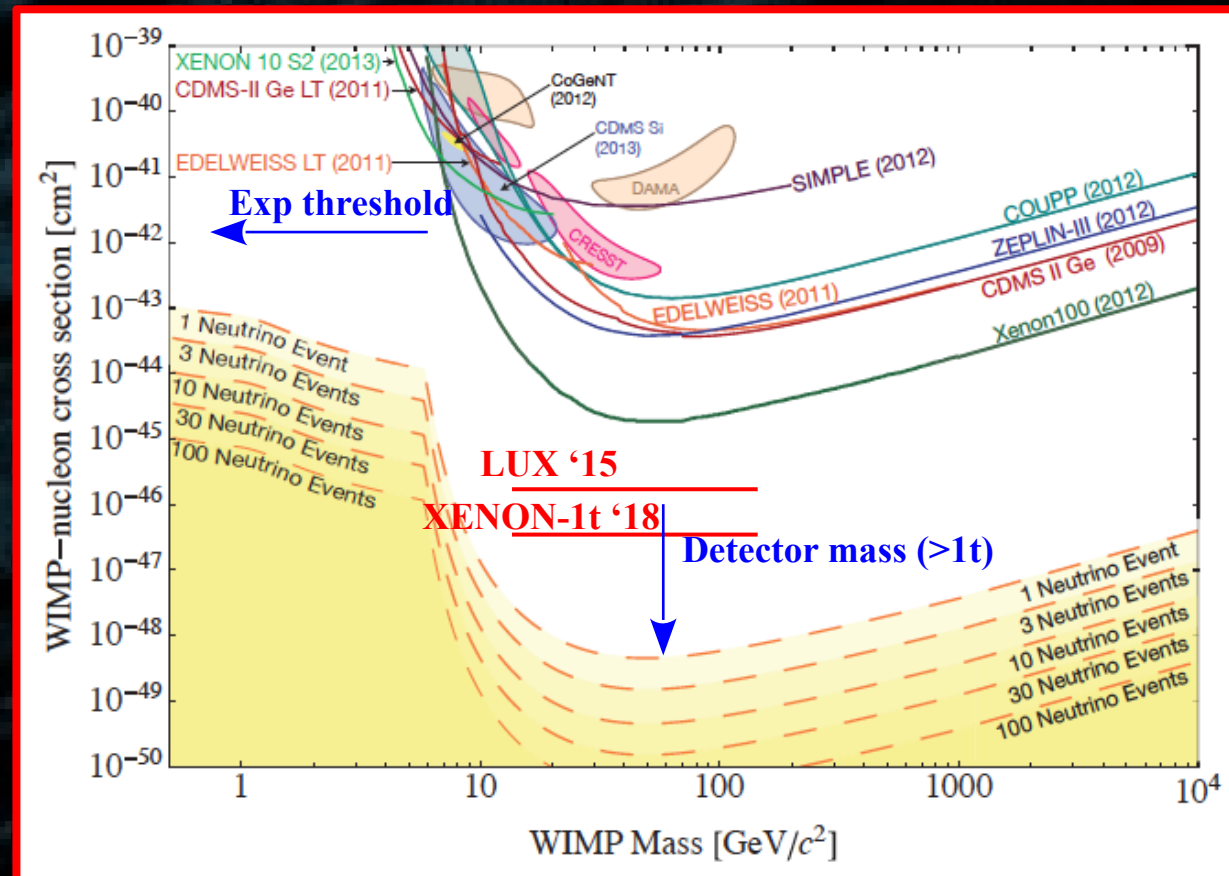
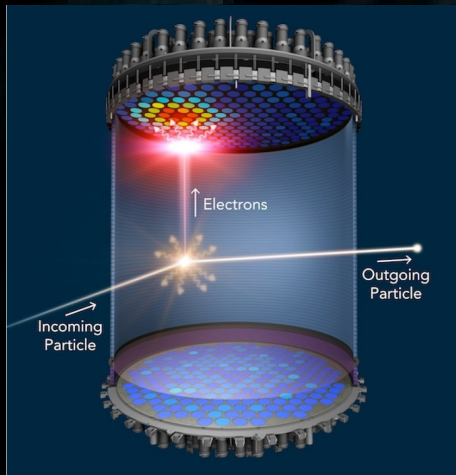
$$\frac{d\phi_{\gamma}^{\text{ann.}}}{dE} = \frac{\delta \langle \sigma v \rangle}{4\pi} \frac{dN_{\gamma}}{dE} \int_{\text{res.}} d\Omega \int_{\text{l.o.s}} dl \left[\frac{\rho(r)}{m_{\chi}} \right]^2$$



Direct WIMP searches

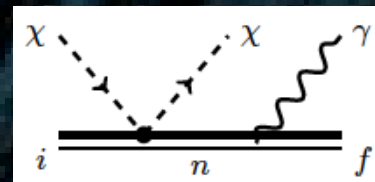
Billard+ 13

XENON-1t results:
=> the sub-zepto-barn era!

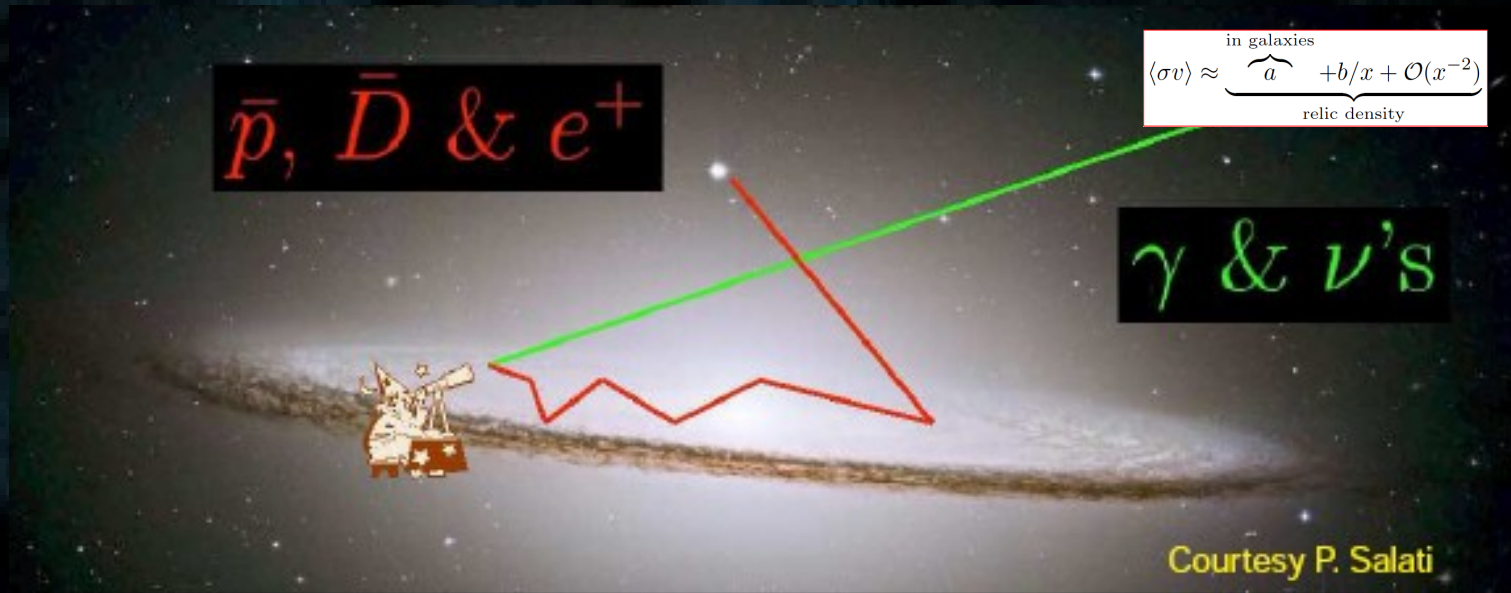


Also sensitive at lower energy:

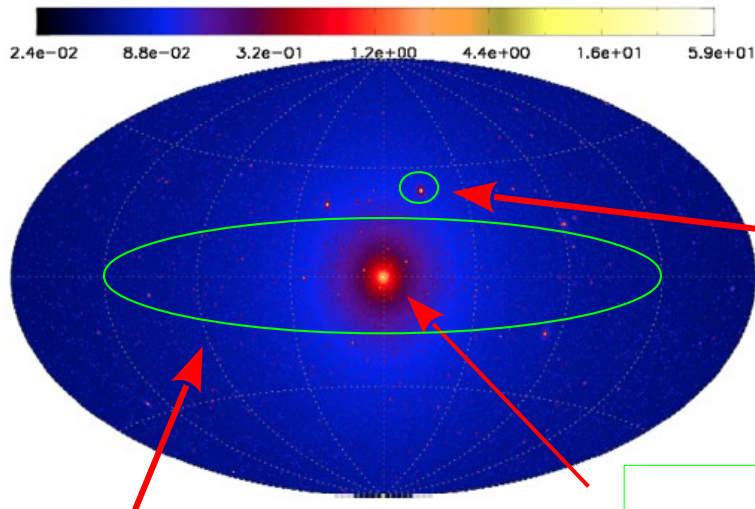
- * electronic recoils (e.g. Essig+12)
- * Bremsstrahlung (e.g. Pradler & Kouvaris 17)



Up to the skies!



Pieri, JL+ '11



Diffuse gamma-ray emission

=> check spectral/spatial properties wrt background

Requirements (and/or):

- * **clean signal**
(spectral lines or features)
- * **large signal/noise ratio**
=> Control astrophysical backgrounds

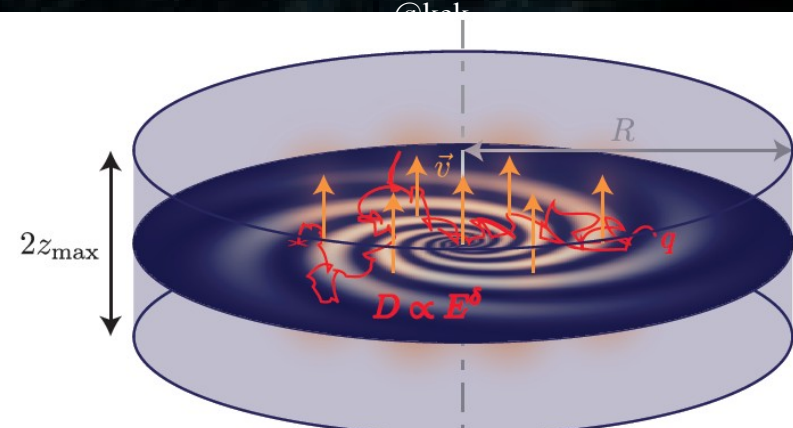
Big DM subhalos

- * **Dwarf Galaxies** (~40) – no other HE astrophysical processes expected there.

Galactic Center

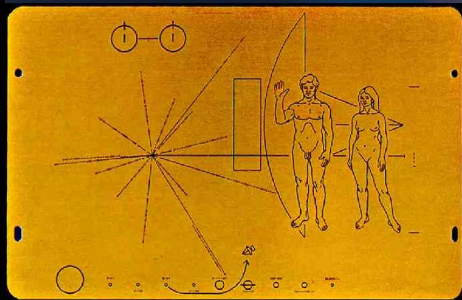
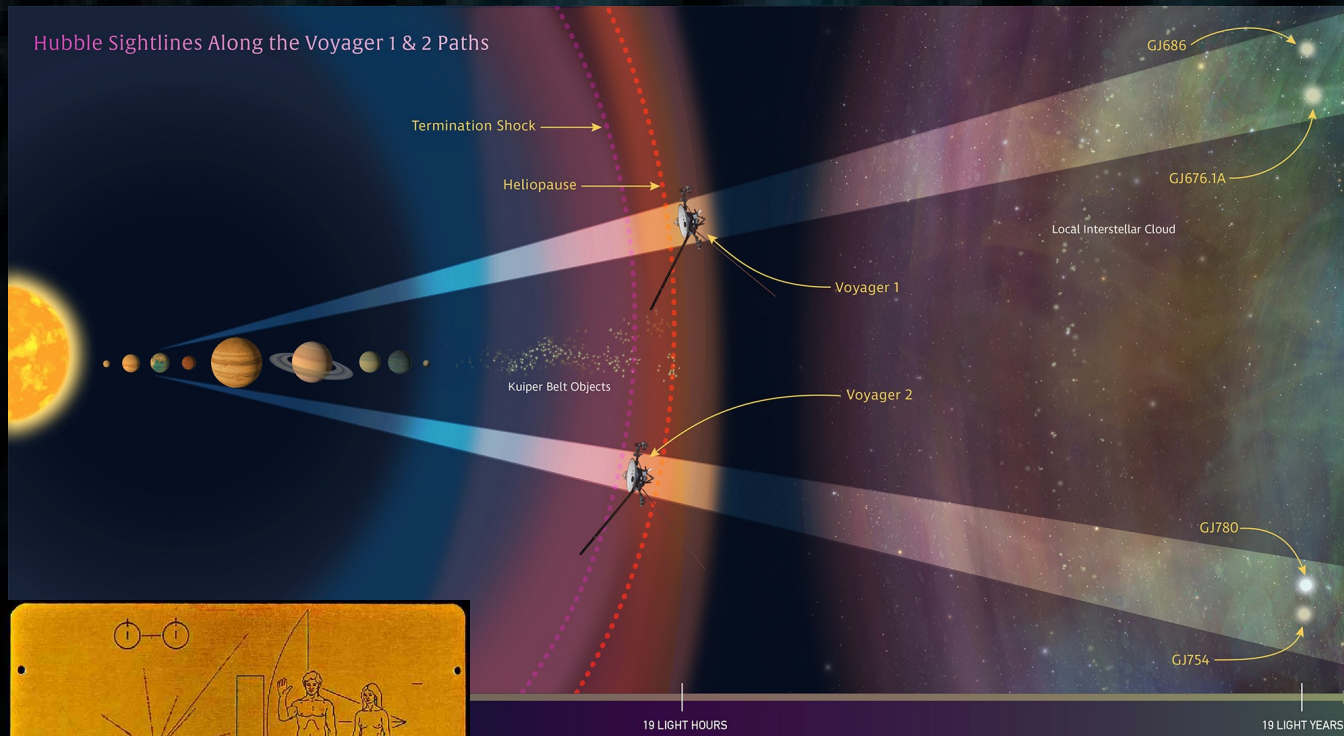
- * Closest/Largest expected annihilation rate
- * **Large theoretical uncertainties** (background not controlled)

Cosmic-ray transport



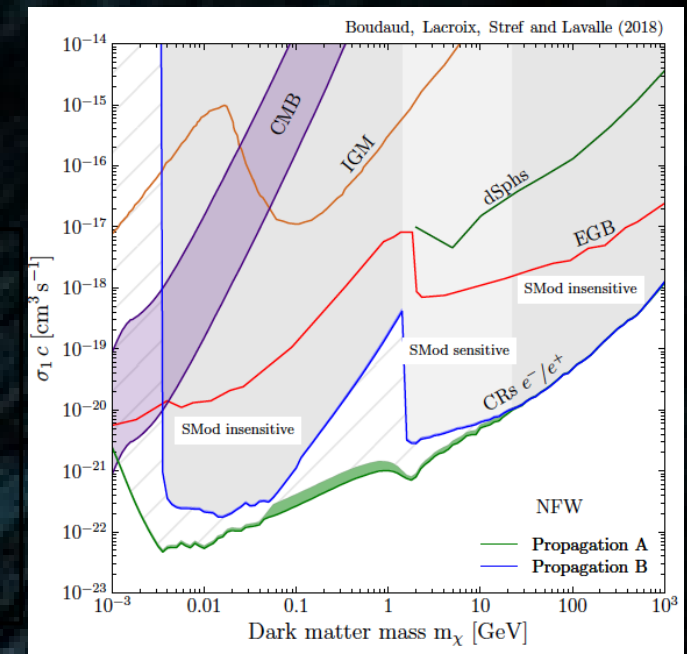
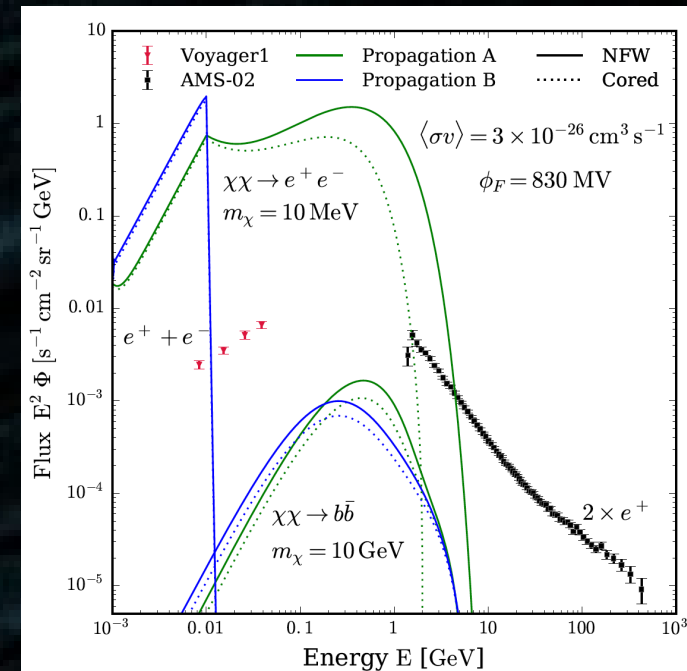
Mertsch PhD thesis '10

Down to MeV DM with cosmic rays + p-wave

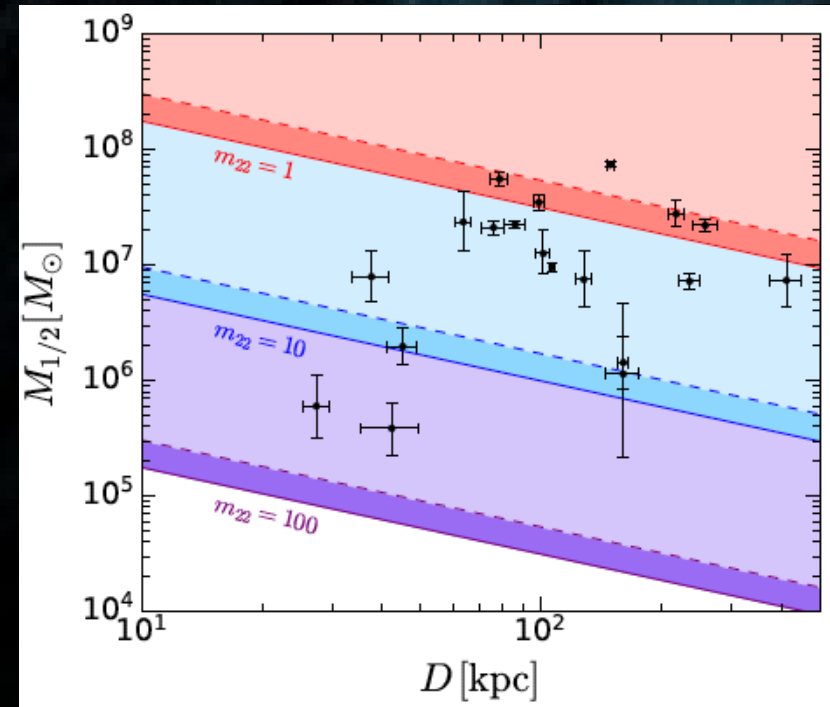


Voyager 1 has passed the heliopause in 2012!
 \Rightarrow cosmic rays no longer shielded by solar magnetic fields
 \Rightarrow use MeV e^+e^- data on tape + AMS-02 beyond
 \Rightarrow Constraints on annihilating MeV dark matter as stringent as those obtained with CMB.

Boudaud+17-18.



ULA probes



Du+18

Tidal disruption of subhalo solitonic cores



Armengaud+'17 (Ly-alpha from SDSS DR9)

Other effects:

- * Sizable oscillations of the core density (Veltmaat+18)
- * $\rho_c = f(r_c)$ (Deng+18)
- * Abundance of ultra-faint lenses HFF@z=6 (Menci+17)
- * Probe incoherent zone (talk by N. Amorisco)
- * Ly-alpha => A catch-22 scenario? (like Maccio+12 for WDM)
- * 21cm? (See Schneider'18)

e.g. Goodmann & Witten '84, Drukier+ '85

Only terms not velocity suppressed ($v \sim 0.001$ c in MW halo)

$$\mathcal{L}_{\text{int}} \supset \left\{ \begin{array}{l} \sum_{\text{quarks}} \left\{ \underbrace{\alpha_v \bar{\chi} \gamma_\mu \chi \bar{q} \gamma^\mu q}_{\text{Dirac WIMPs}} + \alpha_{\text{scal.}} \bar{\chi} \chi \bar{q} q \right\} \\ \sum_{\text{quarks}} \{ \alpha_a \bar{\chi} \gamma_\mu \gamma_5 \chi \bar{q} \gamma^\mu \gamma_5 q \} \end{array} \right\}$$

$$f_n \propto \langle n | \sum_{\text{quarks}} \alpha_q \frac{m_q}{m_n} \bar{q} q | n \rangle$$

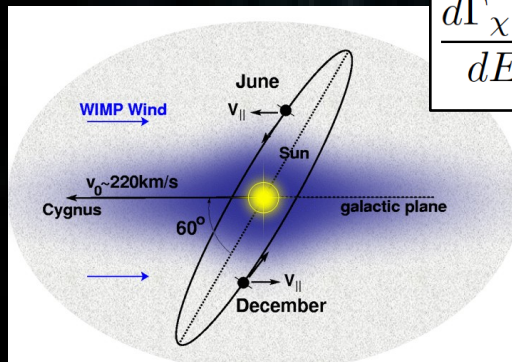
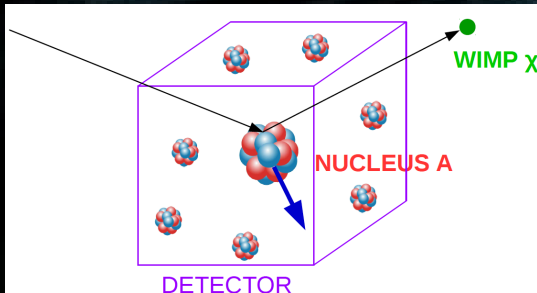
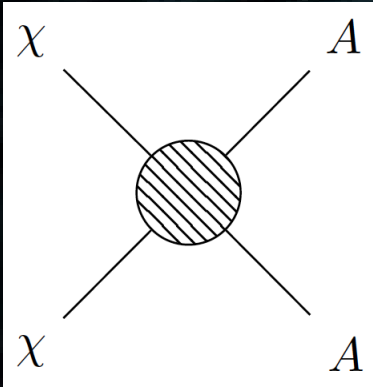
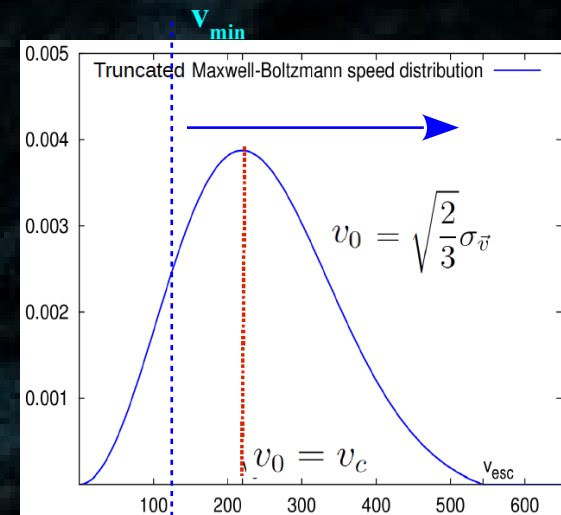
Quark mass content of nucleons:
Lattice QCD calculations
(ongoing)

$$\sigma_{\chi-N} \propto \begin{cases} (Z f_p + (A - Z) f_n)^2 \approx A^2 f_p^2 & (\text{spin-independent}) \\ (a_p \langle S_p \rangle + a_n \langle S_n \rangle)^2 & (\text{spin-dependent}) \end{cases}$$

$$\frac{d\Gamma_{\chi-N}}{dE_r}(E_r, t) = \frac{\sigma_{\chi-N} F^2(E_r)}{2 \mu_r^2} \frac{\rho_\odot}{m_\chi} \int_{v > v_{\min}} d^3 \vec{v} \frac{f(\vec{v}, t)}{v}$$

Astro uncertainties:
* local WIMP phase space
* local DM density

$$v_{\min}(E_r) = \sqrt{\frac{m_N E_r}{2 \mu}}$$



$$\vec{v}_{\text{obs}} = \vec{v}_{\text{halo}} - \{ \vec{v}_{\oplus}(t) \equiv \vec{v}_{\odot} + \vec{v}_{\oplus/\odot}(t) \}$$

Initial statistical/cosmological properties

The initial mass function (linear + ~non-linear)

From primordial spectrum to mass function (ext. Press-Schechter)

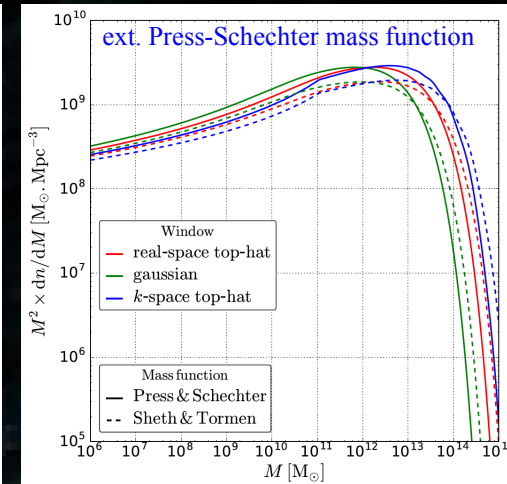
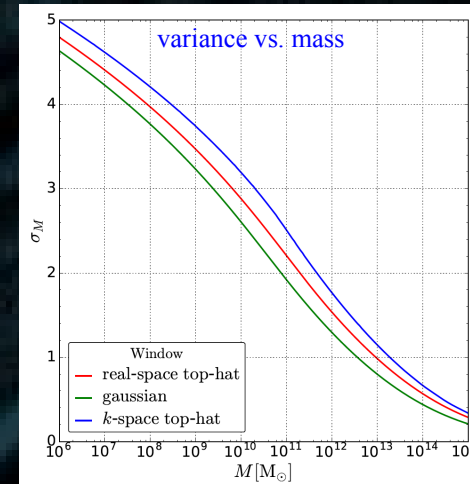
$$P(k, t) = D_+^2(t) \{ P(k) \equiv A_0 T^2(k) P_{\text{prim}}(k) \}$$

$$\sigma^2(R) \equiv \varepsilon_R(|\vec{r}| \rightarrow 0) = \int d \ln k \Delta^2(k) |\tilde{W}(k, R)|^2$$

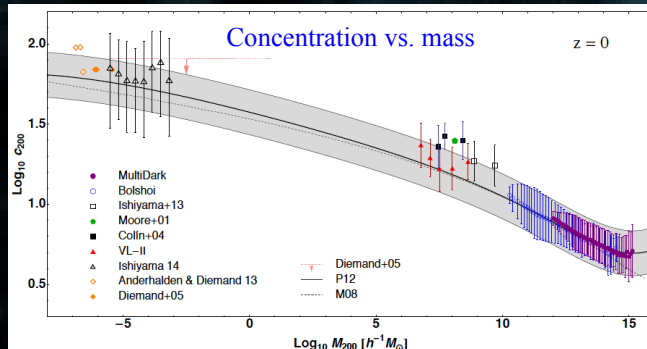
$$\frac{dn}{dM} = \left\{ V_M^{-1} \equiv \frac{\rho_M}{M} \right\} \left| \frac{dF(\delta > \delta_c)}{dM} \right| = \frac{\rho_M}{M^2} \left| \frac{d \ln \sigma}{d \ln M} \right| \nu f(\nu)$$

$$\frac{d\mathcal{P}(m_{200})}{dm_{200}} \propto m_{200}^{-\alpha_m} \left\{ 1 - e^{-\left[\frac{m_{200}}{m_{\text{cut}}} \right]^n} \right\}$$

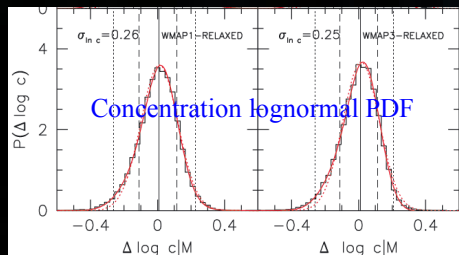
Typically a power law with a cutoff (minimal) mass.



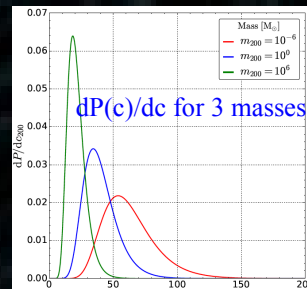
Stref, PhD th. '18



Sanchez-Conde+13



Maccio+08



Stref, PhD th. '18

Concentration function

Traces the density at collapse time.
Modeling based on 2-parameter fit
(Bullock+01, Maccio+08, Prada+12, Dutton+14, etc.)

$$m_{200}(z) = G_z m_*(z_c) \quad \sigma(m_*(z_c)) = \sigma_c^0 D_+(z)$$

$$\bar{c}_{200}(m_{200}, z) = K_{200} \left[\frac{\rho_c(z_c)}{\rho_c(z)} \right]^{1/3}$$

Fitting formula from Sanchez-Conde+13 + lognormal DF

$$\frac{d\mathcal{P}_c}{dc}(c, m) = \frac{1}{K_c} \frac{\exp \left\{ -\frac{(c - \bar{c}(m))^2}{2 \sigma_c^2} \right\}}{c \sqrt{2 \pi \sigma_c^2}}$$